ALMA observations of NGC 6334S. II. Subsonic and Transonic Narrow Filaments in a High-mass Star Formation Cloud

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31 ABSTRACT	
²² We present a study of narrow filaments toward a massive infrared dark cloud NGC 6334S	using
the Atacama Large Millimeter/submillimeter Array (ALMA) Thirteen gas filaments are ide	ntified
using the $H^{13}CO^+$ line while a single continuum filament is revealed by the continuum emission	The
filaments present a compact radial distribution with a median filament width of ~ 0.04 pc ps	rrower

than the previously proposed 'quasi-universal' 0.1 pc filament width. The higher spatial resolution

observations and higher-density gas tracer tend to identify even narrower and lower mass filaments.

The filament widths are roughly twice the size of embedded cores. The gas filaments are largely

supported by thermal motions. The nonthermal motions are predominantly subsonic and transonic
in both identified gas filaments and embedded cores, which may imply that stars are likely born in
environments of low turbulence. A fraction of embedded objects show a narrower velocity dispersion
compared with their corresponding natal filaments, which may indicate that the turbulent dissipation
is taking place in these embedded cores. The physical properties (mass, mass per unit length, gas
kinematics, and width) of gas filaments are analogous to those of narrow filaments found in low- to
high-mass star-forming regions. The more evolved sources are found to be farther away from the

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filaments, a situation that may have resulted from the relative motions between the YSOs and their natal filaments.

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1. INTRODUCTION

Filamentary structures of interstellar medium (ISM) 52 are prevalent in nearby Gould Belt molecular clouds 53 and also more distant molecular clouds as seen in re-54 cent Galactic plane surveys from far-infrared to centime-55 ter wavelengths and in both continuum and molecular 56 line emission (Churchwell et al. 2009; André et al. 2010; 57 Molinari et al. 2010; Arzoumanian et al. 2011; Good-58 man et al. 2014; Wang et al. 2015; Zucker et al. 2015; 59 Contreras et al. 2016; Li et al. 2016; Soler et al. 2020; 60 Wang et al. 2020). These filaments show wide ranges 61 of physical properties (e.g., length, width, mass, length-62 to-width aspect ratios, and masses per unit length) that 63 can vary over an order of magnitude across the revealed 64 filaments. 65

Similar filamentary structures are also commonly seen 66 in both numerical hydrodynamic (HD) and magneto-67 hydrodynamic (MHD) simulations of the ISM (e.g., 68 Padoan et al. 2007; Heitsch et al. 2008; Gong & Ostriker 69 2011; Hennebelle 2013; Gómez & Vázquez-Semadeni 70 2014). Several mechanisms have been proposed for the 71 formation of filaments in molecular clouds, such as gravi-72 tational instability (gravitational fragmentation and col-73 lapse) of sheet-like and elongated clouds (Miyama et al. 74 1987; Nagai et al. 1998; Hartmann & Burkert 2007; Hen-75 nebelle 2013; Gómez & Vázquez-Semadeni 2014; Van 76 Loo et al. 2014), cloud collision (Padoan et al. 2001), 77 and shocked flows (Gong & Ostriker 2011; Chen et al. 78 2020). 79

In dense and self-gravitating clouds, filaments often 80 exhibit cylindrical morphologies. (e.g., Taurus B213; Li 81 & Goldsmith 2012). Large scale filaments often har-82 bor parsec-scale dense massive clumps that become the 83 fertile ground of massive star and cluster formation 84 (Zhang et al. 2009; Jiménez-Serra et al. 2014; Wang 85 et al. 2014; Busquet et al. 2016), although not all fil-86 aments show signs of star-formation activity (e.g., only 87 pre-stellar cores are detected in Polaris flare; Miville-88 Deschênes et al. 2010). The embedded dense cores 89 that are precursors of stars can be formed in the high-90 est density regions of the filament via contraction by 91 self-gravity and local kinematic processes (Inutsuka & 92 Miyama 1992; Hartmann & Burkert 2007; Heitsch et al. 93 2008, 2009; Nakamura & Li 2008; Myers 2009; Gong 94 & Ostriker 2011). The prestellar cores and protostel-95

⁹⁶ lar cores are primarily found to reside in dense filamentary structures with supercritical mass per unit length in 97 both low- and high-mass star-forming molecular clouds 98 (André et al. 2014; Chung et al. 2019; Treviño-Morales 99 et al. 2019), and most of them are believed to have 100 formed by cloud collapse and/or fragmentation along 101 filaments (Men'shchikov et al. 2010; André et al. 2014; 102 Henshaw et al. 2014; Peretto et al. 2014; Beuther et al. 103 2015; Könyves et al. 2015; Clarke et al. 2017). The gas 104 flows along filaments can continuously supply the mate-105 rial for cores to grow in mass (Liu et al. 2012; Kirk et al. 106 2013; Lin et al. 2017; Yuan et al. 2018; Lu et al. 2018; 107 Liu et al. 2019; Treviño-Morales et al. 2019; Sanhueza 108 et al. 2021). 109

Recently, ALMA high angular resolution observations 110 ¹¹¹ reveal that narrow (i.e., filament widths of a few 0.01 pc) filamentary structures (or "fibers" in Hacar et al. 112 2018), are found in some high-mass star-forming clouds 113 (e.g., Orion, G035.39-00.33, and G14.225-0.506; Hen-114 shaw et al. 2014; Hacar et al. 2018; Monsch et al. 2018; 115 Chen et al. 2019b, and references therein). These fil-116 aments are much narrower than the 'quasi-universal' 117 0.1 pc filament width proposed by previous studies using 118 Herschel observations (e.g., André et al. 2014; Arzouma-119 nian et al. 2019, and references therein), and appear to 120 be intimately linked to dense cores (Hacar et al. 2018). 121 122 However, whether such narrow filamentary structures are ubiquitous in high-mass star formation clouds, and 123 what their properties are remain controversial topics to 124 be more fully explored. 125

To understand the nature of filaments and embed-126 ded dense cores in massive star formation regions, we 127 have carried out high angular resolution observations to-128 ward a filamentary infrared dark cloud, NGC 6334S, us-129 ing the Atacama Large Millimeter/submillimeter Array 130 (ALMA). NGC 6334S is located at the southwestern end 131 of the NGC 6334 molecular cloud complex (Figure 1), 132 which is a nearby (1.3 kpc) young and massive "mini-133 starburst" region (Chibueze et al. 2014; Willis et al. 134 2013). In contrast to the well-known infrared bright OB 135 cluster-forming clumps NGC 6334I/I(N)/II/III/IV/V 136 (Persi & Tapia 2008; Russeil et al. 2013), NGC 6334S 137 in some areas is dark in the infrared at wavelengths up 138 to 70 μ m (see Figure 1 of Li et al. 2020a, hereafter 139 ¹⁴⁰ Paper I), signalling its youth. NGC 6334S has a mass

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of $\sim 1390 \,\mathrm{M_{\odot}}$ (Paper I), which is comparable to the 141 clumps with embedded massive protostars and proto-142 clusters elsewhere in the complex, and therefore has the 143 potential to form massive stars together with lower-mass 144 star clusters. Thus NGC 6334S provides an ideal labora-145 tory to investigate the early evolutionary stages of clus-146 ter formation in filamentary clouds. We will use dense 147 gas tracers and continuum emission not only to iden-148 tify the filamentary structures in the position-position-149 velocity (PPV) space but also to study the physical 150 properties (e.g., gas kinematics, mass, structure profile) 151 of both filaments and dense cores, in order to understand 152 the initial cloud environment of filament-based cluster 153 formation. 154

We recently identified 49 continuum dense cores (here-155 after continuum cores, named respectively #1, #2, #3156 ...) using our 3 mm continuum image (Paper I) and 157 found 17 starless cores (hereafter NH_2D cores, namely 158 M1, M2, M3 ...) using the NH₂D line emission (Li et al. 159 2021, hereafter Paper II). These NH_2D cores are nei-160 ther associated with continuum cores nor with Class I/II 161 young stellar objects (YSOs; Willis et al. 2013). For sim-162 plicity, we refer to continuum cores and NH₂D cores as 163 dense cores. The derived masses of dense cores range 164 from 0.13 to 14.1 M_{\odot} , with the mean and median values 165 of 1.8 and 0.8 M_{\odot} , respectively. The sizes of dense cores 166 are between 0.01 and 0.04 pc, with the mean and me-167 dian values of 0.018 and 0.017 pc, respectively. Paper I 168 also shows that the nonthermal motions are predomi-169 nantly subsonic and transonic throughout NGC 6334S 170 and that the external pressure is important in confining 171 the embedded objects. Paper II reported the presence of 172 cluster of low-mass starless and pre-stellar cores that 173 а show small velocity dispersions, a high fractional abun-174 dance of NH₂D, high NH₃ deuterium fractionation, and 175 are dark at infrared wavelengths to 70 μ m. In at least 176 some of the NH_2D cores, turbulence seems dissipated 177 and the gas kinematics is dominated by thermal mo-178 tions. 179

In this work, we focus on filaments and investigate 180 their properties as well as the relationship between fila-181 ments and dense cores. The observations are described 182 in Section 2. Then, we describe the filament identifi-183 cation and the properties of identified filaments in Sec-184 tion 3. We discuss in detail the properties of filaments 185 and dense objects in Section 4. Finally, we summarize 186 our main findings in Section 5. 187

2. OBSERVATION

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We have carried out a 55-pointings mosaic observation with ALMA 12m array towards the massive infrared dark cloud (IRDC) NGC 6334S between March 13 and

21 of 2017 (ID: 2016.1.00951.S). Two 234.4 MHz wide 192 spectral windows were employed to cover the $H^{13}CO^+$ 193 (1-0, 86.7 GHz) and NH_2D $(1_{1,1} - 1_{0,1}, 85.9 \text{ GHz})$ lines 194 with a 0.061 MHz spectral resolution ($\sim 0.21 \text{ km s}^{-1}$ at 195 86 GHz). In addition, three 1.875 GHz wide spectral 196 windows centered at 88.5 GHz, 98.5 GHz, and 100.3 197 GHz with a spectral resolution of 0.977 MHz (~ 3.0 – 198 3.3 km s^{-1}) were used to take broad band continuum 199 data. More details on the observations can be found in 200 Paper I. 201

Data calibration was performed using the CASA 4.7.0 202 software package (McMullin et al. 2007). Both con-203 tinuum and line images were iteratively cleaned with manual masking via the *clean* task down to $\sim 3\sigma$ using the multiscale deconvolver and a robust weighting 206 of 0.5. The resultant continuum and line images have 207 a synthesized beam of $\theta_{\rm mai} \times \theta_{\rm min} = 3^{\prime\prime}.6 \times 2^{\prime\prime}.4$ (or 208 0.023×0.015 pc, with a position angle P.A = 81°) 209 and $\theta_{maj} \times \theta_{min} = 4''.1 \times 2''.8$ (or 0.026 × 0.018 pc, 210 $P.A = 83^{\circ}$), respectively. The achieved 1σ root mean 211 $_{212}$ square (rms) noise levels are 0.3 mJy beam⁻¹ for the continuum image and $\sim 6 \text{ mJy beam}^{-1} \text{ per } 0.21 \text{ km s}^{-1}$ 213 for the spectral line images. The maximum recoverable 214 scale (MRS) of single pointing reaches up to $\sim 30''$ in the 215 ALMA data. All images shown in this paper are prior to 216 primary beam correction. The measured fluxes for mass 217 estimation have the primary beam correction applied. 218

3. RESULTS AND ANALYSIS

NGC 6334S is mostly dark at infrared wavelengths to 70 μ m indicating its early evolutionary stage. (e.g., Sanhueza et al. 2013, 2019; Tan et al. 2013; Contreras et al. 2018; Sanhueza et al. 2017; Li et al. 2019a; Morii et al. 2024 2021). Figure 1 shows an overview of the NGC 6334 molecular cloud complex in the far-infrared and the location of NGC 6334S.

3.1. Molecular Lines Emission

The rotational transitions of several molecular species 228 (i.e., HCO⁺ (1–0), HCN (1–0), CS (2–1), HNCO (4_{0.4} – 229 $3_{0,3}$), H¹⁵NC (1–0), CH₃OH (5_{1,4} – 4_{1,3}), SO (2₂ – 1₁), 230 HC_3N (11–10)) were detected with a coarse spectral res-231 olution of 0.977 MHz (or $\sim 3.0 - 3.3 \text{ km s}^{-1}$). However 232 with these low spectral resolution data we are not able 233 to determine the kinematic properties of the molecular 234 gas. Therefore, only the high spectral resolution (0.061)235 MHz ~ 0.21 km s⁻¹) data of the H¹³CO⁺ (1-0) and 236 NH_2D $(1_{1,1} - 1_{0,1})$ lines will be used as diagnostics of 237 the kinematic properties of the filaments in this work. 238

Figures 1 and 2 show the $\rm H^{13}CO^+$ line, continuum, and NH₂D line emission. The $\rm H^{13}CO^+$ (1-0; critical density $n_{\rm cr} \sim 10^5 \rm \ cm^{-3}$) line traces spatially much more



Figure 1. Panel a: three-color Herschel composite image of NGC 6334 molecular cloud complex with blue, green, and red for $\lambda = 70, 160, \text{ and } 350 \ \mu\text{m}$, respectively. The scale bar (5 pc at the distance of 1.3 kpc), the Equatorial and the Galactic cardinal directions are shown on the upper right hand of the image. The white box presents the NGC 6334S region. Six bright infrared (IR) clumps (I, IN, II, III, IV, and V) are marked in the image (McBreen et al. 1979). Two O type stars (O7.5 and O6.5) are marked with blue cross "x" symbols (Persi & Tapia 2008). Panel b: the filament spines (color solid curves) overlaid on the peak intensity ($I_{\text{H}^{13}\text{CO}^+}$; the maximum intensity of the spectrum) image of H^{13}CO^+ line emission. Magenta open squares correspond to the 49 continuum cores identified by the ALMA 3mm continuum image (Paper I). Blue open triangles show the 17 NH₂D cores revealed by the NH₂D line emission (Paper II). The red cross "x" and yellow plus "+" symbols correspond to the 25 Class I and 58 Class II YSOs (Willis et al. 2013), respectively. The beam size (blue filled ellipse) of the H¹³CO⁺ image is shown in the bottom left of the panel.

extended gaseous structures than the NH_2D (1_{1,1} - 1_{0,1}; $n_{\rm cr} \sim 10^6 {\rm ~cm^{-3}}$) line since their critical densities are 243 different by nearly an order-of-magnitude. The NH₂D 244 emission appears preferentially toward the location of 245 dense cores. In addition, the $H^{13}CO^+$ emission is in 246 a better agreement with the Spitzer dark and Hershcel 247 bright filamentary structures than that of NH_2D (see 248 also Paper I). These all suggest that the H¹³CO⁺ emis-249 sion is a better tracer of filamentary structures than 250 NH_2D . In what follows, the $H^{13}CO^+$ will be therefore 251 used to identify the velocity-coherent filamentary struc-252

²⁵³ tures. There is the continuum filamentary structure in ²⁵⁴ the south-eastern part of the map (see Figures 1 and ²⁵⁵ 2), which continuum emission is unlikely dominated by ²⁵⁶ dust emission (See discussions below in Section 4.1).

²⁵⁷ We used the $\sim 7''$ resolution NH₃ rotational tempera-²⁵⁸ tures ($T_{\rm NH_3}$) derived in paper I. For the regions where ²⁵⁹ the NH₃ data are not available, we assume a gas kine-²⁶⁰ matic temperature of $\langle T_{\rm NH_3} \rangle = 15$ K, the average gas ²⁶¹ temperature derived from the observed NH₃ data.

3.2. Velocity Structures



Figure 2. Magenta open squares, blue open triangles, red cross "x", and yellow plus "+" symbols show the continuum cores, NH₂D cores, Class I, and Class II, respectively. Left: the filament spines (cyan and green solid curves) overlaid on the 3 mm continuum image. Right: the filament spines (cyan and green solid curves) overlaid on the peak intensity map ($I_{\rm NH_2D}$) of the NH₂D line emission. White box shows the region where outflows are identified, with zoomed-in views presented in Figures 9. The beam size is shown in the bottom left of each panel.

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Paper I found that multiple velocity components 263 were detected in some areas where significant $H^{13}CO^+$ 264 emission was detected. Since the majority ($\sim 85\%$) 265 $H^{13}CO^+$ emission appears as a single velocity of 266 component, we show the intensity-weighted velocity 267 1st-moment) and intensity-weighted dispersion (2nd-268 moment) of the $H^{13}CO^+$ line emission in Figure 3. We 269 note that there are complex velocity structures across 270 NGC 6334S, especially toward the central region which 271 appears to be associated with multiple velocity compo-272 nents. 273

We fit Gaussian line profiles to the H¹³CO⁺ data pixel by pixel with multiple velocity components, under the assumption that the H¹³CO⁺ emission is optically thin. The detailed fitting process of molecular lines is summarized in the Paper I. The observed velocity dispersions $_{279}$ ($\sigma_{\rm obs}$) derived from the Gaussian fitting are between $_{280}$ 0.10 and 0.80 km s⁻¹, with mean and median values $_{\rm 281}$ of 0.23 and 0.20 km s $^{-1},$ respectively. The observed $\sigma_{\rm obs}$ is composed of the thermal and nonthermal com-282 ponents. Paper I shows that the nonthermal velocity 283 dispersion $\sigma_{\rm nth}$ is dominated by subsonic and transonic 284 motions throughout NGC 6334S. The $\sigma_{\rm obs}$ of the dense cores is greater than in the quiescent regions; the $\sigma_{\rm nth}$ 286 and the $\sigma_{\rm obs}$ toward the central region of NGC 6334S, 287 have generally larger values than that measured in the 288 outer regions (see Paper I).

3.3. Filament Identification

3.3.1. Friend-of-Friend Algorithm

The results from the Gaussian fitting as described above in Section 3.2 were used to identify gas fila-



Figure 3. Left and middle panels show the $H^{13}CO^+$ intensity-weighted velocity (1st-moment) and intensity-weighted dispersion (2nd-moment) maps, respectively. The beam size is shown in the bottom left of each panel. Right panel shows the spectra of $H^{13}CO^+$ extracted from positions 1, 2, and 3. Three selected positions are marked with red cross "x" in both left and middle panels.

²⁹⁴ ments. Following similar procedures as Hacar et al. ²⁹⁵ (2013, 2018), we used the python-based friend-of-friend ²⁹⁶ (fof) algorithm¹ (Huchra & Geller 1982) to identify the ²⁹⁷ velocity-coherent filaments, i.e., no abrupt change of ²⁹⁸ sign of the gradient along the filament in PPV space.

We first used the fof algorithm to identify the seed 299 points, those that have peak intensities (I, the maxi-300 mum intensity of the spectrum) above a certain thresh-301 old I_0 (7 σ), of each individual structure. In total, about 302 $\sim 70\%$ of the data points are above I_0 . The spatial cri-303 terion between nearby points to be considered as friends 304 is $\Delta r \leq 0.023$ pc (~1 beam size linear scale), while 305 the velocity criterion uses an adaptive velocity gradient 306 $\nabla v_{\text{LSR},i} = \frac{1}{2} \frac{\Delta v_i}{\theta_{\text{FWHM}}}$ similar to the definition in Hacar et al. (2018). Here, Δv_i is the line full width half maxi-307 308 mum (FWHM) of H¹³CO⁺ of the *i*th pixel and θ_{FWHM} is 309 the beam size. Only structures that contain more than 310 150 data points (the area of a structure larger than 3 311 times the beam size) were considered. Second, we ran 312 fof again to search for new friend points of each group 313 identified in the first step, where the new friend points 314

³¹⁵ come from the remaining data points, in which the low ³¹⁶ intensity points ($\leq I_0$) are encompassed; the same spa-³¹⁷ tial and velocity criteria are used. After the second fof ³¹⁸ run, there are about 20% of points that are not included ³¹⁹ within any group. The majority of them have relatively ³²⁰ low intensities and/or appear to unaffiliated with the ³²¹ identified filaments.

We employed the FilFinder² algorithm to compute 322 323 the filament spine. The FilFinder package reduces the masking area to identify a skeleton that represents the 324 topology of the area, using a Medial Axis Transform. 325 The masking area is delineated by the spatial distribu-326 tion of the identified filaments; we refer to the derived 327 skeletons as the filament spines. The derived filament 328 spines are shown in Figure 1. In total, 13 velocity-329 coherent filaments have been identified by the fof al-330 gorithm from the PPV space of $H^{13}CO^+$ data. Fila-331 ments are named F1, F2, F3 ... in order from south to 332 north. Filaments F4 and F10 have additional branches 333 and they are named as F4b and F10b. The physical 334

² https://github.com/e-koch/FilFinder

¹ https://github.com/ShanghuoLi/pyfof

³³⁵ lengths of these identified filaments $(L_{\rm fil})$ range between ³³⁶ 0.4 and 1.3 pc.

3.3.2. Velocity-Coherent Filaments

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The filament spines overlaid on the channel maps of 338 $H^{13}CO^+$ are shown in Figure 4, which shows that the 339 line emission exhibits a filamentary distribution and that 340 the identified filaments are consistent with the majority 341 of the $H^{13}CO^+$ emission. This provides further evidence 342 that the python-based fof algorithm can accurately re-343 cover the gas filamentary structures that are connected 344 in both velocity and space (see also Figure 5). 345

Several small regions show significant H¹³CO⁺ emis-346 sion but are not grouped into any identified filament. 347 For instance, there is a small $H^{13}CO^+$ emission region 348 on the west of F2 at velocity range of between -4.20349 and 3.78 km s^{-1} , which is marked with red arrows in 350 Figure 4. Two separated substructures appear in this 351 small region, implying the emission is not connected in 352 the spatial space. There are also some isolated small re-353 gions separated from the identified filaments in spatial 354 space. These isolated regions fail to be considered as an 355 independent filament because their emission is too weak 356 and/or the number of total data points are lower than 357 the criteria of identification. We stress that the iden-358 tified filaments are likely to be incomplete. Potential 359 low density and diffuse molecular filamentary structures 360 could have been missed if their $H^{13}CO^+$ line emission is 361 not significant and/or the detection suffers from severe 362 missing flux. 363

The H¹³CO⁺ line emission of identified filaments gen-364 erally spans ≥ 4 channels (a velocity range of ≥ 0.84 km 365 s^{-1}). The filament with the largest spread in velocity is 366 F4, which spans from -6.52 to -2.3 km s⁻¹. The major-367 ity of the filaments are spatially distinct, while several 368 filaments partly overlap in position, such as F2-F4, F4-369 F6, F4–F7, and F7-F8. The overlapping regions tend 370 to show complex velocity structures as characterized by 371 multiple velocity components along the line of sight. 372

3.4. Filament Profile

We employed the $RadFil^3$ package (Zucker & Chen 374 2018), a radial density profile building and fitting tool 375 for interstellar filaments, to construct the filament radial 376 profile from the velocity integrated intensity of H¹³CO⁺ 377 inside the mask of a given filament. We used the RadFil 378 tangent to the filament spine at 7 or 8 pixel (about 1 379 beam size; 1 pixel = 0''.43) intervals along the filament, 380 then took the radial cut perpendicular to each tangent. 381

The radial profile has been shifted along each cut in or-382 der to ensure that it is centered on the pixel with the 383 peak intensity. Figure 6 shows the radial cut and the 384 pixels (blue points) of the peak in the radial cut for F1. 385 Along each cut, the radial distance is calculated as the 386 projected distance from the peak intensity. Prior to fit-387 ting the profile, the background was subtracted using 388 the background subtraction estimator of RadFil. The 389 background is estimated by a first-order polynomial to 390 all profiles at the given radial distance range, and then 391 subtracts it from each cut; the background subtraction 392 radii vary slightly from filament to filament, with a typ-393 ical range of 0.08–0.15 pc. 394

To compute the filament widths (FWHM), we performed a Gaussian fitting to the average profile of the $\rm H^{13}CO^+$ intensity of each filament. The Gaussian function is given by

$$A(r) = A_0 \exp\left(\frac{-(\mathbf{r}-\mu)^2}{2\sigma_{\rm G}^2}\right),\tag{1}$$

where r is the radial distance, A is the profile ampli-396 tude at the radial distance r, A_0 is the amplitude, σ_G is the standard deviation, and μ is the mean. Here, μ is fixed to zero. The best-fit Gaussian of each fila-398 399 ment profile is listed in Table 1. An example of the fit is shown in Figure 6, where the red solid line is 400 the best fit, the black dots correspond to the aver-401 aged integrated intensity of $H^{13}CO^+$ and the error bars 402 are the standard deviation of the radial profile of all cuts perpendicular to the filament. The best-fit filament widths range from 0.036 to 0.074 pc, with the 405 mean and median values of 0.046 and 0.045 pc, re-406 spectively. We also estimated the beam-deconvolved 407 FWHM with FWHM_{decon} = $\sqrt{\text{FWHM}^2 - \text{FWHM}_{\text{bm}}^2}$, where FWHM_{bm} is the half-power beam width. The 408 409 FWHM_{bm} is about 3''.4 (~0.021 pc) in our observa-410 tions. The FWHM_{decon} is between 0.029 and 0.071 pc, 411 with the mean and median values of 0.041 and 0.039 pc, 412 413 respectively.

In previous studies, observed filaments have been considered as cylindrical structures that can be described by a Plummer-like function of the form (e.g., Nutter et al. 2008; Arzoumanian et al. 2011; Palmeirim et al. 2013; Smith et al. 2014; Liu et al. 2018):

$$\int f dv(r) = \frac{A_0}{\left[1 + \left(\frac{r}{R_{\text{flat}}}\right)^2\right]^{\frac{p-1}{2}}},\tag{2}$$

⁴¹⁴ where $\int f dv$ is the integrated intensity, A_0 is the peak ⁴¹⁵ profile amplitude, R_{flat} is the flattening radius, and p is ⁴¹⁶ the power-law index of the density profile at large radii



Figure 4. The filament spines (solid curves) overlaid on the channel map of $H^{13}CO^+$. The velocity value is presented in the top left of each panel.

⁴¹⁷ (Cox et al. 2016; Zucker & Chen 2018). We also per-⁴¹⁸ formed a Plummer fitting to the identified filaments in ⁴¹⁹ NGC 6334S. The best Plummer fit is shown in dashed ⁴²⁰ green line in Figure 6. The filament widths derived by ⁴²¹ the Plummer fitting are similar to those of the Gaus⁴²² sian fitting, and FWHM ranges from 0.03 to 0.066 pc, ⁴²³ with the mean and median values of 0.045 and 0.042 ⁴²⁴ pc, respectively. The FWHM_{decon} is between 0.023 and ⁴²⁵ 0.062 pc, with the mean and median values of 0.039 and ⁴²⁶ 0.037 pc (Table 1), respectively. $R_{\rm flat}$ is between 0.012



Figure 5. Position-position-velocity (PPV) cube shows the centroid velocity of the identified filaments. (The animated version of the PPV cube is available in https://github.com/ShanghuoLi/NGC6334S-filament.)

⁴²⁷ and 0.081 pc, with a mean and median values of 0.033
⁴²⁸ and 0.027 pc, respectively. Figure 6 shows that some
⁴²⁹ of the filament profiles have relatively large dispersions
⁴³⁰ due to non-uniform line intensities throughout the fila⁴³¹ ments. The significant variations of H¹³CO⁺ emission
⁴³² across the filaments results in a poor fit in their profiles,
⁴³³ e.g., F4 and F9.

The derived filament widths are similar to those 434 of Musca (~ 0.07 pc; Kainulainen et al. 2016), 435 Aquila/Polaris (~0.04 pc; Men'shchikov et al. 2010), 436 Orion ($\sim 0.02 - 0.05$ pc for OMC-1/2 and ISF; Hacar 437 et al. 2018), G14.225-0.506 ($\sim 0.05 - 0.09$ pc; Chen 438 et al. 2019b), G035.39-00.33 (~ 0.028 pc; Henshaw et al. 439 2017), and L1287 (~0.03 pc; Sepúlveda et al. 2020). 440 In contrast, the derived filament widths are narrower 441 than those of *Herschel* filaments studied toward IC 5146 442 (~ 0.1 pc; Arzoumanian et al. 2019), Taurus (~ 0.1 pc; 443 Palmeirim et al. 2013), NGC 6334IN and NGC 6334I 444 $(\sim 0.24 \text{ pc}; \text{Russeil et al. 2013})$. But note that the spa-445 tial resolution of *Herschel* observations (beam size \sim 446 36'') is much poorer than that of the ALMA observa-447 tions. This supports the idea that higher spatial reso-448 lution observations and higher-density gas tracers can 449 identify narrower filaments. In addition, the dust con-450 tinuum emission cannot be resolved into separate fila-451 ments when they overlap, whereas velocities measure-452 ments generally can do so. Spatially blended filaments 453 might broaden the measured filament widths (see also 454 Henshaw et al. 2017). This also indicates that filaments 455

⁴⁵⁶ identified with different procedures might show deviat-⁴⁵⁷ ing filament widths.

3.5. Filament Mass

The mass per unit length is one important indicator for assessing the stability of filaments. The continuum emission from dust is one of the most frequently used measurement to compute the mass. Figure 2 shows the filament spines overlaid on the 3 mm continuum image. Unfortunately, only 2 gas filaments (F4 and F1) have significant continuum emission detection (Figure 2); the remaining 11 gas filaments are either only partly detected in continuum emission or not detected at all above 5σ . An alternative way to estimate the filament mass is to make use of molecular gas emission; in this work we use $H^{13}CO^+$. With the fractional abundance of $H^{13}CO^+$ relative to H_2 , $X(H^{13}CO^+) = N(H^{13}CO^+)/N(H_2)$, the filament mass can be computed as follows:

$$M_{\rm fil} = \mu_{\rm H_2} \, m_{\rm H} \sum \frac{N({\rm H}^{13}{\rm CO}^+)}{X({\rm H}^{13}{\rm CO}^+)} \,\Omega, \tag{3}$$

⁴⁵⁹ where $N(\mathrm{H^{13}CO^+})$ is the column density of $\mathrm{H^{13}CO^+}$, ⁴⁶⁰ $\mu_{\mathrm{H}_2} = 2.8$ is the mean molecular weight of the interstel-⁴⁶¹ lar medium (ISM; Kauffmann et al. 2008), m_{H} is the ⁴⁶² hydrogen mass, and Ω is the solid angle of the $\mathrm{H^{13}CO^+}$ ⁴⁶³ emission. Assuming local thermodynamic equilibrium ⁴⁶⁴ (LTE), the molecular column densities can be esti-⁴⁶⁵ mated from the velocity-integrated intensity (see Ap-⁴⁶⁶ pendix A1), and finally leads to M_{fil} (see Eq.3).

In order to estimate $X(\mathrm{H}^{13}\mathrm{CO}^+)$ for NGC 6334S, we have focused on F4 because both $\mathrm{H}^{13}\mathrm{CO}^+$ line



Figure 6. Panel a: the filament spine (red solid curves) of F1 overlaid on the velocity-integrated intensity map of $H^{13}CO^+$. Magenta cross "x" and cyan plus "+" symbols are continuum cores and NH₂D cores, respectively. The velocity range of this filament is presented in the upper middle of the panel. The beam size is shown in the bottom left of the panel. Panel b: mean integrated intensity profile of $H^{13}CO^+$ (black dots) was built by sampling radial cuts (short red solid lines) every 8 pixels (which corresponds to 3".44 or ~0.019 pc at the source distance of 1.3 kpc) along the spine. The radial distance is the projected distance from the peak emission at a given cut (blue dots in panel a). The error bar represents the standard deviation of the cuts at each radial distance. The orange solid line shows the beam response with a FWHM of ~3".4. The red solid and green dashed lines present the best-fit results of Gaussian and Plummer fitting, respectively. Panel c and d: the mean centroid velocity $\langle v_{\text{LSR}} \rangle$ and mean observed velocity dispersion $\langle \sigma_{\text{obs}} \rangle$ of $H^{13}CO^+$ line variation along the filament. The error bars show the standard deviation of corresponding v_{LSR} and σ_{obs} . Vertical magenta and cyan lines indicate the positions of associated continuum cores and NH₂D cores, respectively. The red cross "x" and green filled star symbols mark the core mean σ_{obs} derived from the $H^{13}CO^+$ and NH₂D lines, respectively. The complete figure set (4 images, see Figure 13) is available in the online journal.

and continuum emission are significantly detected (Fig-469 ures 1 and 2). The derived $N(H^{13}CO^+)$ ranges from 470 7.2×10^{11} cm⁻² to 1.4×10^{13} cm⁻² and $N_{\rm H_2}$ is between 1.3×10^{22} cm⁻² and 6.1×10^{23} cm⁻². The re-471 472 sulting values of $X(H^{13}CO^+)$ extend from 7.7×10^{-12} 473 to 3.1×10^{-10} , with a median value of 5.4×10^{-11} . The 474 derived $X(H^{13}CO^+)$ is similar to the reported values 475 of $3.0 \times 10^{-11} - 4.0 \times 10^{-10}$ in Butner et al. (1995), 476 4.5×10^{-11} in Gerner et al. (2014), 4.8×10^{-10} in San-477 hueza et al. (2012), and 1.3×10^{-10} in Hoq et al. (2013). 478 Using the median $X(H^{13}CO^{+}) = 5.4 \times 10^{-11}$, we es-479 timated the gas mass $(M_{\rm fil})$ for each filament. The de-480 rived masses are in the range of 4 – 82 M_{\odot} (see Ta-481 ble 1) and the total gas mass in the filaments is about 482

⁴⁸³ 342 M_{\odot} . The total gas mass estimated from $H^{13}CO^+$ ⁴⁸⁴ in the observed region is about 395 M_{\odot} , which indicates ⁴⁸⁵ that these filaments contain most of the dense gas (87% ⁴⁸⁶ = 342/395), as revealed by the total $H^{13}CO^+$ line emis-⁴⁸⁷ sion (see Section 4.5 below). The masses per unit length ⁴⁸⁸ ($M_{\rm line} = M_{\rm fil}/L_{\rm fil}$) of filaments range between 14 and 64 ⁴⁸⁹ M_{\odot} pc⁻¹, with a median value of 29 M_{\odot} pc⁻¹ (see Ta-⁴⁹⁰ ble 1).

⁴⁹¹ The uncertainties in the distance, assumed gas tem-⁴⁹² perature, and variations of the $\rm H^{13}CO^+$ fractional abun-⁴⁹³ dance introduce uncertainties in the estimates of the fil-⁴⁹⁴ ament masses and masses per unit length. The typi-⁴⁹⁵ cal uncertainties in the temperatures derived from NH₃ ⁴⁹⁶ is ~15% (see Paper I). The uncertainty in distance



Figure 7. Left and right: violin plots of the Mach number distributions derived from $H^{13}CO^+$ and NH_2D for each filament. The blue bars from the top to bottom represent the maximum, mean, and minimum values, respectively. The red and blue solid lines are the Mach number of 1 and 2, respectively.

548

from the trigonometric parallax measurement is $\sim 20\%$ 497 Chibueze et al. 2014). The standard deviation (std) of 498 $X(\mathrm{H}^{13}\mathrm{CO}^+)$ for F4 is about 3.7×10^{-11} , which corresponds to 1σ uncertainty of $70\% = \frac{3.7 \times 10^{-11}}{5.4 \times 10^{-11}}$. We settle 499 500 on an uncertainty estimate of a factor of ~ 2 for both fil-501 ament mass and mass per unit length according to the 502 propagation of error. Considering of the inclination an-503 gle is unknown, the uncertainties in the mass per unit 504 length could be larger. 505

3.6. Subsonic and Transonic Filaments

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The three-dimensional (3D) Mach number is \mathcal{M} = 507 $\sqrt{3}\sigma_{\rm nth}/c_{\rm s}$, where $\sigma_{\rm nth} = \sqrt{\sigma_{\rm obs}^2 - (\triangle_{\rm ch}/2\sqrt{2\ln 2})^2 - \sigma_{\rm th}^2}$ is the nonthermal velocity dispersion, $c_{\rm s}$ is the sound 508 509 speed, and \triangle_{ch} is the channel width. The molecular 510 thermal velocity dispersion can be estimated by $\sigma_{\rm th} =$ 511 $\sqrt{(k_{\rm B}T)/(\mu m_{\rm H})} = 0.098 \,{\rm km \, s^{-1} \, (\frac{T}{K})^{0.5} \mu^{-0.5}}$, where $\mu =$ 512 $m/m_{\rm H}$ is the molecular weight, m is the molecular mass, 513 $m_{\rm H}$ is the hydrogen mass, and T is the gas temperature 514 (see also Paper I). The sound speed $c_{\rm s}$ was estimated us-515 ing a mean molecular weight per free particle of $\mu_{\rm p}=2.37$ 516 Kauffmann et al. 2008). Figure 7 shows the Mach num-517 ber (\mathcal{M}) distributions derived from $\mathrm{H}^{13}\mathrm{CO}^+$ and $\mathrm{NH}_2\mathrm{D}$ 518 for each filament, except for F11 which has no significant 519 NH₂D detection. Some filaments are partially overlap-520 ping but the corresponding NH₂D line emission shows 521 only one velocity component clearly. This NH₂D emis-522 sion is assigned to a particular filament based on the 523 minimum velocity differences between NH₂D emission 524 and that filament. The Mach number distributions de-525 rived from both $H^{13}CO^+$ and NH_2D lines reveal that 526 the majority of filaments are subsonic ($\mathcal{M} \leq 1$) and 527 transonic $(1 < \mathcal{M} \leq 2)$ in nonthermal motions. In gen-528 eral, the \mathcal{M} derived from NH₂D tends to be smaller 529

than those from $H^{13}CO^+$. This is because NH_2D emission traces colder, denser gas and it is less affected by 531 the protostellar feedback (e.g., outflows) as compared to 532 the $H^{13}CO^+$ emission; this is confirmed by the fact that 533 the observed line widths of the former narrower than 534 those of the latter. The subsonic and transonic features 535 imply a quiescent nature of these filaments. The sub-536 sonic and transonic nonthermal line widths found here 537 in dense filaments and dense cores have been seen pre-538 viously in low-mass star-forming regions (e.g., Perseus, Pineda et al. 2010; Serpens, Gong et al. 2021; Ophiuchus 540 and Taurus, Chen et al. 2019a; L1478 in the California, 541 Chung et al. 2019), intermediate- and high-mass star-542 forming regions (e.g., Orion, Hacar et al. 2018; Mon-543 sch et al. 2018; Yue et al. 2021; IRDC G035.39-00.33, 544 Sokolov et al. 2018; IRDC G14.225–0.506, Chen et al. 545 2019b). 546

4. DISCUSSION

4.1. Continuum Filament

The majority of the continuum emission structures 549 550 have a significant line emission counterparts. One exception is the continuum filamentary structure in the 551 south-eastern part of the map (see Figures 1 and 2), 552 which has no line emission counterpart except for a small 553 554 area near the middle that shows weak emission in the $H^{13}CO^+$, CS, HCN and HCO⁺ lines. If this filamentary 555 structure's continuum emission was dominated by free-556 free or synchrotron emission rather than dust emission, 557 the stellar feedback from O type stars (O7.5 and O6.5, see Figure 1; Persi & Tapia 2008) on the north-eastern 559 side of NGC 6334S are most likely responsible. 560

⁵⁶¹ We used the FilFinder to extract this filamentary ⁵⁶² structure and its filament spine (see Figure 8). The fil-



Figure 8. Left: the filament spine (red solid curve) of continuum filament overlaid on the 3 mm continuum image. Right: mean integrated intensity profile (black dots) was built by sampling radial cuts (short red solid lines) every 8 pixels (3".44 corresponds to ~0.019 pc at the source distance of 1.3 kpc) along the spine. The radial distance is the projected distance from the peak emission at a given cut (blue dots in the left panel). The error bar represents the standard deviation of the cuts at each radial distance. The orange solid line shows the beam response with a FWHM of ~2.9". The red solid and green dashed lines present the best-fit results of Gaussian and Plummer fitting, respectively.

ament length is about 0.8 pc. Using Radfil, the filament widths are about 0.032 pc and 0.023 pc derived by
Gaussian and Plummer fitting based on the continuum
emission (Table 1), respectively. The gas mass cannot
be reliably estimated because of the unknown fraction
of dust emission.

569 4.2. T

4.2. The Kinematics of Filaments

Figure 6 shows the variations of $v_{\rm LSR}$ and $\sigma_{\rm obs}$ derived 570 from the $H^{13}CO^+$ line emission along the filament. Only 571 one filament (F1) shows monotonic changes along the fil-572 ament in $v_{\rm LSR}$. In contrast, the $\sigma_{\rm obs}$ shows small fluctu-573 ations along F1 rather than monotonic change. Four 574 continuum cores and two NH₂D cores are associated 575 with this filament. The core mean $\sigma_{\rm obs}$ derived from the 576 $\rm H^{13}CO^+$ line is comparable to the $\sigma_{\rm obs}$ of filament, how-577 ever continuum cores #25 and #21 have slightly larger 578 $\sigma_{\rm obs}$. Line widths may be broadened by active star for-579 mation. In contrast, some cores show much narrower 580 $\sigma_{\rm obs}$ than their respective filament; e.g., #31/#36/#49581 in F2, #4/#24 in F4, M11 in F5, M10 in F6, M14 in 582 F10. The measured $\sigma_{\rm obs}$ of NH₂D is always narrower 583 than those of $H^{13}CO^+$ toward the continuum cores and 584 NH₂D cores, and this feature is also seen in the fila-585 ments (see Figure 7). In Section 4.4, we will discuss the 586 properties of $\sigma_{\rm obs}$ in both continuum cores and NH₂D 587 cores. 588

Some filaments show only small v_{LSR} variations along their spine (F4b, F5, F7, F8, F10, F10b, F12), while



Figure 9. Magenta open squares show the continuum cores. The blue-shifted (blue contours) and red-shifted (red contours) of HCN (1-0) line emission overlaid on the continuum image. The arrows show the outflow directions. The beam size is shown in the bottom left of each panel.

others display significant variations (F2, F3, F4, F6, 591 F9, F11, F13). The $\sigma_{\rm obs}$ also shows irregular varia-592 tions in all of filaments, except for F1 and F13. The 593 latter shows roughly an increasing trend from east to 594 west (Figure 13). There is another gaseous structure 595 seen in the CS (1-0), HCO⁺ (1-0), and HCN (1-0) lines, 596 which runs northwest to southeast through the western 597 part of F13. The interaction between two gas flows can 598 599 broaden the H¹³CO⁺ line widths around the intersection regions. On the other hand, the star formation activity 600 is responsible for some of the $v_{\rm LSR}$ and $\sigma_{\rm obs}$ variations 601 in some filaments. For instance, F4 shows $v_{\rm LSR}$ and $\sigma_{\rm obs}$ 602 variations at positions in which several strong molecular 603 outflows are detected in the HCN, HCO⁺, and CS lines 604 (see Figure 9). These molecular outflows can inject en-605 ergy and momentum into the immediate surroundings 606 of protostars and affect the gas kinematics, and then 607 the turbulence (or line width) will be increased and the 608 gas velocity will be modified (Li et al. 2019b, 2020b; Lu 609 et al. 2021). Filament F4 encompasses the highest num-610 611 ber of continuum cores and YSOs among the filaments (Figures 1 and 13), and therefore the $v_{\rm LSR}$ and $\sigma_{\rm obs}$ of 612 the $H^{13}CO^+$ line emission in F4 is most likely signifi-613 614 cantly affected by protostellar feedback. Overall, both protostellar activity and interaction between gas flows 615 can significantly alter the local gas kinematics. 616

4.3. Velocity Gradient Along F1

617

As shown in Figure 6, F1 presents a smooth velocing ity change in $H^{13}CO^+$ emission from the south (-3.3 km

 $_{620}$ s⁻¹) to the north (-1.8 km s⁻¹) along the filament, resulting in a projected velocity gradient of $\sim 1.8 \pm 0.1$ km 621 $^{-1}$ pc⁻¹. The NH₂D line emission also shows a similar 622 \mathbf{S} velocity gradient along F1. The velocity gradient along 623 F1 could be attributed to the ongoing accretion flow in 624 F1 (e.g., Kirk et al. 2013), whereas we cannot completely 625 rule out the possibility that the gas kinematics is affected 626 by the external feedback from the western YSOs, such 627 as molecular outflows and/or expanding shells. 628

If the velocity gradient comes from the accretion flow along the F1 filament, one can estimate the mass flow rate using the derived velocity gradient and filament mass. Assuming that the filament has a cylindrical geometry, the mass flow rate, \dot{M} , can be calculated as (see Kirk et al. 2013)

$$\dot{M} = \frac{M \,\nabla_{||} v_{\text{obs}}}{\tan(\alpha)} \tag{4}$$

where M is the filament mass, $\nabla_{||} v_{obs}$ is the observed 629 velocity gradient along the filament, and α is the angle 630 of inclination to the plane of sky. Using the derived 631 filament mass of 14 M_{\odot} , the observed velocity gradient 632 of $1.8 \text{ km s}^{-1} \text{ pc}^{-1}$, and assuming a moderate inclination 633 angle of $\alpha = 45^{\circ}$, the mass flow rate is estimated to be 634 about 26 M_{\odot} Myr⁻¹ for F1. This result indicates that 635 the F1 filament will double its mass in several free-fall 636 time; $\sim 1 \times 10^5$ yrs assuming a density of 10^{5-6} cm⁻³ 637 that is the typical value of continuum cores in the F1 638 (see Paper I). 639

Considering the uncertainties of the derived mass and 640 inclination angle, the estimated flow accretion is roughly 641 comparable to the values of $70\pm40 \text{ M}_{\odot} \text{ Myr}^{-1}$ in the 642 IRDC G035.39-00.33 (Henshaw et al. 2014), and 17 - 72 643 M_{\odot} Myr⁻¹ in the Monoceros R2 (Treviño-Morales et al. 644 2019), and 20 – 130 M_{\odot} Myr⁻¹ in the IRDC G14.225– 645 0.506 (Chen et al. 2019b). The estimated mass flow rate 646 could be treated as a lower limit, because the $H^{13}CO^+$ 647 only traces relatively high dense gas and F1 filament is 648 only a small part of a much large filamentary structure 649 seen in the infrared image (see Figure 1). 650

A velocity gradient is also detected in sections of the 651 other filaments (e.g., F7 and F13) and around some em-652 bedded cores (e.g., #29 in the F3; see Figure 13). Unfor-653 tunately, in these cases we cannot distinguish whether 654 the velocity gradient is the result of gas flow or some 655 other physical process, e.g., molecular outflow or rota-656 tion. Thus, we refrain from estimating the mass flow 657 rate for other filaments. 658

4.4. The Kinematics of Embedded Cores

As mentioned in Section 4.3, some cores show smaller $\sigma_{\rm obs}$ compared to their immediate surrounding. This is

probably because the surrounding gas is affected by the 662 protostellar activity (e.g., molecular outflows) for some 663 cores. For instance, there is a molecular outflow ema-664 nating from #2 in the immediate vicinity of cores #4665 and #24, thus the H¹³CO⁺ line widths around both #4666 and #24 can be broadened by this outflow activity (see 667 Figure 2). The outflow driven by core #8 also affects 668 the molecular gas around the core #4. The details of 669 molecular outflow analysis is beyond the scope of this 670 paper but is the topic of a followup paper. 671

Furthermore, some of the cores indeed have narrow 672 line widths as revealed by the NH₂D line, which is less 673 affected by the molecular outflows than $H^{13}CO^+$ as mentioned above. In addition, there are no outflow signatures around these cores. For instance, the observed 676 velocity dispersion appears to decrease toward the cen-677 ter of M1 (See Figure 10). A trend of σ_{obs} decreasing 678 with decreasing radial distance (R_{dist}) from the center 679 of core is found in 16 cores (see Figure 10), including 6 680 continuum cores (#5, #10, #22, #25, #35, and #37)681 and 10 NH₂D cores (M1, M4, M6, M7, M8, M9, M13, 682 M10, M15, and M17; see also Figure 3 in Paper II for 683 M1). Note that the annularly averaged $\sigma_{\rm obs}$ has rela-684 tively large uncertainties toward the outer edges of the 685 cores due to the low S/N. The decreasing trend of $\sigma_{\rm obs}$ 686 toward these core centres may indicate that turbulent 687 dissipation from the filaments to the embedded objects 688 is ongoing, enabling the dense precursors to collapse to 689 form protostars. Alternatively, a number of theo-690 retical studies suggest that for pre-stellar cores the line 691 width will be smaller in the more central regions if the 692 infall speed decreases toward the center because of an 693 outside-in collapse (e.g., Whitworth & Summers 1985; 694 Lai 2000; Gómez et al. 2021). In summary, some dense 695 cores indeed have narrower observed velocity dispersion 696 compared to their natal filaments. This may indicate 697 698 that turbulent dissipation is taking place in these embedded cores. 699

4.5. Filament Stability

The comparison between the M_{line} and the corre-701 sponding critical line-mass $M_{\rm crit} = 2\sigma_{\rm eff}^2/G$ can be used 702 to evaluate the stability of the filament; where σ_{eff} is the 703 effective velocity dispersion and G is the gravitational 704 constant (see Appendix B for the estimation of criti-705 cal line-mass.). Ignoring external pressure and magnetic 706 fields, we computed the $M_{\rm crit}$ for thermally supported 707 $(\sigma_{\text{eff}} = c_{\text{s}})$, nonthermal motions supported $(\sigma_{\text{eff}} = \sigma_{\text{nth}})$, 708 and total motions supported (i.e. including both ther-709 ⁷¹⁰ mal and nonthermal contributions, $\sigma_{\rm eff} = \sqrt{c_{\rm s}^2 + \sigma_{\rm nth}^2}$ 711 filaments. As shown in Figure 11, M_{line} is larger than ⁷¹² the thermal critical mass $(M_{\rm crit,th})$, except for F4b, F6



Figure 10. The annularly averaged observed NH_2D velocity dispersions (σ_{obs}) as a function of radial distance from the center of cores. The error bars show the statistical standard deviation inside each ring divided by the square root of the length of the ring. M1 is modified from Paper II. The name of each core is shown in the top left of each panel.

and F13 that are smaller than the $M_{\rm crit,th}$. This indi-713 cates that the filaments would be gravitationally bound 714 (except for F4b, F6 and F13) in the purely thermally 715 supported case. M_{line} is about 2 times the nonther-716 mal critical mass $(M_{\rm crit,nth})$, which suggests that non-717 thermal support alone cannot prevent gravitational col-718 lapse. The ratios of $M_{\rm crit,nth}/M_{\rm crit,th}$ are in the range 719 0.4-1.4 with a mean value of 0.7, which suggests that 720 the filaments are mostly supported by thermal motions. 721 The estimated M_{line} is smaller than the total critical 722 $(M_{\rm crit,tot})$ mass in all the filaments, except for F4. 723

Although most of the filaments at the current evo-724 lutionary state are gravitationally unbound when con-725 sidering only the balance between self-gravity and the 726 thermal plus nonthermal support, the presence of dense 727 cores suggests that in fact star formation has already 728 started. Note that by neglecting external pressure, 729 magnetic field, mass uncertainty, and inclination an-730 gle uncertainty might bring an addition error into the 731 $M_{\rm line}/M_{\rm crit,tot}$. Being gravitationally bound is not the 732

sole prerequisite for forming stars in a filament. The 733 fragmentation may have occurred already very early in 734 the evolution of the filaments, if these dense cores origi-735 736 nate from filament fragmentation. In addition, the subsonic and transonic dominated filaments and embed-737 ded cores indicate that there are low turbulence envi-738 ronments (Paper II); this is analogous to the situation 739 in low-mass star-forming clouds (e.g., Hartmann 2002; 740 Pineda et al. 2010; Hacar & Tafalla 2011; Hacar et al. 741 742 2016, 2017). The similarity suggests that similar turbulent conditions may apply in the very early evolutionary 743 phases of low- and high-mass star formation at clump 744 scales (\leq of a few pc) where turbulence inherited from 745 larger scales (e.g., giant molecular clouds) has already 746 decayed or dissipated in a short timeframe (Mac Low 747 1999; Mac Low & Klessen 2004). 748

Figure 11 shows M_{line} as a function of $\sigma_{\text{nth}}/c_{\text{s}}$. The derived masses per unit length are similar to those of narrow filaments in B213-L1495 (24±19 M_{\odot} pc⁻¹), Musca rs₂ (26 M_{\odot} pc⁻¹), NGC 1333 (34±22 M_{\odot} pc⁻¹), and Orion



Figure 11. Left: the line-mass for each filament. The black filled circles, red filled stars, blue filled squares, and orange filled crosses show the estimated mass per unit length, thermal critical line-mass, nonthermal critical line-mass, and total (thermal + nonthermal) critical line-mass, respectively. The shaded gray region shows the thermal critical line-mass of $16.6 - 25 \text{ M}_{\odot} \text{ pc}^{-1}$ corresponding to the gas temperature of 10 - 15 K. The arrows indicate that the estimated mass per unit length could be treated as a lower limit. Right: mass per unit length vs. σ_{nth}/c_s . The error bars indicate the standard deviation of the parameters. The dashed lines show the expected total critical line-mass for an infinite filament in hydrostatic equilibrium at temperatures of 5 K, 10 K, 15 K, and 20 K, respectively (see Appendix B). The data points of B213-L1495, NGC1333, ISF, OMC1, OMC2, and Musca are retrieved from Hacar et al. (2018).

 $(23{\pm}11~M_{\odot}~pc^{-1}$ for ISF, $20{\pm}18~M_{\odot}~pc^{-1}$ for OMC-753 and 26 \pm 21 M $_{\odot}$ pc⁻¹ for OMC-2; Hacar et al. 2013, 1. 754 2016, 2017, 2018). The measured $\sigma_{\rm nth}/c_{\rm s}$ are also com-755 parable to those narrow filaments in the B213-L1495, 756 Musca, NGC 1333, and Orion (OMC-1/2 and ISF; see 757 Figure 11). These results indicate that the masses per 758 unit length and gas kinematics of narrow filaments in 759 NGC 6334S are comparable to those found in various 760 other environments, from low-mass to high-mass star-761 forming molecular clouds. 762

The total gas mass computed from $\mathrm{H^{13}CO^{+}}$ is about 763 $395 \,\mathrm{M}_{\odot}$, which is larger than the total gas mass of 160 764 M_{\odot} estimated from continuum emission. The $H^{13}CO^+$ 765 recovers about 28% of the accumulated mass (1389 M_{\odot}) 766 derived from H_2 column density map (derived in Pa-767 per I; see Appendix A in Paper I for detailed deriva-768 tion of H₂ column density.) This indicates that the 769 extended flux, which contains a significant amount of 770 mass, is not fully recovered by the $H^{13}CO^+$ line toward 771 NGC 6334S in this ALMA observation. The estimated 772 filament masses should thus be treated as lower limits 773 because H^{13}CO^+ (1-0; $n_{\rm cr} \sim 10^5 {\rm ~cm^{-3}})$ only probes 774 higher density gas components; moreover, the data suf-775 fer from missing flux due to the lack of short spacing 776 observations. 777

4.6. Population of Embedded Cores and YSOs

The continuum cores are likely at protostellar or prestellar evolutionary phases, while the NH₂D cores seem at the starless/pre-stellar phases (see Paper II). Fig-

ure 1(b) shows the distribution of identified dense ob-782 783 jects and filaments toward NGC 6334S. The majority of the 45 continuum cores are associated with filaments, 784 while only 4 continuum cores (#22, #28, #33 and #48)785 are not associated with any identified filament. In addi-786 tion, 15 out of 17 NH₂D cores are associated with fila-787 ments. These results indicate that the majority of dense 788 cores are closely related with filaments in NGC 6334S; 789 as noted earlier, this situation is also found in nearby 790 low-mass star-forming regions (e.g., André et al. 2010). 791 Figure 1(b) also shows the YSOs spatial distributions 792 toward NGC 6334S. There are 25 Class I and 58 Class II 793 YSOs in the NGC 6334S. The Class I and II YSOs are 794 identified with the near-IR (NEWFIRM) and mid-IR 795 (IRAC) data (see Willis et al. 2013). Among the 49 796 identified continuum cores, 12 cores are spatially associ-797 ated with Class I objects, 5 cores are spatially associated 798 799 Class II objects, and the remaining 32 cores do not have YSOs counterparts. This indicates that these 32 cores 800 could be younger compared to those cores associated 801 with Class I and Class II YSOs. The majority of YSOs 802 have no continuum core counterparts, perhaps because 803 their continuum emission is too faint ($1\sigma \sim 0.03 \text{ mJy}$) 804 $beam^{-1}$, or ~0.04 M_{\odot} at a temperature of 10 K). Fur-805 thermore, the YSOs are not associated with NH₂D cores 806 counterparts, because the NH₂D line emission is in cold 807 dense gas still in its extremely early evolutionary stages (e.g., starless and/or pre-stellar). 809



Figure 12. Left: violin plot of the distance distributions for each type object, where the distances are the objects to the nearest filament spine. The shape of each distribution shows the probability density of the data smoothed by a kernel density estimator. The blue bars from the top to bottom represent the maximum, mean, and minimum values, respectively. The vertical red dashed line is the mean beam-convolved filament width of ~ 0.04 pc. Right: the number of the nearest dense cores, Class I and Class II objects for each filament.

The majority of continuum cores, NH₂D cores, and 810 Class I objects reside in or close to a filament, while the 811 majority of Class II objects are far away (see Figures 1 812 and 2). We computed the distance of these objects to 813 their nearest filament spine, in order to search for possi-814 ble correlations between the evolutionary stages and the 815 distance from the filament. Based on the distance dis-816 tribution of each type of object shown in Figure 12(a), 817 Class II objects have larger distances than Class I, while 818 Class I objects have larger distance than the distribu-819 tion of continuum cores and NH₂D cores. Continuum 820 cores and NH₂D cores are classified as the same type 821 of object in this analysis because the majority of them 822 are embedded in filaments and their evolutionary stages 823 (pre-stellar or protostellar) are earlier than Class I/II 824 (Paper II). The median distances are 0.09 pc, 0.06 pc, 825 and 0.03 pc for Class II, Class I, and dense cores, re-826 spectively. Overall, Figure 12(a) indicates that the more 827 evolved objects are further away from the dense gas fil-828 aments in NGC 6334S. 829

One possible explanation for the different distance dis-830 tributions is that the evolved objects are moving away 831 from their parental dense filament due to the kinemat-832 ical motions (e.g., slingshot mechanism and ejection; 833 Stutz & Gould 2016; Russeil et al. 2020). Assuming 834 the Class II are moving 1 km s^{-1} relative to the fila-835 ments (the typical moving velocity of Class II in Orion; 836 Stutz & Gould 2016), the estimated moving timescales 837 are between 3×10^3 and 4×10^5 yr, with a median value 838 of 9×10^4 yr. We would like to stress the fact that the 839 actual moving distances may be much smaller than the 840 estimated distances because the YSOs might not neces-841 sarily form in the centre of the filament. Therefore, the 842 actual dynamical timescales could be smaller than the 843

estimated values. Another possibility is that NGC 6334S
has experienced star formation before, and the parental
molecular structures of Class II have already been moved
away from the YSOs (e.g., Vázquez-Semadeni et al.
2017; Kumar et al. 2020) or dispersed/destroyed by star
formation feedback. Finally, we cannot rule out the possibility that a few Class II objects may have originated
outside of NGC 6334S; especially those objects that are
distant from the filaments.

The number of nearest dense cores, Class I, and 853 Class II for each filament is presented in Figure 12(b). 854 The number of dense cores and Class I around F4 is 855 much higher than for the rest of filaments, while the 856 857 number of Class II around F1, F2, and F4 is comparable and higher than in the other filaments. F4 is lo-858 cated at the central region where encompasses a signif-859 icant fraction of dense gas and thus it has potential to 860 form more stars as evidenced by the numerous contin-861 uum cores and YSOs. F2 has the longest physical length 862 in NGC 6334S, and thus, it is expected to be associated 863 with more YSOs. As shown in Figure 1, a cluster of 864 YSOs is forming on the western side of F1, resulting in 865 a large number of nearest YSOs. We note that F1 is 866 only a small part of a much larger filamentary structure 867 seen in the infrared image (see Figure 1), implying that 868 it has a large dense gas reservoir from which to form 869 more stars. 870

In summary, all identified filaments show a narrow width and the majority of them host embedded dense core. These embedded dense cores are born in environments of low turbulence, which is similar to conditions found in low-mass star-forming regions. More evolved objects are found to be farther away from the filaments, ⁸⁷⁷ suggesting YSOs or filaments have a tendency to move ⁸⁷⁸ away from their natal place as they evolve.

5. CONCLUSION

In this paper, we investigated the velocity-coherent filaments in the massive IRDC NGC 6334S using ALMA observations. Using the H¹³CO⁺ (1-0) line emission, we have identified 13 velocity-coherent filaments. We investigated the physical properties of the identified filaments and characterized the dense objects in the NGC 6334S. Our main findings are summarized as follows:

- 1. The filaments show a compact radial distribution 887 with a median $FWHM_{decon}$ of ~ 0.04 pc. The 888 derived filament widths are narrower than the 889 previously proposed 'quasi-universal' 0.1 pc fila-890 ment width. In addition, the filament widths are 891 roughly twice the size of embedded cores (radius 892 ~ 0.017 pc). The higher spatial resolution observa-893 tions and higher-density gas tracer tend to identify 894 even narrower and lower mass filaments. 895
- 2. The nonthermal motions are predominantly sub-896 sonic and transonic in all observed filaments; the 897 single exception is F4 which has been significantly 898 affected by protostellar feedback. The filaments 899 are largely supported by thermal motions. The 900 physical properties (mass, mass per unit length, 901 gas kinematics, and width) of filaments are simi-902 lar to those seen in narrow filaments found in vari-903 ous other kinds of environments such as low-mass. 904 intermediate-mass, and high-mass star-forming re-905 gions (i.e., B213-L1495, Musca, NGC 1333, Orion, 906 and G035.39-00.33). 907
- 3. A fraction of the embedded objects show nar-908 rower observed velocity dispersions (σ_{obs}) than 909 their natal filaments, which may indicate that tur-910 bulent dissipation is taking place in these em-911 bedded cores. The subsonic and transonic dom-912 inated filaments and dense cores indicate that in 913 NGC 6334S the stars are often born in environ-914 ments of low turbulent motions. This conclusion 915 hints that similar small turbulent conditions ex-916 ist at very early evolutionary stages of low- and 917 high-mass star formation at clump scales. 918
- 4. The median distance to the nearest filament for 919 dense cores, Class I, and Class II, is 0.03 pc, 920 0.06 pc, and 0.09 pc respectively. The increas-921 ing distances suggest that the more evolved ob-922 jects are farther away from the filaments in the 923 NGC 6334S, perhaps because either YSOs or fila-924 ments tend to move away from their natal place 925 as they evolve. 926

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⁹²⁷ Facilities: ALMA, Herschel.

Software: CASA (McMullin et al. 2007), APLpy
(Robitaille & Bressert 2012), Matplotlib (Hunter 2007),
Astropy (Astropy Collaboration et al. 2013), PySpecKit
(Ginsburg & Mirocha 2011), Numpy (Harris et al. 2020).

	WHM _{decon}	(bc)	(16)	0.042	0.062	0.051	0.039	0.053	0.047	0.029 [†]	0.032H	$0.027_{ m b}$	0.060 ⁻ T	0.033	0.036	0.033	0.038	0.028	0.023	0.039	0.037	0.023	0.062
	FWHM F	(bc)	(15)	0.047	0.066	0.056	0.045	0.057	0.051	0.036	0.038	0.034	0.064	0.039	0.041	0.039	0.043	0.035	0.030	0.045	0.042	0.030	0.066
	d		(14)	9.78 ± 2.37	10.05 ± 5.74	6.27 ± 1.99	2.81 ± 0.34	1.84 ± 0.17	2.78 ± 0.30	$3.94{\pm}1.08$	$2.40{\pm}0.55$	7.16 ± 2.05	2.17 ± 0.24	2.29 ± 0.19	9.85 ± 5.34	9.11 ± 4.18	5.33 ± 2.16	$5.67{\pm}1.56$	2.47 ± 0.23	5.24 ± 1.78	$4.64{\pm}1.32$	1.84 ± 0.17	10.05 ± 5.74
Plummer	$R_{ m flat}$	(bc)	(13)	0.057 ± 0.009	0.081 ± 0.030	$0.051 {\pm} 0.012$	0.021 ± 0.004	0.014 ± 0.003	0.024 ± 0.004	0.023 ± 0.006	0.015 ± 0.006	0.034 ± 0.007	$0.021 {\pm} 0.005$	0.014 ± 0.002	$0.050 {\pm} 0.018$	0.045 ± 0.014	0.035 ± 0.012	0.030 ± 0.007	0.012 ± 0.002	0.033 ± 0.009	0.027 ± 0.006	0.012 ± 0.002	0.081 ± 0.030
	A_{0}	0^{-2} Jy/beam km/s)	(12)	8.53 ± 0.12	$5.16 {\pm} 0.14$	7.25 ± 0.20	$8.84 {\pm} 0.26$	10.05 ± 0.29	6.73 ± 0.22	5.16 ± 0.15	$3.77 {\pm} 0.22$	$7.62 {\pm} 0.19$	4.29 ± 0.15	9.09 ± 0.25	11.21 ± 0.25	11.35 ± 0.25	$7.48 {\pm} 0.35$	$5.84{\pm}0.18$	0.032 ± 0.001	7.03 ± 0.20	7.37 ± 0.21	0.03 ± 0.001	11.35 ± 0.35
	VHM _{decon}	(pc) (1	(11)	0.042	0.057	0.049	0.044	0.040	0.052	0.029	0.030	0.029	0.071	0.040	0.036	0.034	0.039	0.030	0.032	0.041	0.039	0.029	0.071
	FWHM FV	(pc)	(10)	0.047	0.061	0.054	0.049	0.045	0.056	0.036	0.037	0.036	0.074	0.045	0.042	0.040	0.044	0.037	0.037	0.046	0.045	0.036	0.074
Jaussian	stddev]	(bc)	(6)	0.020	0.026	0.023	0.021	0.019	0.024	0.015	0.016	0.015	0.031	0.019	0.018	0.017	0.019	0.016	0.016	0.020	0.019	0.015	0.031
0	A_{0}	$0^{-2} \mathrm{Jy/beam km/s})$	(8)	$8.45 {\pm} 0.12$	5.20 ± 0.06	7.30 ± 0.11	8.39 ± 0.23	$9.90 {\pm} 0.21$	6.37 ± 0.16	5.06 ± 0.11	$3.65 {\pm} 0.18$	7.46 ± 0.22	3.92 ± 0.13	$8.34 {\pm} 0.23$	11.09 ± 0.23	11.22 ± 0.23	7.34 ± 0.46	$5.68 {\pm} 0.18$	0.029 ± 0.001	$6.84 {\pm} 0.18$	7.32 ± 0.18	0.03 ± 0.001	11.22 ± 0.46
	$M_{ m crit,th}$	$[M_{\odot} \mathrm{pc}^{-1})$ (1	(2)	24	24	24	25	24	24	24	24	24	24	24	24	24	24	24		24	24	24	25
	$M_{ m crit,nth}$	$(M_\odot~{ m pc}^{-1})$ ((9)	15	20	14	36	15	16	14	15	18	17	19	20	17	18	11		18	17	11	36
	$M_{ m crit,tot}$	$(M_\odot {\rm \ pc}^{-1})$	(5)	41	47	41	65	41	41	43	40	42	43	44	47	45	47	43		45	43	40	65
	$M_{ m line}$	$M_{\odot}~{ m pc}^{-1})$	(4)	29	38	33	64	14	34	19	24	28	28	26	34	37	42	21		32	29	14	64
	$M_{ m fil}$	(M_{\odot}) ($_{i}$	(3)	14	52	17	82	4	18	16	15	11	23	13	12	15	18	17		22	16	4	82
	$L_{\rm fil}$	(pc)	(2)	0.48	1.37	0.50	1.27	0.27	0.53	0.86	0.62	0.40	0.82	0.53	0.35	0.42	0.43	0.78	² 0.80	0.65	0.53	0.27	1.37
	Filament		(1)	F1	F2	F3	F4	F4b	F5	F6	F7	F8	F9	F10	F10b	F11	F12	F13	cont filament ^a	mean	median	minimun	maximum

Table 1. Physical parameters of the filaments.

е amplitude, standard deviation $\sigma = FWHM/(2\sqrt{2\ln(2)})$, and width, and beam-deconvolved width derived from the Gaussian fitting. (12)–(16) The amplitude, flattening radius, density profile, width, and beam-deconvolved width derived from the Plummer fitting. a: the amplitude unit is Jy beam⁻¹.



Figure 13. Left column: the filament spine (red solid curve) overlaid on the velocity-integrated intensity image. Magenta cross "x" and cyan plus "+" symbols are continuum cores and NH₂D cores, respectively. Middle column: mean integrated intensity profile and best-fit result (black dots) built by sampling radial cuts (short red solid lines) every 7 or 8 pixels (3".44 corresponds to ~0.019 pc at the source distance of 1.3 kpc) along the spine. The radial distance is the projected distance from the peak emission at a given cut (blue dots in the left column). The error bar represents the standard deviation of the cuts at each radial distance. The orange solid line shows the beam response with a FWHM of ~3." 4. The red solid and green dashed lines present the best-fit results of Gaussian and Plummer fitting, respectively. Right column: the mean $v_{\rm LSR}$ and mean $\sigma_{\rm obs}$ of H¹³CO⁺ line emission variation along the filament. The error bars show the standard deviation of corresponding $v_{\rm LSR}$ and $\sigma_{\rm obs}$. Vertical magenta and cyan lines indicate the positions of associated continuum cores and NH₂D cores, respectively. The red cross "x" and green filled star symbols mark the core mean $\sigma_{\rm obs}$ derived from the H¹³CO⁺ and NH₂D lines, respectively.



 $\operatorname{NGC}6334S$



Figure 13.

21



Figure 13.



Figure 13.

Dec. (J2000)

20"-

40"

-36°04'40"

02'00".

-36°04'40".

02'00"-

20"-

Dec. (J2000)

40"-

02.00"

45"

30"

Dec. (J2000)

15"

-36°04'00"





$\rm NGC\,6334S$

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APPENDIX

A. COLUMN DENSITY

Assuming local thermodynamic equilibrium (LTE), the column density of molecules can be calculated following (Mangum & Shirley 2015)

$$N = C_{\tau} \frac{3h}{8\pi^3 R} \frac{Q_{\rm rot}}{S\mu^2 g_{\rm u}} \frac{\exp(\frac{E_{\rm u}}{kT_{\rm ex}})}{\exp(\frac{h\nu}{kT_{\rm ex}}) - 1} \left(J_{\nu}(T_{\rm ex}) - J_{\nu}(T_{\rm bg})\right)^{-1} \int \frac{T_{\rm R}dv}{f},\tag{A1}$$

where $C_{\tau} = \tau/(1 - \exp(-\tau))$ is the optical depth correction factor, h is the Planck constant, $S\mu^2$ is the line strength multiplied by the square of dipole moment, R is the line intensity, $g_{\rm u}$ is the statistical weight of the upper level, $T_{\rm ex}$ is 1175 the excitation temperature, $T_{\rm bg}$ is the back ground temperature, $E_{\rm u}$ is the energy of the upper state, ν is the transition 1176 frequency, $\int T_{\rm R} dv$ is the velocity-integrated intensity, f is the filling factor, and $Q_{\rm rot}$ is the partition function. Here f 1177 is assumed to be 1 and the $T_{\rm NH_3}$ approximates the $T_{\rm ex}$ of molecular lines (see Section 3.1). Both H¹³CO⁺ and NH₂D 1178 emission are generally optically thin. The NH₂D partition function is $Q_{\rm rot} = 0.73T_{\rm ex}^{3/2} + 6.56$ that is the best-fit result 1179 from a fit to the partition function obtained from CDMS catalogues at the different excitation temperatures of 10-300 1180 K (Müller et al. 2005), while the H¹³CO⁺ partition function can be estimated from $Q_{\rm rot} \approx kT_{\rm ex}/hB + 1/3$ that is 1181 a approximation for diatomic linear molecules (Mangum & Shirley 2015). For NH₂D, the molecular parameters are 1182 15 for $g_{\rm u}$; 11.91 D for $S\mu^2$; 20.68 K for $E_{\rm u}$; 85.926 GHz for ν ; 1/2 for R that is the relative intensity of the main 1183 hyperfine transition with respect to the other hyperfine transitions. For $H^{13}CO^+$, the molecular parameters are 3 for 1184 ¹¹⁸⁵ $g_{\rm u}$; 15.21 D² for $S\mu^2$; 15.21 K for $E_{\rm u}/k$; 86.754288 GHz for ν ; 1 for R.

The $N_{\rm H_2}$ is derived from the continuum emission with

$$N_{\rm H_2} = \eta \frac{S_\nu}{\Omega B_\nu(T_{\rm dust}) \,\kappa_\nu \,\mu \,m_{\rm H}},\tag{A2}$$

where $\eta = 100$ is the gas-to-dust ratio, S_{ν} is the peak flux density, Ω is the beam solid angle, $m_{\rm H}$ is the proton mass, $\mu = 2.8$ is the mean molecular weight of the interstellar medium (Kauffmann et al. 2008), and κ_{ν} is the dust opacity at a frequency of ν . We used $\kappa_{\nu} = 0.235$ cm⁻² g⁻¹ by assuming $\kappa_{\nu} = 10(\nu/1.2$ THz)^{β} cm⁻² g⁻¹ and $\beta = 1.5$ (Hildebrand 1189–11983).

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B. FILAMENT CRITICAL LINE-MASS

Assuming the filament is an infinite self-gravitating isothermal cylinder in hydrostatic equilibrium, the critical linemass of filament can be estimated by (Ostriker 1964)

$$M_{\rm crit} = \frac{2\sigma_{\rm eff}^2}{G},\tag{B3}$$

where σ_{eff} is the effective velocity dispersion and G is the gravitational constant. If the thermal gas pressure is the only force opposing gravity, the $\sigma_{\text{eff}} = c_{\text{s}}$. If the turbulence is the only force against gravity, $\sigma_{\text{eff}} = \sigma_{\text{nth}}$. If both thermal and turbulence supports are considered, $\sigma_{\text{eff}} = \sqrt{\sigma_{\text{nth}}^2 + c_{\text{s}}^2}$. In the last case, the Equation B3 can be written as (see also Hacar et al. 2018):

$$M_{\rm crit}(T,\sigma_{\rm nth}) = \frac{2\,c_{\rm s}^2}{G} \left(1 + \left(\frac{\sigma_{\rm nth}}{c_{\rm s}}\right)^2\right).\tag{B4}$$

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