

# Dark Energy and the Cosmic Microwave Background

Ruth Durrer  
Université de Genève  
Département de Physique Théorique et Center for Astroparticle Physics



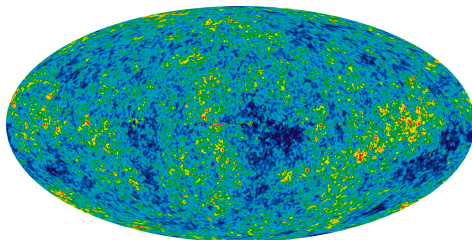
Dark Energy and Simulations

Ringberg June 28, 2012

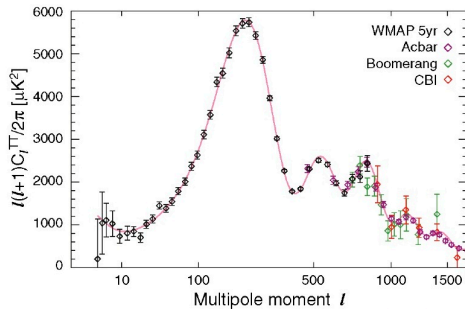
- 1 Introduction
- 2 Dark Energy and the CMB at the last scattering surface
- 3 Dark Energy and the CMB at low redshift
  - ISW
  - CMB lensing
- 4 Conclusions

## The CMB data

WMAP 7 year CMB sky



The WMAP Team



- The CMB data is **precise** and **well understood**.
- Most of it can be calculated within **linear perturbation theory** to **percent accuracy**.
- The resulting anisotropy and polarization spectra depend on **a few cosmological parameters** and **a few parameters describing the initial conditions** of the fluctuations. Which can also be determined accurately.

Minimal  $\Lambda$ CDM parameters (WMAP 7yr + ACT from [Dunkley et al. '11](#))

| Parameter                      |                       |
|--------------------------------|-----------------------|
| $\omega_b \equiv \Omega_b h^2$ | $0.02214 \pm 0.00050$ |
| $\omega_c \equiv \Omega_c h^2$ | $0.1127 \pm 0.0054$   |
| $\Omega_\Lambda$               | $0.721 \pm 0.030$     |
| $n_s$                          | $0.962 \pm 0.013$     |
| $\tau$                         | $0.087 \pm 0.014$     |
| $10^9 \Delta_{\mathcal{R}}^2$  | $2.47 \pm 0.11$       |

- The CMB data is **precise** and **well understood**.
- Most of it can be calculated within **linear perturbation theory** to **percent accuracy**.
- The resulting anisotropy and polarization spectra depend on **a few cosmological parameters** and **a few parameters describing the initial conditions** of the fluctuations. Which can also be determined accurately.

Minimal  $\Lambda$ CDM parameters (WMAP 7yr + ACT from [Dunkley et al. '11](#))

| Parameter                      |                       |
|--------------------------------|-----------------------|
| $\omega_b \equiv \Omega_b h^2$ | $0.02214 \pm 0.00050$ |
| $\omega_c \equiv \Omega_c h^2$ | $0.1127 \pm 0.0054$   |
| $\Omega_\Lambda$               | $0.721 \pm 0.030$     |
| $n_s$                          | $0.962 \pm 0.013$     |
| $\tau$                         | $0.087 \pm 0.014$     |
| $10^9 \Delta_{\mathcal{R}}^2$  | $2.47 \pm 0.11$       |

- The CMB data is **precise** and **well understood**.
- Most of it can be calculated within **linear perturbation theory** to **percent accuracy**.
- The resulting anisotropy and polarization spectra depend on **a few cosmological parameters** and **a few parameters describing the initial conditions** of the fluctuations. Which can also be determined accurately.

Minimal  $\Lambda$ CDM parameters (WMAP 7yr + ACT from [Dunkley et al. '11](#))

| Parameter                      |                       |
|--------------------------------|-----------------------|
| $\omega_b \equiv \Omega_b h^2$ | $0.02214 \pm 0.00050$ |
| $\omega_c \equiv \Omega_c h^2$ | $0.1127 \pm 0.0054$   |
| $\Omega_\Lambda$               | $0.721 \pm 0.030$     |
| $n_s$                          | $0.962 \pm 0.013$     |
| $\tau$                         | $0.087 \pm 0.014$     |
| $10^9 \Delta_{\mathcal{R}}^2$  | $2.47 \pm 0.11$       |

- The CMB data is **precise** and **well understood**.
- Most of it can be calculated within **linear perturbation theory** to **percent accuracy**.
- The resulting anisotropy and polarization spectra depend on **a few cosmological parameters** and **a few parameters describing the initial conditions** of the fluctuations. Which can also be determined accurately.

Minimal  $\Lambda$ CDM parameters (WMAP 7yr + ACT from [Dunkley et al. '11](#))

| Parameter                      |                       |
|--------------------------------|-----------------------|
| $\omega_b \equiv \Omega_b h^2$ | $0.02214 \pm 0.00050$ |
| $\omega_c \equiv \Omega_c h^2$ | $0.1127 \pm 0.0054$   |
| $\Omega_\Lambda$               | $0.721 \pm 0.030$     |
| $n_s$                          | $0.962 \pm 0.013$     |
| $\tau$                         | $0.087 \pm 0.014$     |
| $10^9 \Delta_{\mathcal{R}}^2$  | $2.47 \pm 0.11$       |

Prominent feature in the CMB: peaks from coherent acoustic oscillations of the baryon photon plasma prior to recombination.

- Scale: sound horizon  $r_s(z_*) = (1 + z_*)^{-1} \int_0^{t_*} (1 + z(t)) c_s(t) dt$ , depends on  $\omega_m, \omega_b, \omega_\gamma$ . Angle:  $\theta_S = r_s / D_A(z_*)$ .
- Amplitude:  $\Delta_{\mathcal{R}}^2, n_s, \omega_m$ .
- Relative amplitude of even and odd peaks:  $\omega_b$ .
- Damping envelope:  $\omega_b, n_s$ .
- Relative amplitude of 2nd and 3rd peak:  $\omega_m$ .

Dark energy enters here only over  $D_A(z_*)$ !

$$\begin{aligned} D_A(z_*) &= \frac{1}{1 + z_*} \int_0^{z_*} \frac{dz}{H(z)} \\ &= \frac{h}{H_0(1 + z_*)} \int_0^{z_*} \frac{dz}{\sqrt{\omega_r(1 + z)^4 + \omega_m(1 + z)^3 + \omega_k(1 + z)^2 + \omega_{de}(z)}} \end{aligned}$$

( $h/H_0 = 2998 \text{Mpc}$ ).



Prominent feature in the CMB: peaks from coherent acoustic oscillations of the baryon photon plasma prior to recombination.

- Scale: sound horizon  $r_s(z_*) = (1 + z_*)^{-1} \int_0^{t_*} (1 + z(t)) c_s(t) dt$ , depends on  $\omega_m, \omega_b, \omega_\gamma$ . Angle:  $\theta_S = r_s / D_A(z_*)$ .
- Amplitude:  $\Delta_{\mathcal{R}}^2, n_s, \omega_m$ .
- Relative amplitude of even and odd peaks:  $\omega_b$ .
- Damping envelope:  $\omega_b, n_s$ .
- Relative amplitude of 2nd and 3rd peak:  $\omega_m$ .

Dark energy enters here only over  $D_A(z_*)$ !

$$\begin{aligned} D_A(z_*) &= \frac{1}{1 + z_*} \int_0^{z_*} \frac{dz}{H(z)} \\ &= \frac{h}{H_0(1 + z_*)} \int_0^{z_*} \frac{dz}{\sqrt{\omega_r(1 + z)^4 + \omega_m(1 + z)^3 + \omega_k(1 + z)^2 + \omega_{de}(z)}} \end{aligned}$$

( $h/H_0 = 2998 \text{Mpc}$ ).

Prominent feature in the CMB: peaks from coherent acoustic oscillations of the baryon photon plasma prior to recombination.

- Scale: sound horizon  $r_s(z_*) = (1 + z_*)^{-1} \int_0^{t_*} (1 + z(t)) c_s(t) dt$ , depends on  $\omega_m, \omega_b, \omega_\gamma$ . Angle:  $\theta_S = r_s / D_A(z_*)$ .
- Amplitude:  $\Delta_{\mathcal{R}}^2, n_s, \omega_m$ .
- Relative amplitude of even and odd peaks:  $\omega_b$ .
- Damping envelope:  $\omega_b, n_s$ .
- Relative amplitude of 2nd and 3rd peak:  $\omega_m$ .

Dark energy enters here only over  $D_A(z_*)$ !

$$\begin{aligned} D_A(z_*) &= \frac{1}{1 + z_*} \int_0^{z_*} \frac{dz}{H(z)} \\ &= \frac{h}{H_0(1 + z_*)} \int_0^{z_*} \frac{dz}{\sqrt{\omega_r(1 + z)^4 + \omega_m(1 + z)^3 + \omega_k(1 + z)^2 + \omega_{de}(z)}} \end{aligned}$$

( $h/H_0 = 2998 \text{Mpc}$ ).

Prominent feature in the CMB: peaks from coherent acoustic oscillations of the baryon photon plasma prior to recombination.

- Scale: sound horizon  $r_s(z_*) = (1 + z_*)^{-1} \int_0^{t_*} (1 + z(t)) c_s(t) dt$ , depends on  $\omega_m, \omega_b, \omega_\gamma$ . Angle:  $\theta_S = r_s / D_A(z_*)$ .
- Amplitude:  $\Delta_{\mathcal{R}}^2, n_s, \omega_m$ .
- Relative amplitude of even and odd peaks:  $\omega_b$ .
- Damping envelope:  $\omega_b, n_s$ .
- Relative amplitude of 2nd and 3rd peak:  $\omega_m$ .

Dark energy enters here only over  $D_A(z_*)$ !

$$\begin{aligned} D_A(z_*) &= \frac{1}{1 + z_*} \int_0^{z_*} \frac{dz}{H(z)} \\ &= \frac{h}{H_0(1 + z_*)} \int_0^{z_*} \frac{dz}{\sqrt{\omega_r(1 + z)^4 + \omega_m(1 + z)^3 + \omega_k(1 + z)^2 + \omega_{de}(z)}} \end{aligned}$$

( $h/H_0 = 2998 \text{Mpc}$ ).

Prominent feature in the CMB: peaks from coherent acoustic oscillations of the baryon photon plasma prior to recombination.

- Scale: sound horizon  $r_s(z_*) = (1 + z_*)^{-1} \int_0^{t_*} (1 + z(t)) c_s(t) dt$ , depends on  $\omega_m, \omega_b, \omega_\gamma$ . Angle:  $\theta_S = r_s / D_A(z_*)$ .
- Amplitude:  $\Delta_{\mathcal{R}}^2, n_s, \omega_m$ .
- Relative amplitude of even and odd peaks:  $\omega_b$ .
- Damping envelope:  $\omega_b, n_s$ .
- Relative amplitude of 2nd and 3rd peak:  $\omega_m$ .

Dark energy enters here only over  $D_A(z_*)$ !

$$\begin{aligned} D_A(z_*) &= \frac{1}{1 + z_*} \int_0^{z_*} \frac{dz}{H(z)} \\ &= \frac{h}{H_0(1 + z_*)} \int_0^{z_*} \frac{dz}{\sqrt{\omega_r(1 + z)^4 + \omega_m(1 + z)^3 + \omega_k(1 + z)^2 + \omega_{de}(z)}} \end{aligned}$$

( $h/H_0 = 2998 \text{Mpc}$ ).

Prominent feature in the CMB: peaks from coherent acoustic oscillations of the baryon photon plasma prior to recombination.

- Scale: sound horizon  $r_s(z_*) = (1 + z_*)^{-1} \int_0^{t_*} (1 + z(t)) c_s(t) dt$ , depends on  $\omega_m, \omega_b, \omega_\gamma$ . Angle:  $\theta_S = r_s / D_A(z_*)$ .
- Amplitude:  $\Delta_{\mathcal{R}}^2, n_s, \omega_m$ .
- Relative amplitude of even and odd peaks:  $\omega_b$ .
- Damping envelope:  $\omega_b, n_s$ .
- Relative amplitude of 2nd and 3rd peak:  $\omega_m$ .

Dark energy enters here only over  $D_A(z_*)$ !

$$\begin{aligned} D_A(z_*) &= \frac{1}{1 + z_*} \int_0^{z_*} \frac{dz}{H(z)} \\ &= \frac{h}{H_0(1 + z_*)} \int_0^{z_*} \frac{dz}{\sqrt{\omega_r(1 + z)^4 + \omega_m(1 + z)^3 + \omega_k(1 + z)^2 + \omega_{de}(z)}} \end{aligned}$$

( $h/H_0 = 2998 \text{Mpc}$ ).

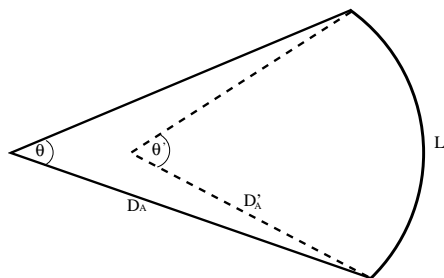
Prominent feature in the CMB: peaks from coherent acoustic oscillations of the baryon photon plasma prior to recombination.

- Scale: sound horizon  $r_s(z_*) = (1 + z_*)^{-1} \int_0^{t_*} (1 + z(t)) c_s(t) dt$ , depends on  $\omega_m, \omega_b, \omega_\gamma$ . Angle:  $\theta_S = r_s / D_A(z_*)$ .
- Amplitude:  $\Delta_{\mathcal{R}}^2, n_s, \omega_m$ .
- Relative amplitude of even and odd peaks:  $\omega_b$ .
- Damping envelope:  $\omega_b, n_s$ .
- Relative amplitude of 2nd and 3rd peak:  $\omega_m$ .

Dark energy enters here only over  $D_A(z_*)$ !

$$\begin{aligned} D_A(z_*) &= \frac{1}{1 + z_*} \int_0^{z_*} \frac{dz}{H(z)} \\ &= \frac{h}{H_0(1 + z_*)} \int_0^{z_*} \frac{dz}{\sqrt{\omega_r(1 + z)^4 + \omega_m(1 + z)^3 + \omega_k(1 + z)^2 + \omega_{de}(z)}} \end{aligned}$$

( $h/H_0 = 2998 \text{Mpc}$ ).



(from  
Vonlanthen, Räsänen & RD '10)

$$\begin{aligned}
 C(\theta) \equiv \langle \Delta T(\mathbf{n}_1) \Delta T(\mathbf{n}_2) \rangle &= \frac{1}{4\pi} \sum_{\ell} (2\ell + 1) C_{\ell} P_{\ell}(\cos \theta) \\
 &= \frac{1}{4\pi} \sum_{\ell} (2\ell + 1) C'_{\ell} P_{\ell}(\cos \theta') = C'(\theta')
 \end{aligned}$$

$$\text{For } \ell \gtrsim 20 \quad C_{\ell} = \left( \frac{D'_A}{D_A} \right)^2 C'_{\frac{D'_A}{D_A} \ell} .$$

In [Vonlanthen, Räsänen & RD '10](#) we have studied how well we can fit the CMB with a cosmological model which is Einstein de Sitter up to last scattering and the distance to last scattering is arbitrary,  $D_A = S D_{A,EdS}$ .

Features on the lss are then simply seen under a different angle,

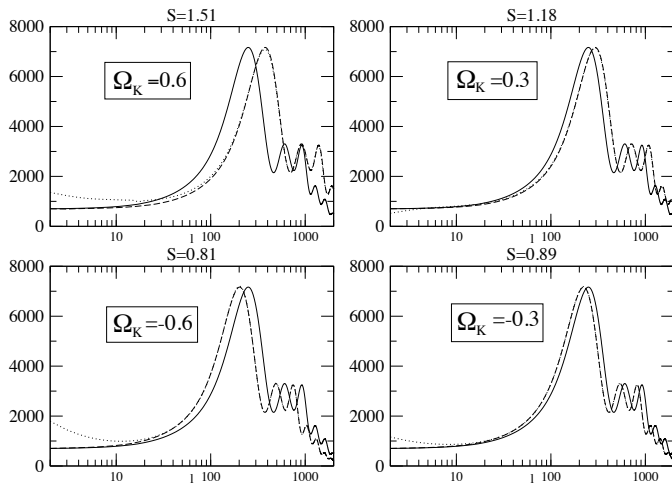
$$C_\ell = S^{-2} C_{S^{-1}\ell}^{EdS}.$$

With this we can fit all present CMB data with  $\ell \gtrsim 40$ .

$\Rightarrow$  CMB data with  $\ell > 40$  measures very precisely  $\omega_b$ ,  $\omega_m$ ,  $n_s$  and  $D_A(z_*)$  or  $S$ , but it cannot determine the nature of dark energy.

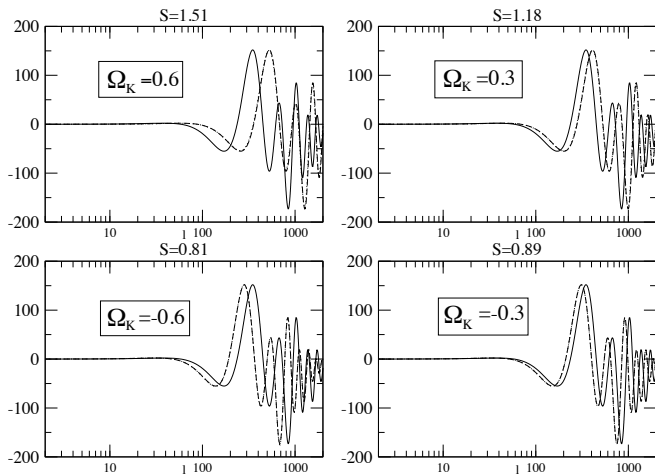


# Scaled spectra from curved cosmologies



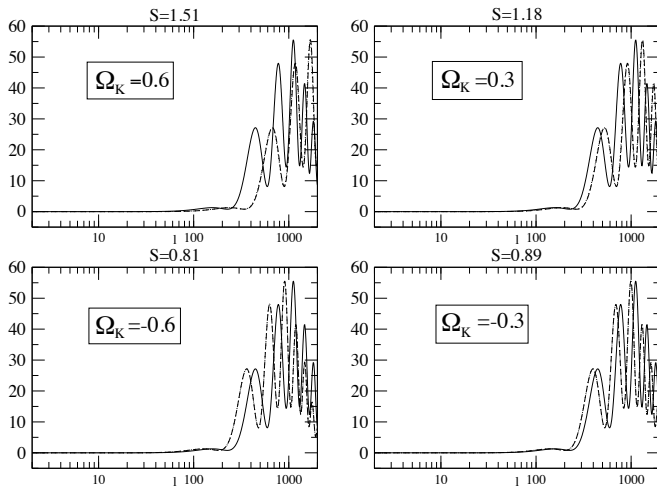
(from Vonlanthen, Räsänen & RD '10)

# Scaled spectra from curved cosmologies



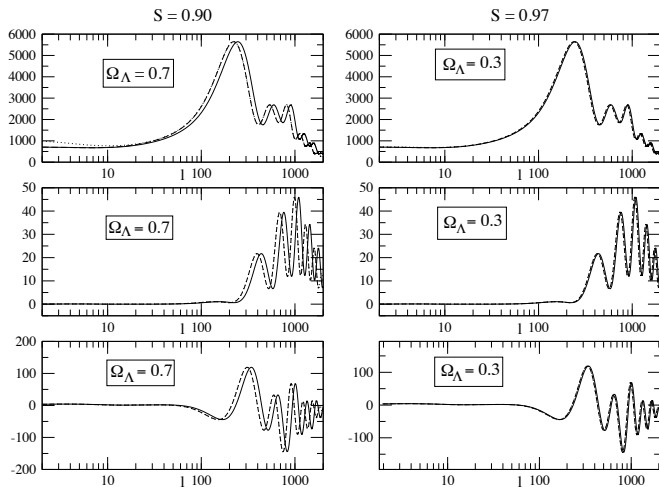
(from Vonlanthen, Räsänen & RD '10)

# Scaled spectra from curved cosmologies



(from Vonlanthen, Räsänen & RD '10)

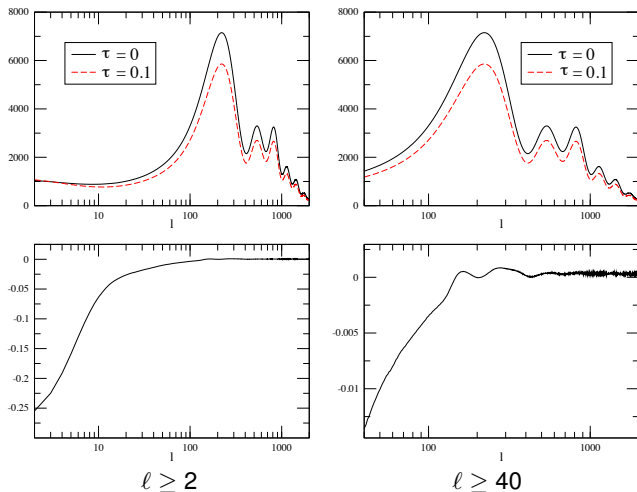
# Scaled spectra from $\Lambda$ cosmologies



(from Vonlanthen, Räsänen & RD '10)

# Reionization

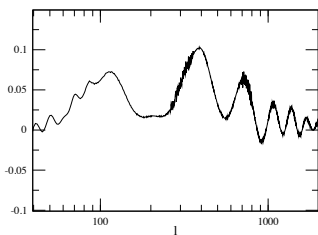
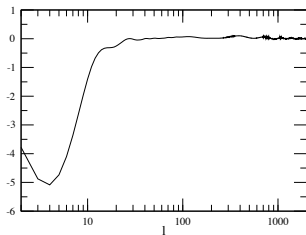
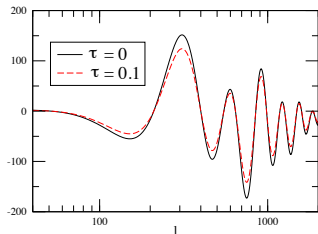
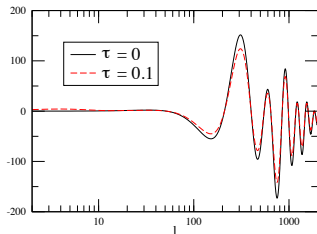
TT



(from Vonlanthen, Räsänen & RD '10)

# Reionization

TE



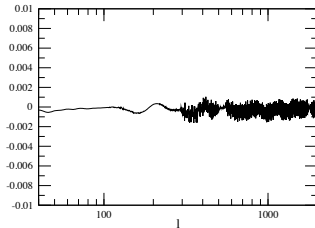
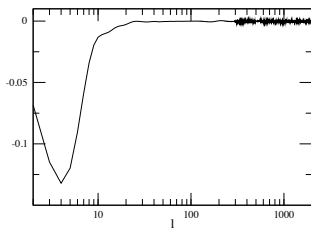
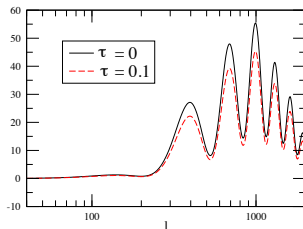
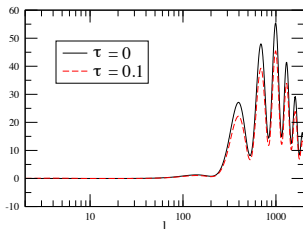
$\ell \geq 2$

$\ell \geq 40$

(from [Vonlanthen, Räsänen & RD '10](#))

# Reionization

EE

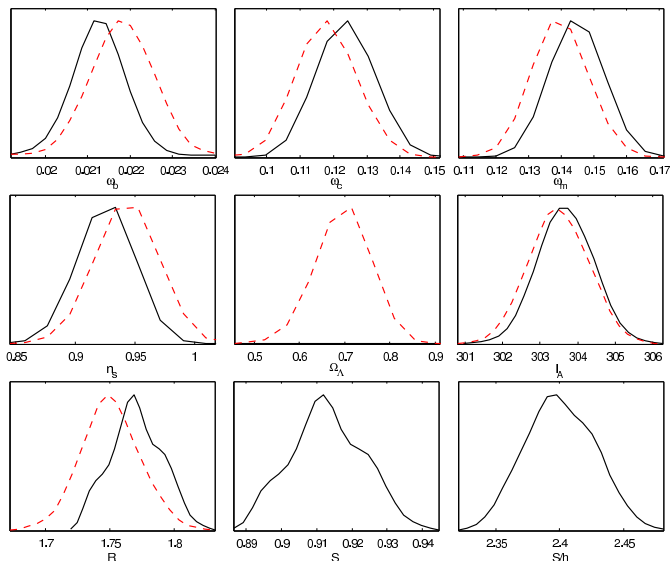


$\ell \geq 2$

$\ell \geq 40$

(from Vonlanthen, Räsänen & RD '10)

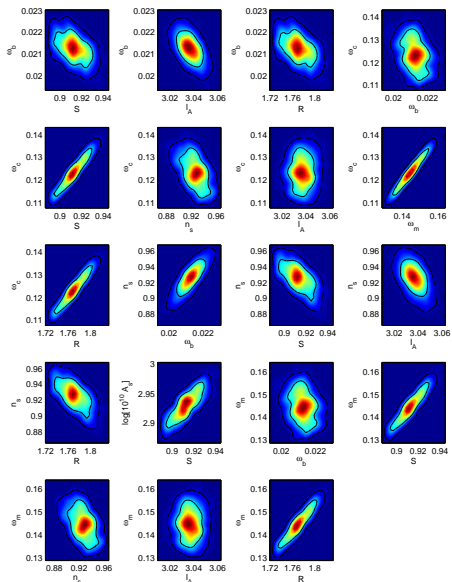
# Cosmological parameters



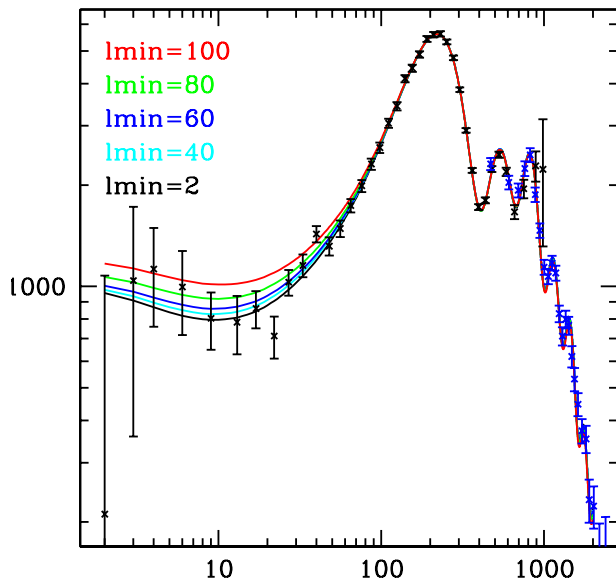
(from Vonlanthen, Räsänen & RD '10)



# Cosmological parameters



(from  
Vonlanthen, Räsänen & RD '10)



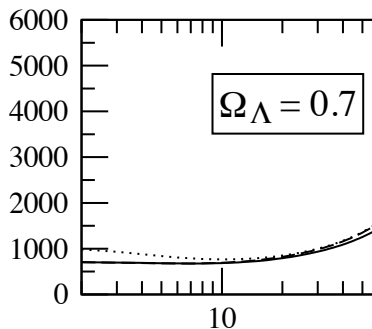
(from [Vonlanthen, Räsänen & RD '10](#))

## The integrated Sachs Wolfe effect (ISW)

On there way into our telescope CMB photons loose/gain energy if they move through a time-dependent gravitational potential:

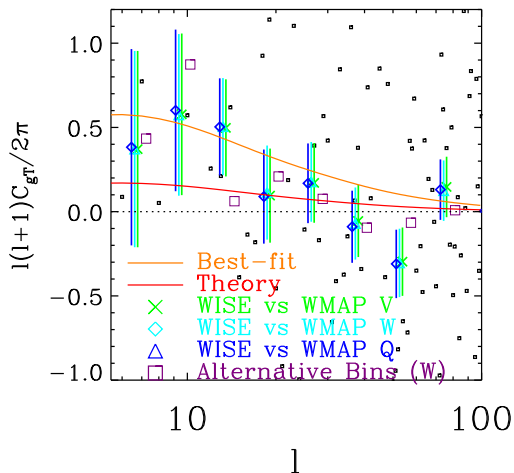
$$\left(\frac{\Delta T}{T}\right)_{ISW}(\mathbf{n}) = \int_{t_0}^{t_*} \partial_t(\Phi + \Psi)(t, \mathbf{x}(t)) dt$$

In a flat pure matter Universe  $\partial_t \Psi = \partial_t \Phi = 0$ . When  $\Lambda$  takes over, the gravitational potentials decay.



# ISW from correlation with LSS

Correlation of the WISE (wide field infrared survey explorer) with WMAP 7year.  
A  $3.1\sigma$  detection.

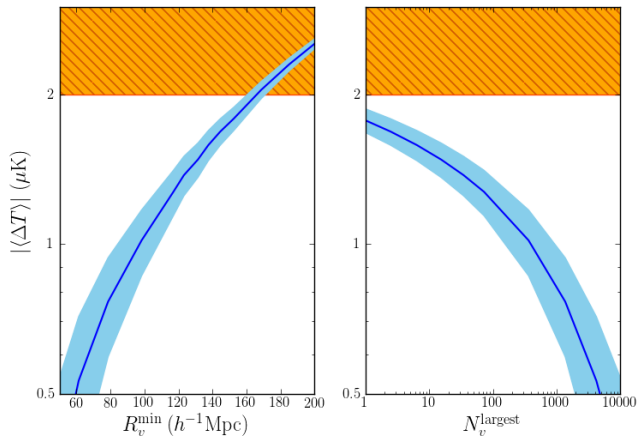


(from Goto, Szapudi & Granett '11)

# Is the detected ISW too large?

measured  $\Rightarrow$

simulated  $\Rightarrow$

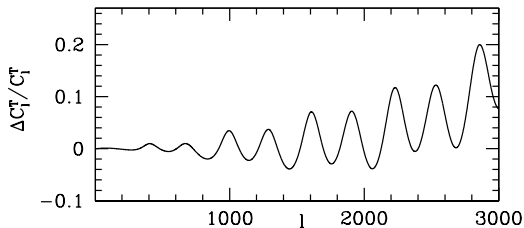
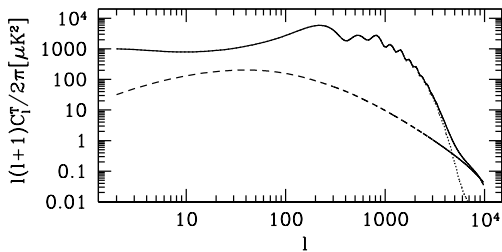


(from Nadatur, Hotschkiss & Sarkar '11)

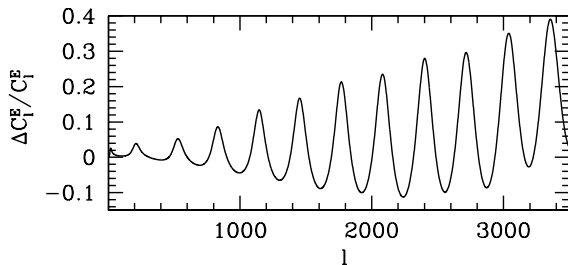
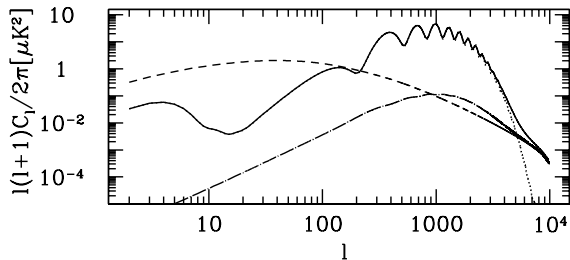
# CMB lensing

On their path into our antennas, CMB photons are deflected by the gravitational potential of the large scale matter distribution, the lensing potential:

$$\psi(\mathbf{n}) = \int_0^{\eta_0 - \eta_*} dr \frac{r_* - r}{rr_*} (\Phi + \Psi)(\eta_0 - r, \mathbf{n}r)$$



# CMB lensing



- The strongest signal of dark energy in the CMB is via its effect on the **distance to the lss,  $D_A(z_*)$** .
  - At present this is the only signal of dark energy safely (more than  $5\sigma$  significance) detected in the CMB.
  - **One can fit the observed data perfectly well without dark energy by a simple rescaling of  $D_A(z_*)$**  for  $\ell > 20$ . We found  $2\Delta \log \mathcal{L} = 22$  (2591 data points) for  $\ell_{\min} = 2$  and  $2\Delta \log \mathcal{L} \lesssim 1$  for  $\ell_{\min} \geq 20$ .
  - The ISW expected for  $\Lambda$ CDM is detected at about  $(3-4)\sigma$  by several experiments but it seems rather high.
  - **CMB lensing** is another effect which contains information about dark energy and, especially **modified gravity** which will be explored in future high precision CMB experiments.
-



# Conclusions

- The strongest signal of dark energy in the CMB is via its effect on the **distance to the lss,  $D_A(z_*)$** .
  - At present this is the only signal of dark energy safely (more than  $5\sigma$  significance) detected in the CMB.
  - One can fit the observed data perfectly well without dark energy by a simple rescaling of  $D_A(z_*)$  for  $\ell > 20$ . We found  $2\Delta \log \mathcal{L} = 22$  (2591 data points) for  $\ell_{\min} = 2$  and  $2\Delta \log \mathcal{L} \lesssim 1$  for  $\ell_{\min} \geq 20$ .
  - The ISW expected for  $\Lambda$ CDM is detected at about  $(3-4)\sigma$  by several experiments but it seems rather high.
  - **CMB lensing** is another effect which contains information about dark energy and, especially **modified gravity** which will be explored in future high precision CMB experiments.
-

# Conclusions

- The strongest signal of dark energy in the CMB is via its effect on the **distance to the lss,  $D_A(z_*)$** .
  - At present this is the only signal of dark energy safely (more than  $5\sigma$  significance) detected in the CMB.
  - **One can fit the observed data perfectly well without dark energy by a simple rescaling of  $D_A(z_*)$  for  $\ell > 20$** . We found  $2\Delta \log \mathcal{L} = 22$  (2591 data points) for  $\ell_{\min} = 2$  and  $2\Delta \log \mathcal{L} \lesssim 1$  for  $\ell_{\min} \geq 20$ .
  - The ISW expected for  $\Lambda$ CDM is detected at about  $(3-4)\sigma$  by several experiments but it seems rather high.
  - **CMB lensing** is another effect which contains information about dark energy and, especially **modified gravity** which will be explored in future high precision CMB experiments.
-

# Conclusions

- The strongest signal of dark energy in the CMB is via its effect on the **distance to the lss,  $D_A(z_*)$** .
  - At present this is the only signal of dark energy safely (more than  $5\sigma$  significance) detected in the CMB.
  - **One can fit the observed data perfectly well without dark energy by a simple rescaling of  $D_A(z_*)$  for  $\ell > 20$** . We found  $2\Delta \log \mathcal{L} = 22$  (2591 data points) for  $\ell_{\min} = 2$  and  $2\Delta \log \mathcal{L} \lesssim 1$  for  $\ell_{\min} \geq 20$ .
  - The ISW expected for  $\Lambda$ CDM is detected at about  $(3-4)\sigma$  by several experiments but it seems rather high.
  - **CMB lensing** is another effect which contains information about dark energy and, especially **modified gravity** which will be explored in future high precision CMB experiments.
-

- The strongest signal of dark energy in the CMB is via its effect on the **distance to the lss,  $D_A(z_*)$** .
  - At present this is the only signal of dark energy safely (more than  $5\sigma$  significance) detected in the CMB.
  - **One can fit the observed data perfectly well without dark energy by a simple rescaling of  $D_A(z_*)$**  for  $\ell > 20$ . We found  $2\Delta \log \mathcal{L} = 22$  (2591 data points) for  $\ell_{\min} = 2$  and  $2\Delta \log \mathcal{L} \lesssim 1$  for  $\ell_{\min} \geq 20$ .
  - The ISW expected for  $\Lambda$ CDM is detected at about  $(3-4)\sigma$  by several experiments but it seems rather high.
  - **CMB lensing** is another effect which contains information about dark energy and, especially **modified gravity** which will be explored in future high precision CMB experiments.
-