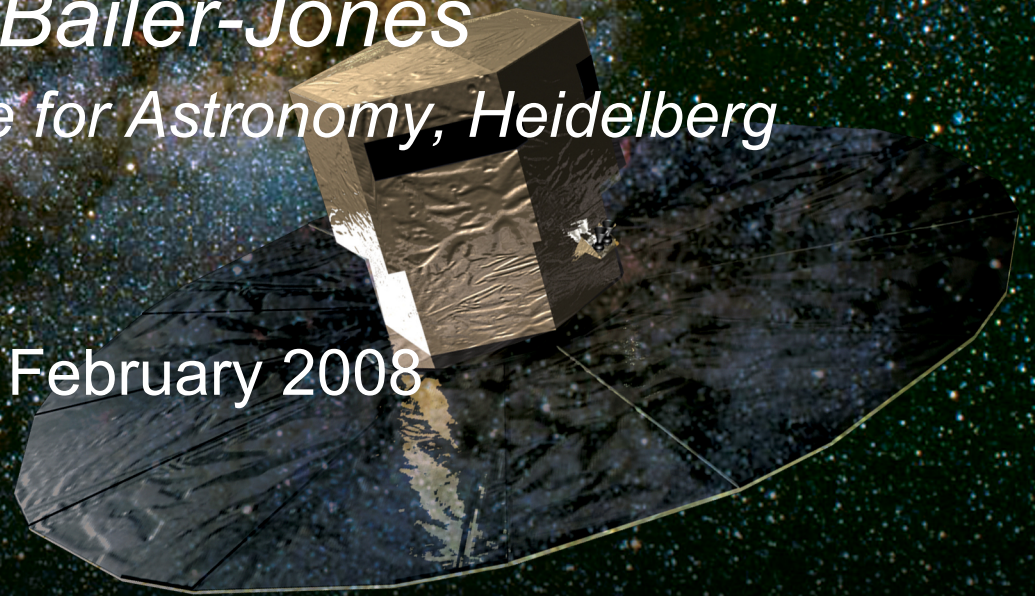


Classification and parameter estimation in astronomy

Coryn Bailer-Jones

Max Planck Institute for Astronomy, Heidelberg

UCL, 4 February 2008



- ◆ learning from astronomical data
- ◆ Gaia Galactic survey mission
- ◆ object classification
- ◆ astrophysical parameter estimation
- ◆ optimizing the survey: heuristic filter design
- ◆ summary

<http://www.mpia.de/homes/calj>

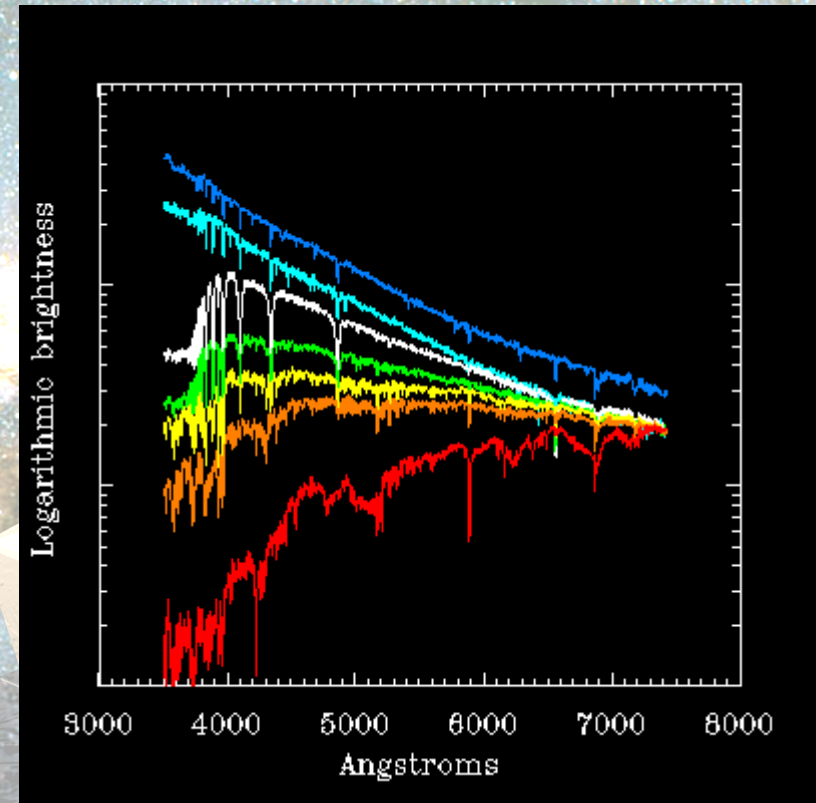
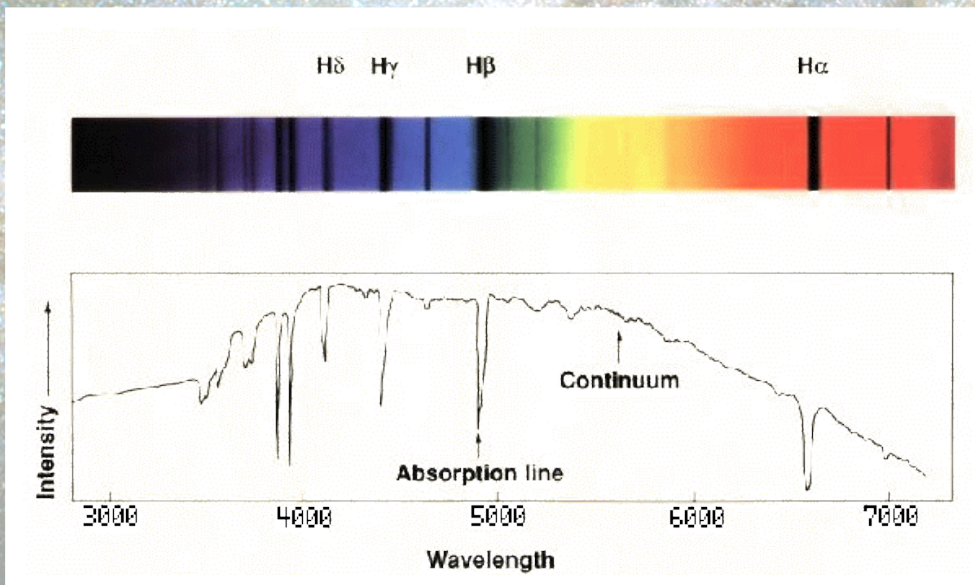
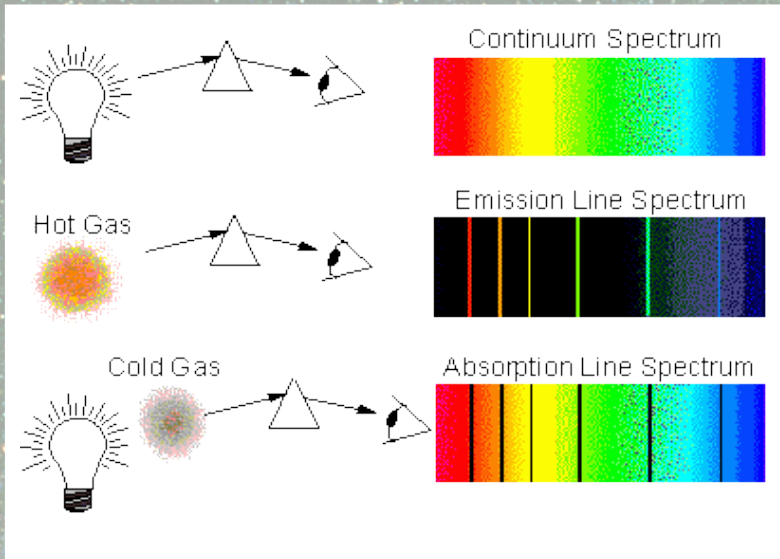
- ♦ Gaia @ MPIA group
 - Christian Elting
 - Paola Re Fiorentin
 - Kester Smith
 - Carola Tiede
 - Vivi Tsalmantza



- ♦ More information on Gaia:
<http://sci.esa.int/Gaia>

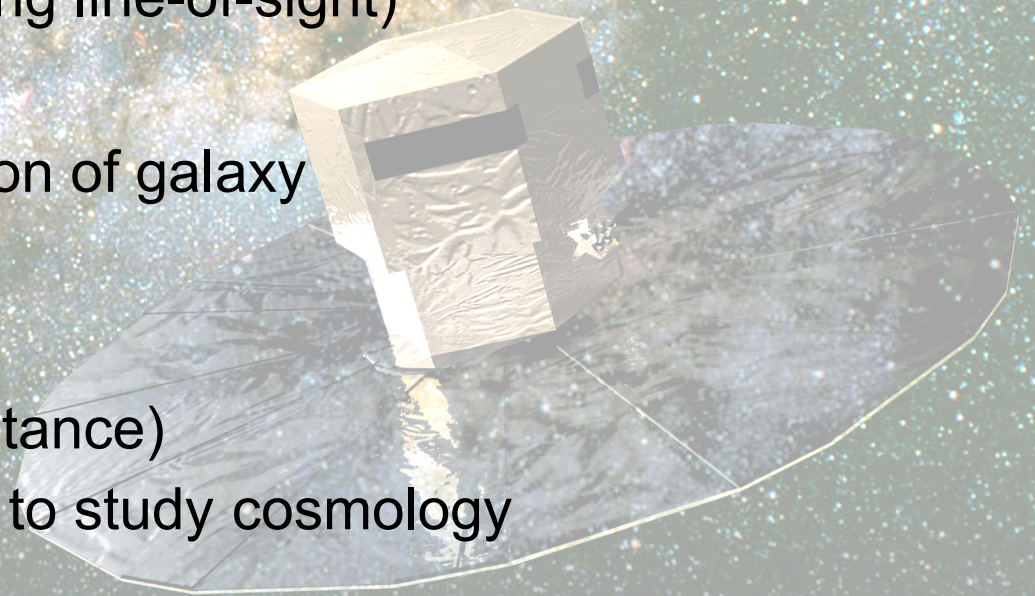


Astronomical spectra

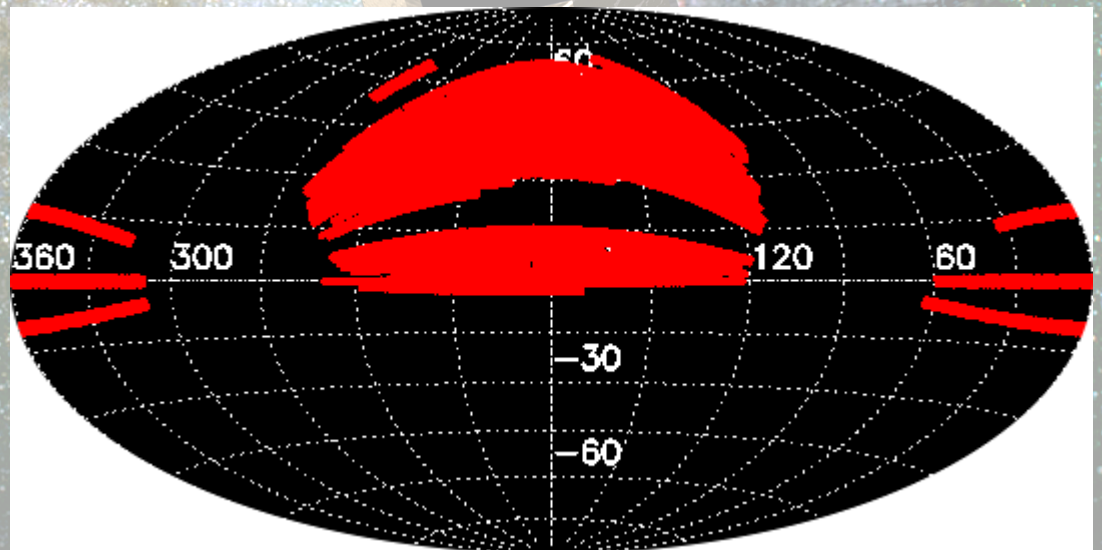
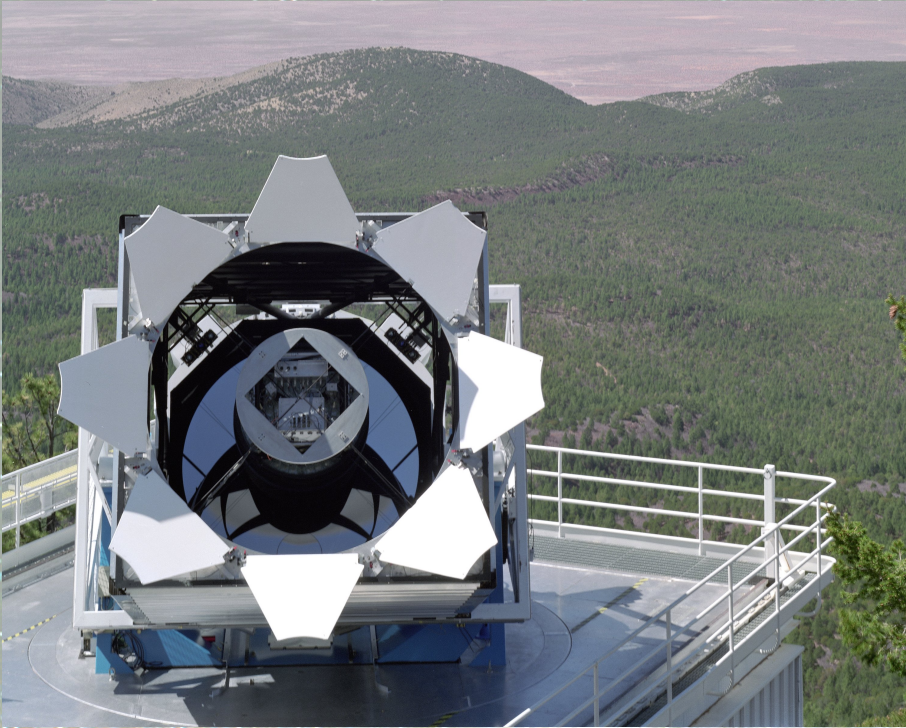


What can we learn from spectra?

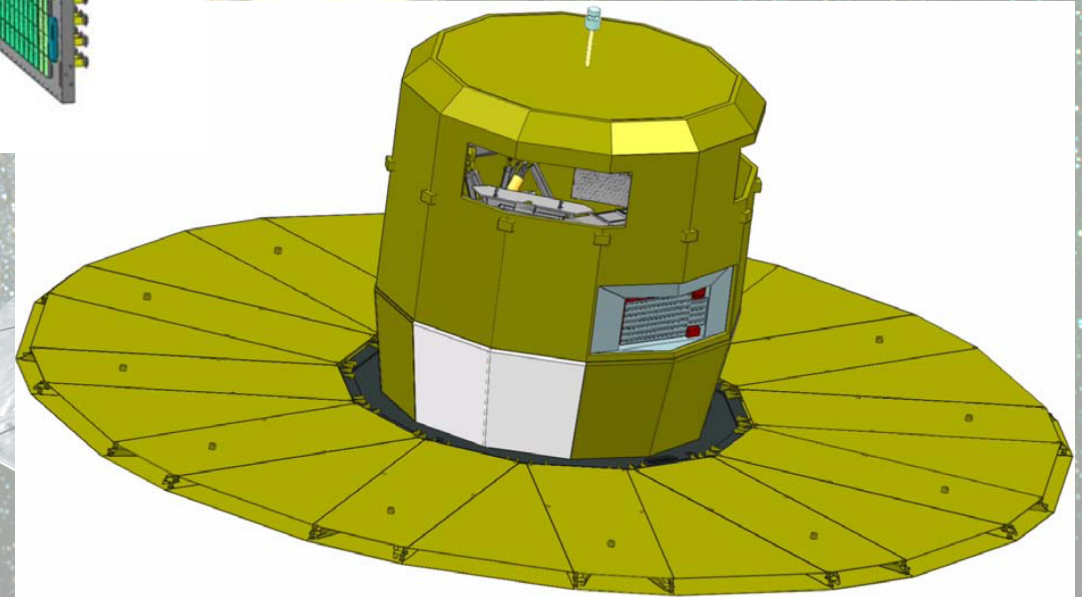
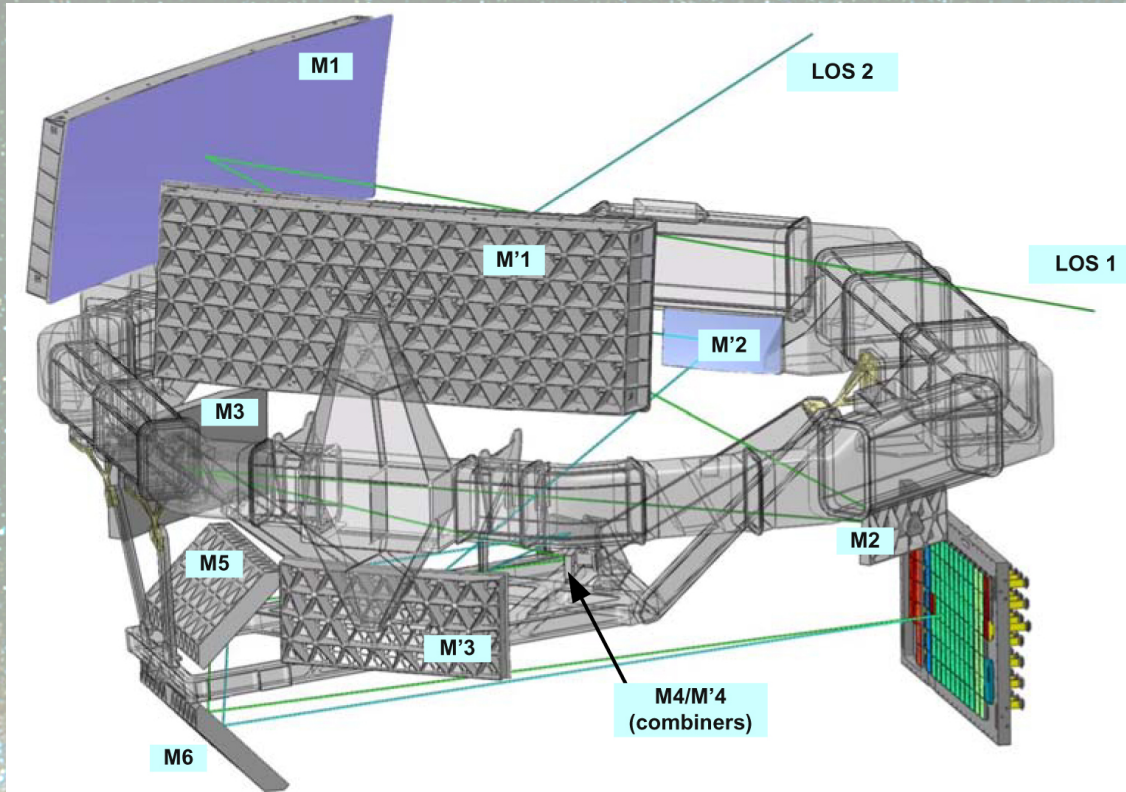
- ▶ object type (classification)
 - overall spectral shape
 - characteristic features
- ▶ stars
 - atmospheric temperature, pressure, abundances
 - derive mass, age, radius (via evolutionary models)
 - interstellar extinction (along line-of-sight)
- ▶ galaxies
 - stellar and gas composition of galaxy
 - infer evolution
- ▶ quasars
 - redshift (cosmological distance)
 - use as background lights to study cosmology



Astronomical surveys

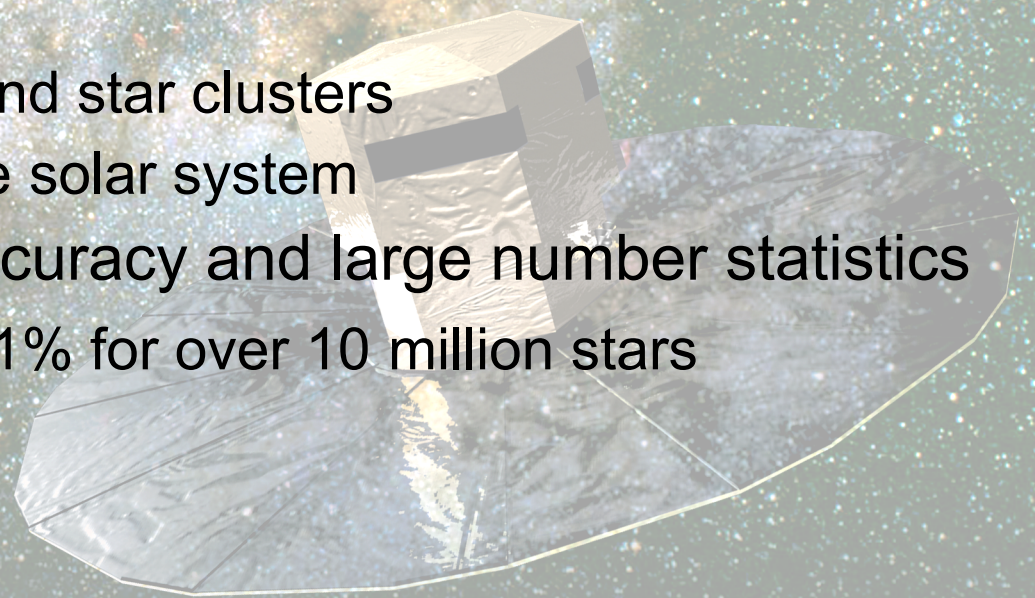


The Gaia Galactic survey mission

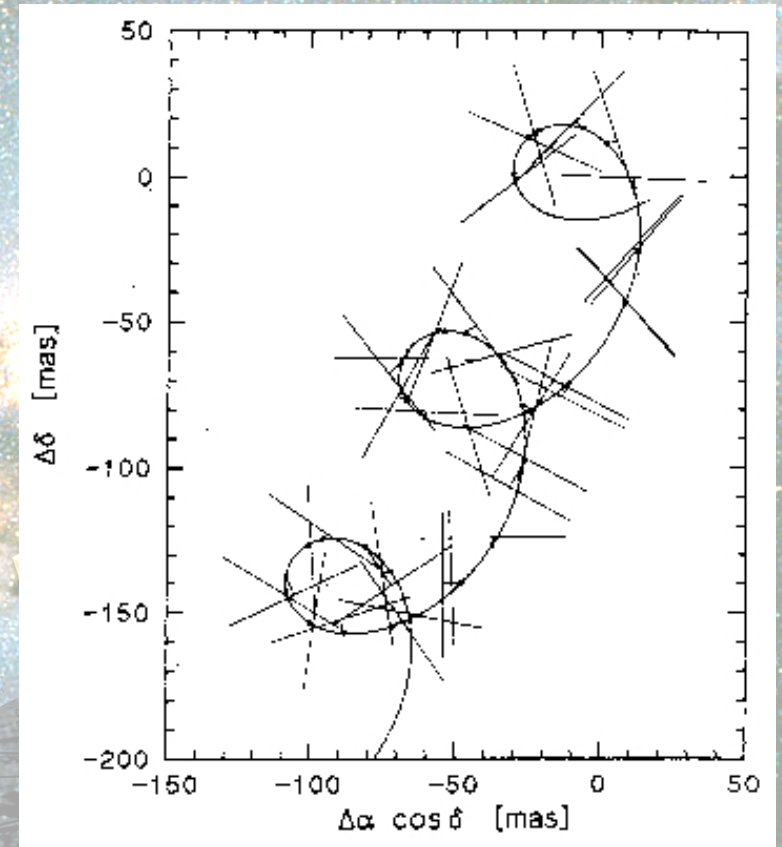
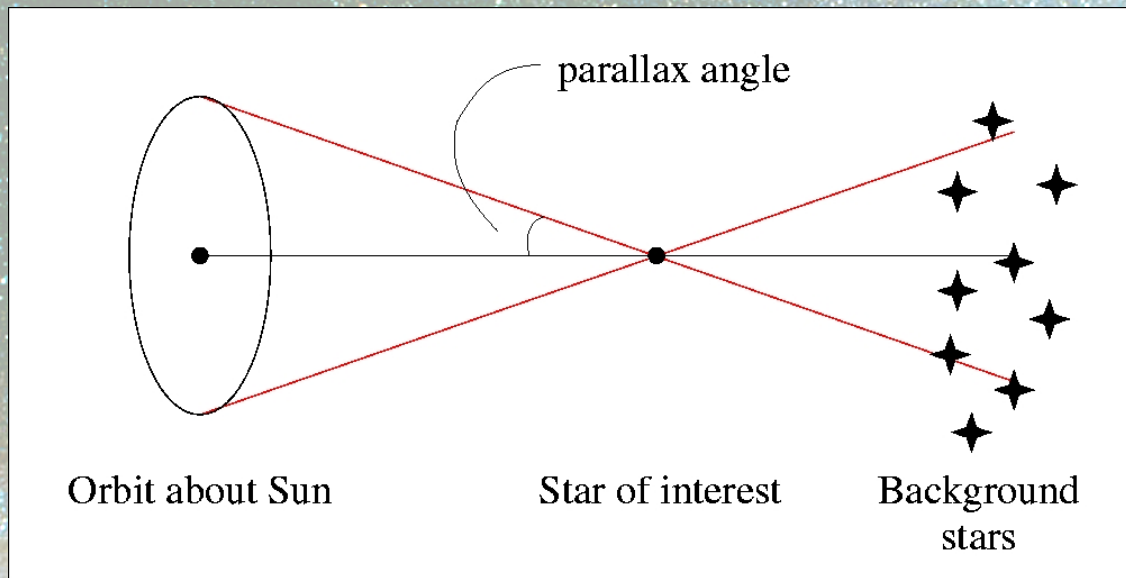


The Gaia Galactic survey mission

- ▶ five-year all sky survey of one billion objects
- ▶ detect objects in real time and measure
 - distances and space velocities
 - spectra (to determine physical properties)
- ▶ Science goals
 - structure, origin and evolution of our Galaxy
 - nature of dark matter
 - better understand stars and star clusters
 - find planets outside of the solar system
- ▶ strength of Gaia is both accuracy and large number statistics
 - distances to accuracy of 1% for over 10 million stars

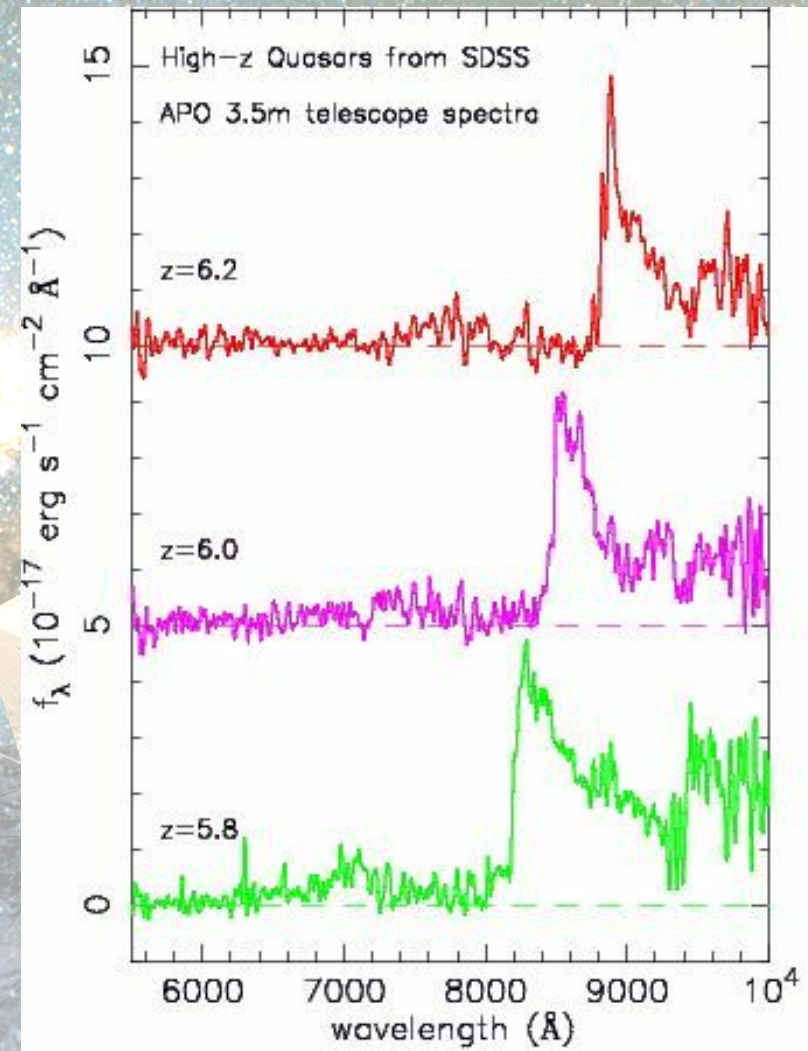


Measuring distances via parallax



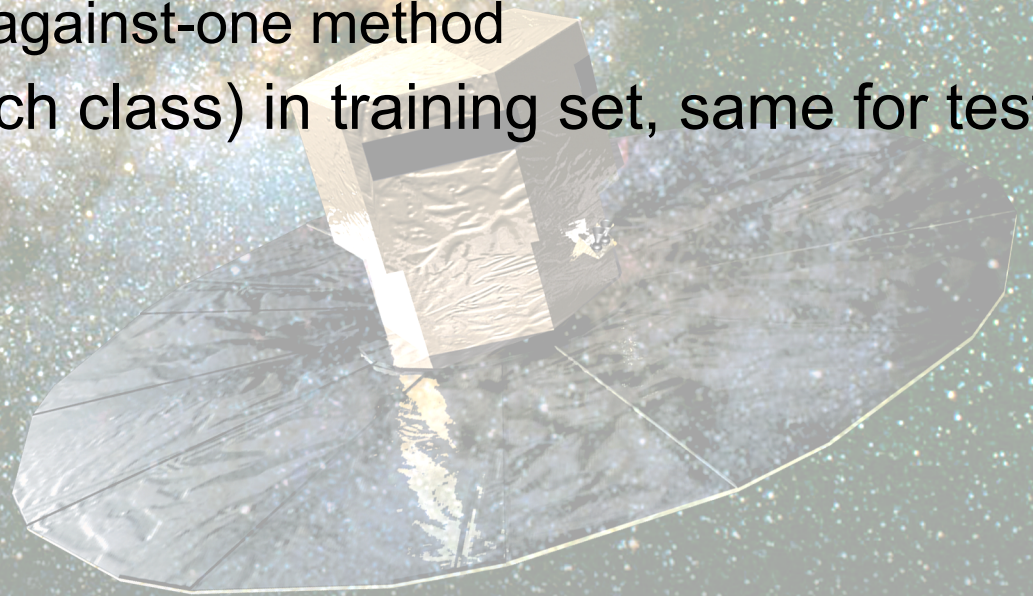
parallax measurements are relative to reference (background) objects

- ▶ extragalactic objects at large distances
- ▶ used to define an inertial reference frame (“fixed background”)
- ▶ characteristic broad emission lines
- ▶ position of lines in spectrum varies due to redshift

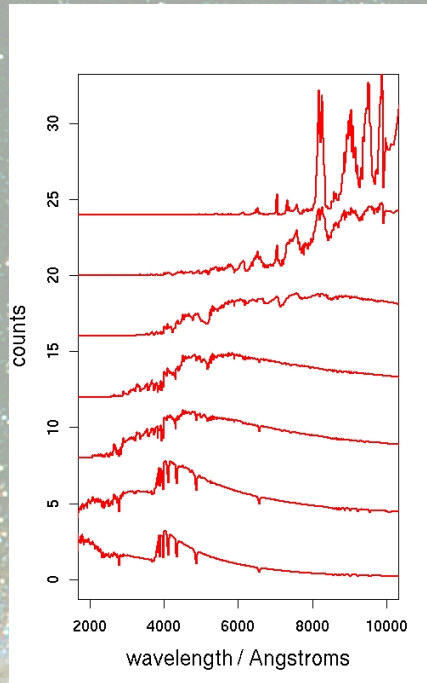


The classification problem

- ◆ “blind” survey
- ◆ object (spectrum) classification via pattern recognition
- ◆ four class problem
 - star, quasar, galaxy, physical binary star
- ◆ support vector machine classifier (libsvm)
 - RBF kernel
 - multiclass using the one-against-one method
- ◆ 8000 objects (~2000 of each class) in training set, same for test

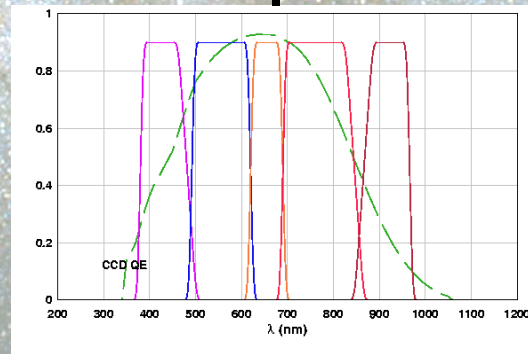


Data simulation



synthetic spectra

instrument
simulator
including
noise



instrument model

```
10001 20.00000 -0.10 -0.29 2500 4.3
#674e+05 7.7241e-01 0.0000e+00 1.902
#5e-04 5.2929e-03 6.7152e-02 6.7281e
#-04 3.3129e-04 4.4695e-04 1.5668e-0
#3 2.0442e-03 1.8526e-03 1.0861e-02
#1.6168e-02 1.1581e-02 3.8494e-02 7.
#0319e-02
10002 20.00000 -0.10 -0.29 2800 4.3
#856e+05 7.6885e-01 0.0000e+00 8.136
#1e-04 5.5531e-03 6.7737e-02 3.9509e
#-04 7.6133e-04 5.0675e-04 1.6689e-0
#3 2.0563e-03 1.8983e-03 1.0170e-02
#1.7575e-02 1.2697e-02 4.0409e-02 6.
#8905e-02
10003 20.00000 -0.10 -0.29 3000 4.3
#642e+05 7.7226e-01 6.3604e-05 8.551
#4e-04 5.2069e-03 6.7463e-02 0.0000e
#+00 8.2641e-04 3.3651e-04 1.4364e-0
#3 1.9594e-03 1.3885e-03 9.1568e-03
#1.7968e-02 1.2089e-02 3.8761e-02 7.
#0228e-02
10004 20.00000 -0.10 -0.29 3200 4.4
#211e+05 7.6343e-01 0.0000e+00 1.199
#1e-03 5.8359e-03 6.8723e-02 2.9065e
#-04 1.4214e-03 6.5282e-04 1.8446e-0
#3 3.2223e-03 1.9828e-03 1.0671e-02
#2.0650e-02 1.2534e-02 4.1652e-02 6.
--- base12.2.1f_01_g=20.1.nphot
```

fluxes
and estimated
covariances

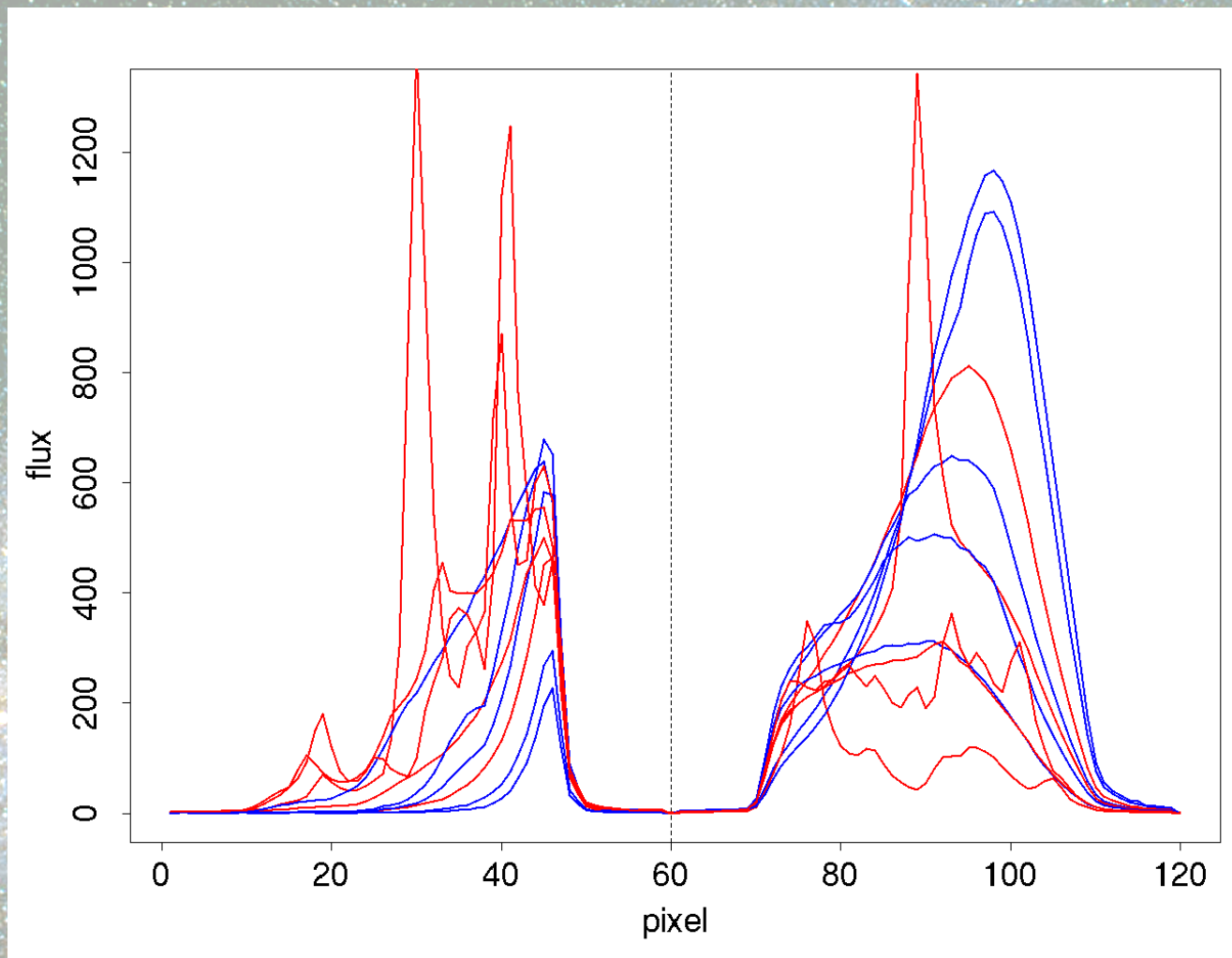
```
10001 20.00000 -0.10 -0.29 2500 4.3
#674e+05 7.7241e-01 0.0000e+00 1.902
#5e-04 5.2929e-03 6.7152e-02 6.7281e
#-04 3.3129e-04 4.4695e-04 1.5668e-0
#3 2.0442e-03 1.8526e-03 1.0861e-02
#1.6168e-02 1.1581e-02 3.8494e-02 7.
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#-04 7.6133e-04 5.0675e-04 1.6689e-0
#3 2.0563e-03 1.8983e-03 1.0170e-02
#1.7575e-02 1.2697e-02 4.0409e-02 6.
#8905e-02
10003 20.00000 -0.10 -0.29 3000 4.3
#642e+05 7.7226e-01 6.3604e-05 8.551
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10004 20.00000 -0.10 -0.29 3200 4.4
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#1e-03 5.8359e-03 6.8723e-02 2.9065e
#-04 1.4214e-03 6.5282e-04 1.8446e-0
#3 3.2223e-03 1.9828e-03 1.0671e-02
#2.0650e-02 1.2534e-02 4.1652e-02 6.
--- base12.2.1f_01_g=20.1.nphot
```

training set

```
10001 20.00000 -0.10 -0.29 2500 4.3
#674e+05 7.7241e-01 0.0000e+00 1.902
#5e-04 5.2929e-03 6.7152e-02 6.7281e
#-04 3.3129e-04 4.4695e-04 1.5668e-0
#3 2.0442e-03 1.8526e-03 1.0861e-02
#1.6168e-02 1.1581e-02 3.8494e-02 7.
#0319e-02
10002 20.00000 -0.10 -0.29 2800 4.3
#856e+05 7.6885e-01 0.0000e+00 8.136
#1e-04 5.5531e-03 6.7737e-02 3.9509e
#-04 7.6133e-04 5.0675e-04 1.6689e-0
#3 2.0563e-03 1.8983e-03 1.0170e-02
#1.7575e-02 1.2697e-02 4.0409e-02 6.
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#+00 8.2641e-04 3.3651e-04 1.4364e-0
#3 1.9594e-03 1.3885e-03 9.1568e-03
#1.7968e-02 1.2089e-02 3.8761e-02 7.
#0228e-02
10004 20.00000 -0.10 -0.29 3200 4.4
#211e+05 7.6343e-01 0.0000e+00 1.199
#1e-03 5.8359e-03 6.8723e-02 2.9065e
#-04 1.4214e-03 6.5282e-04 1.8446e-0
#3 3.2223e-03 1.9828e-03 1.0671e-02
#2.0650e-02 1.2534e-02 4.1652e-02 6.
--- base12.2.1f_01_g=20.1.nphot
```

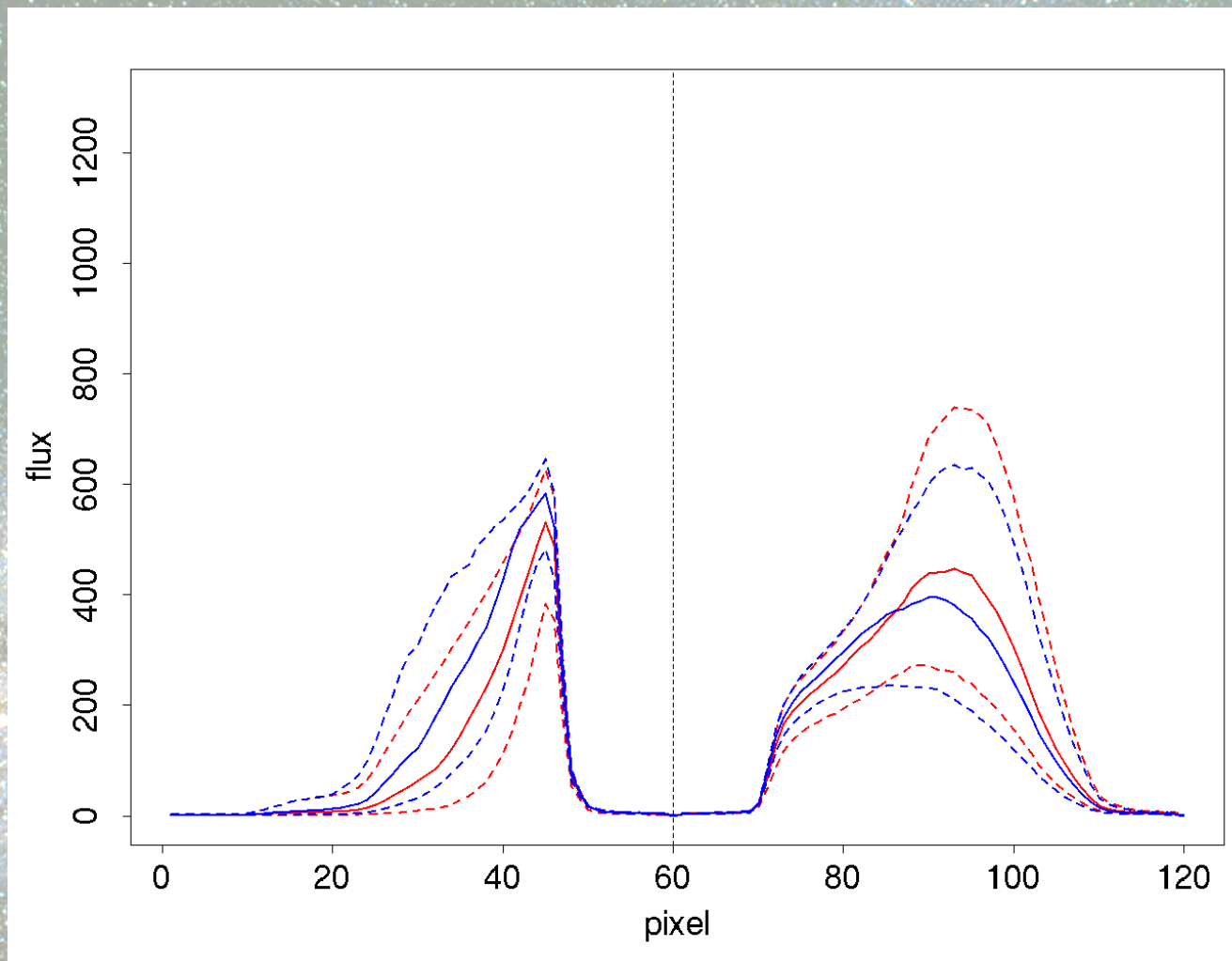
test set

Example Gaia spectra



blue: star red: quasar

Gaia spectral data



blue: star red: quasar

solid: median

dashed: upper and lower quartiles

Classification results: contingency table

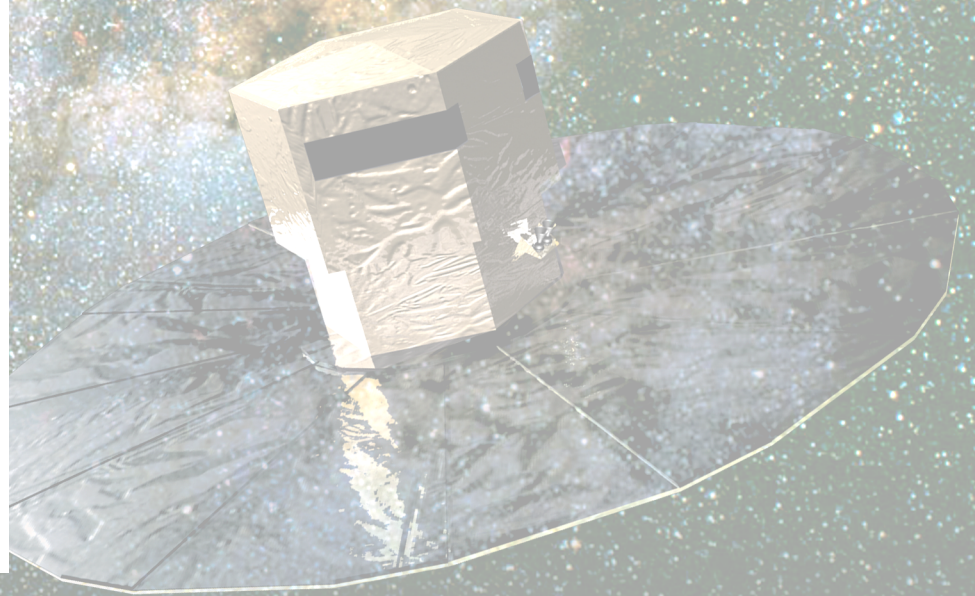
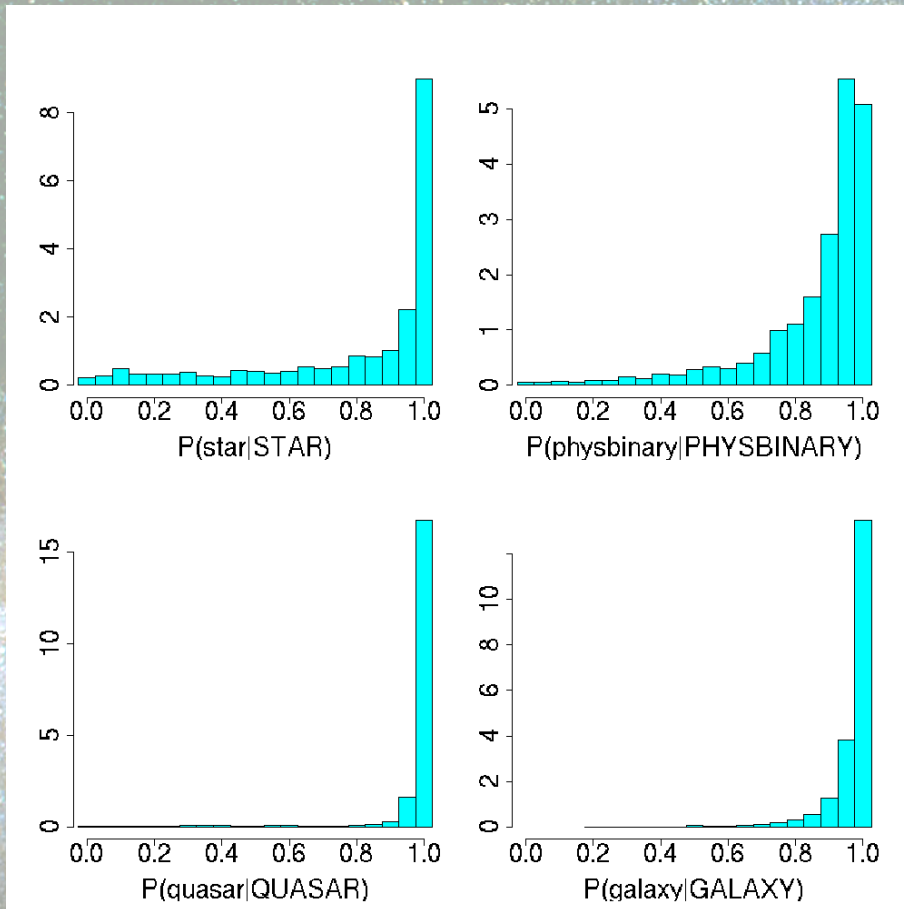
	galaxy	physbin	quasar	star
GALAXY	99.65	0.00	0.35	0.00
PHYSBIN	0.00	94.38	0.15	5.46
QUASAR	2.93	0.05	96.81	0.21
STAR	0.10	13.99	3.16	82.75

- stars and physbin (physical binaries) are hard to distinguish, even in principle
- use output probabilities to vary *completeness* and *contamination* of a sample

Classifier confidence

how well does it find the correct objects?

$P(\text{class} \mid \text{CLASS})$



classifier output probability →

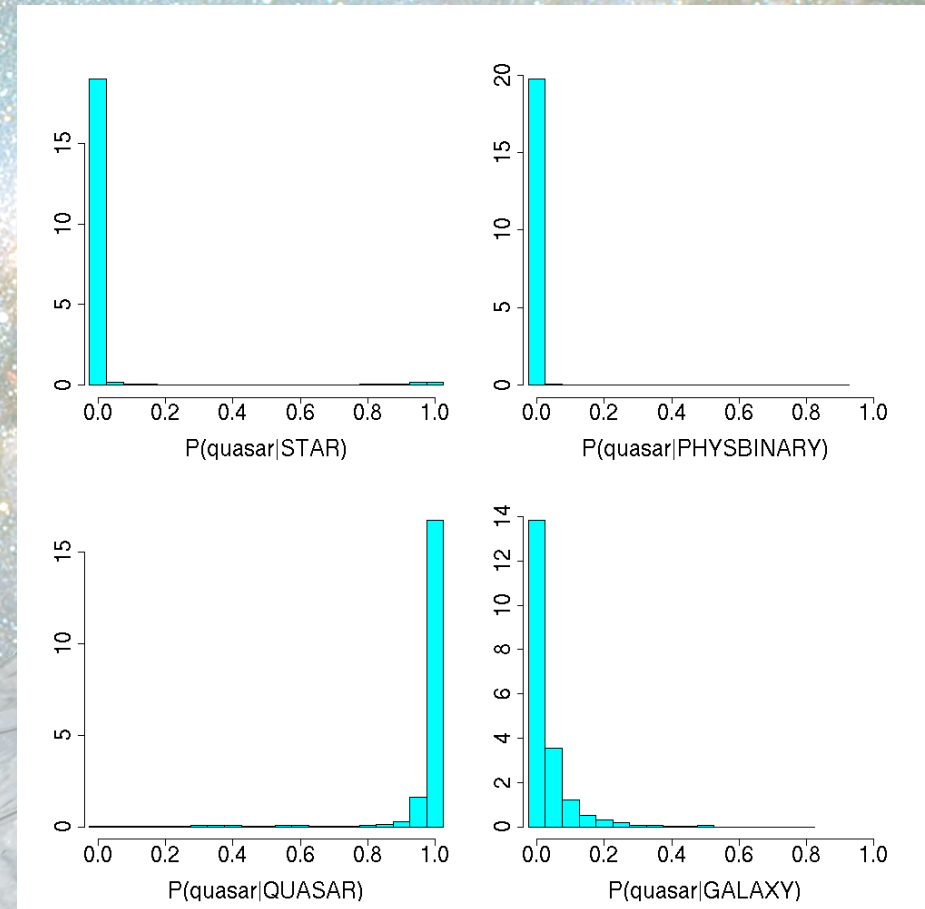
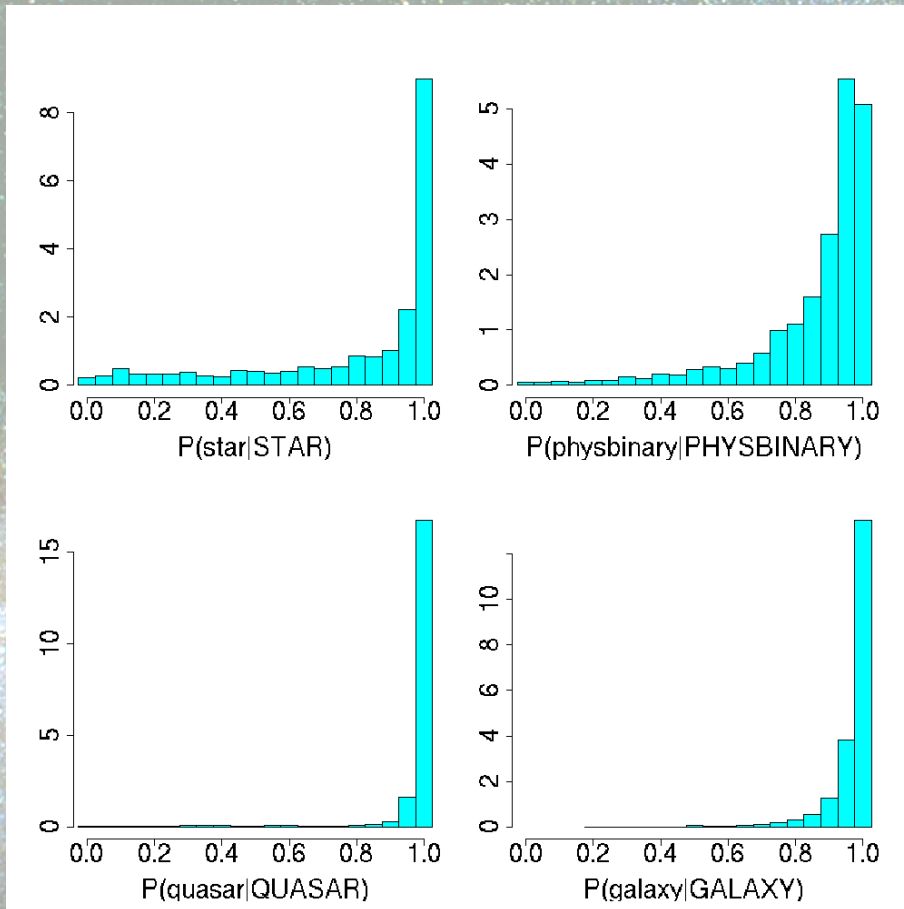
Classifier confidence

how well does it find the correct objects?

$P(\text{class} \mid \text{CLASS})$

how much many false positives in the quasar sample?

$P(\text{quasar} \mid \text{CLASS})$

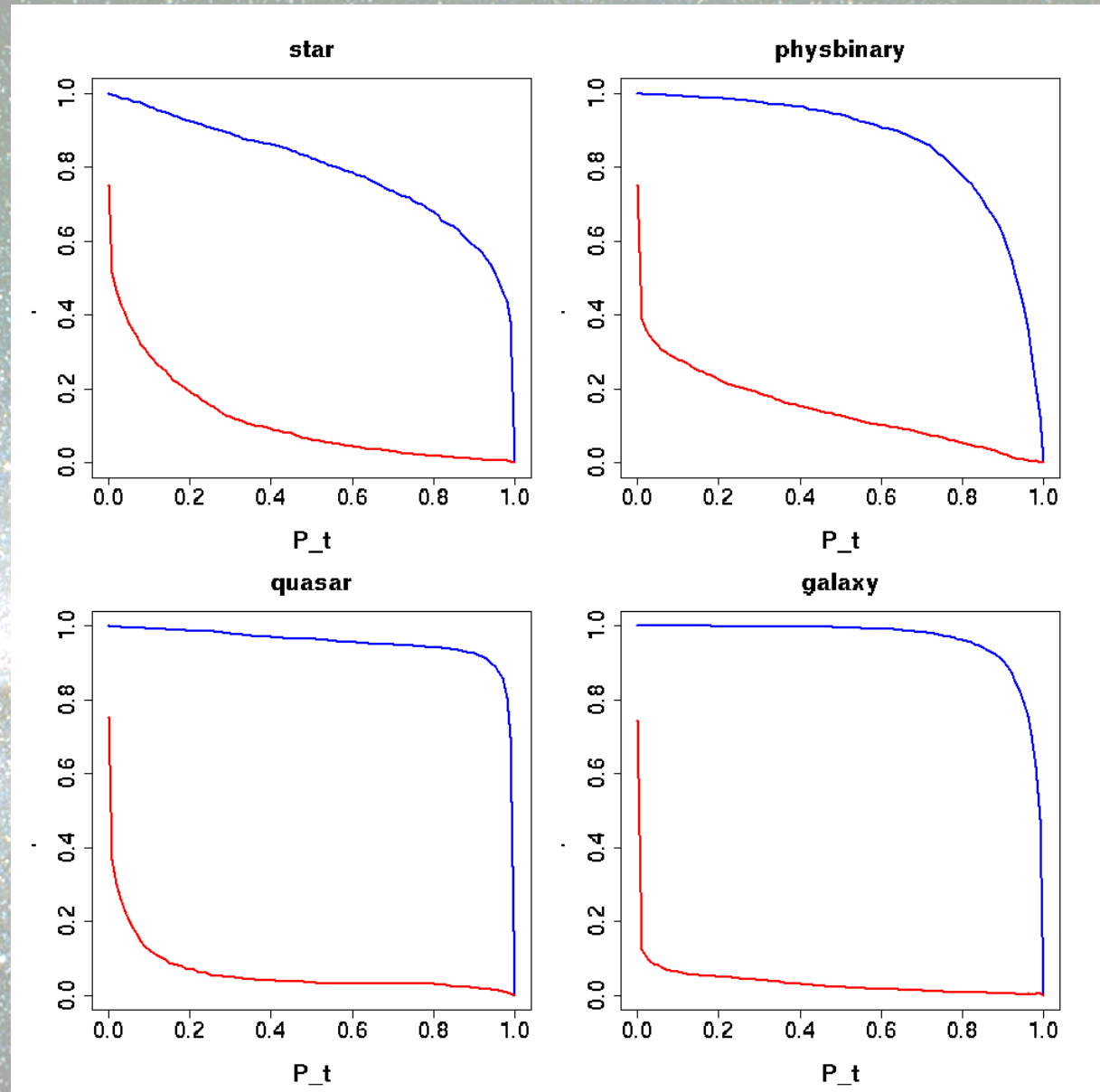


classifier output probability →

Sample completeness & contamination

select threshold to
build a sample

blue = completeness
red = contamination

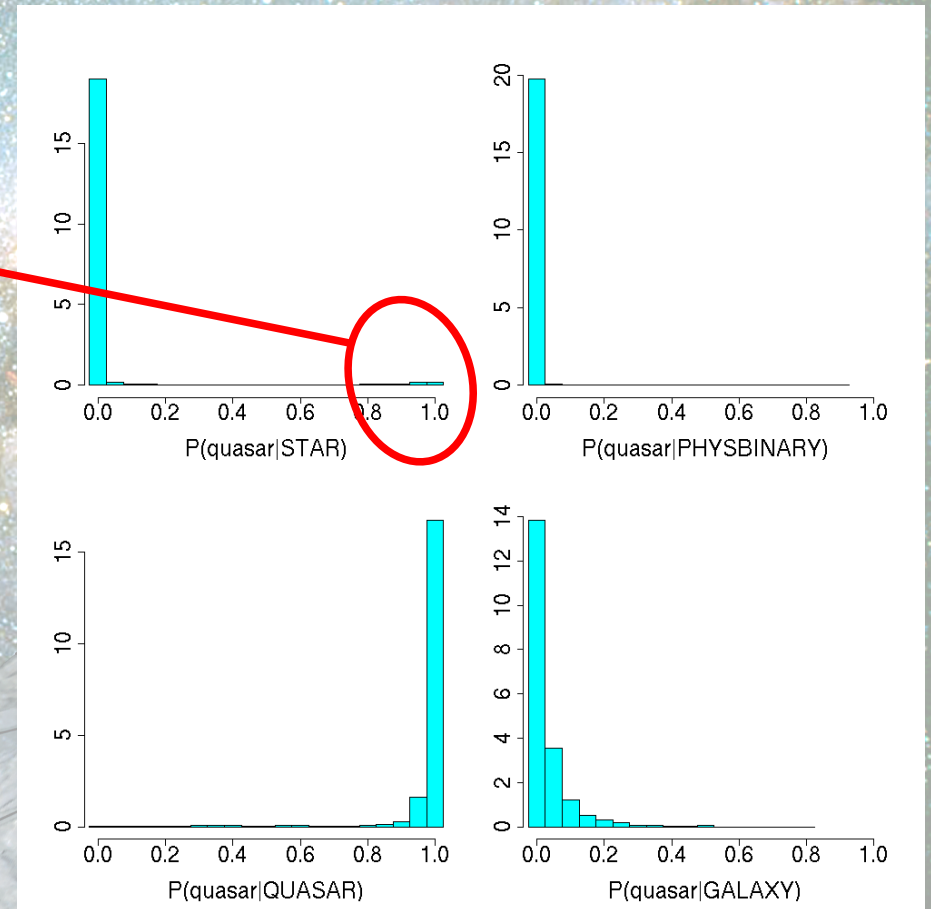


threshold probability \longrightarrow

Classifier confidence

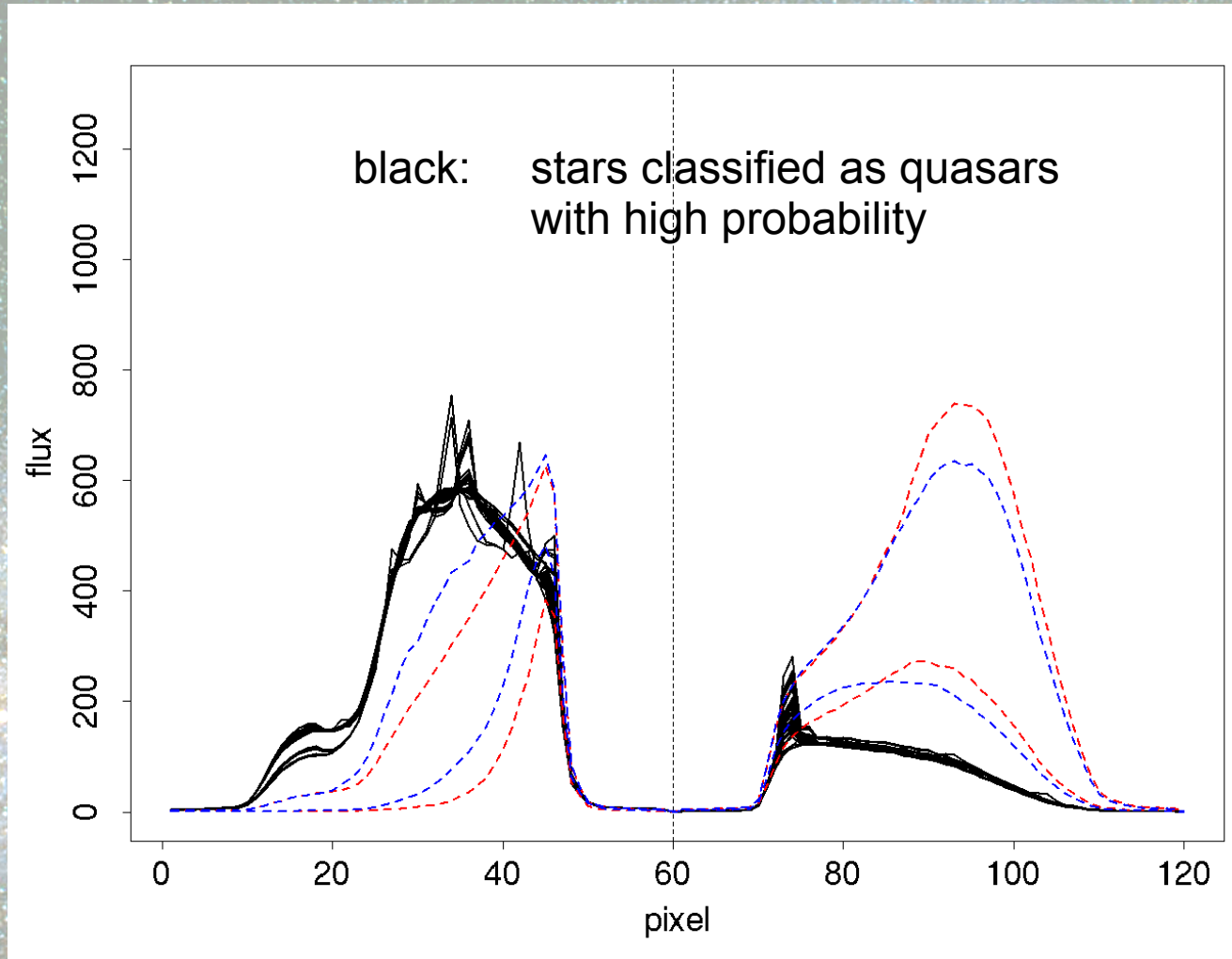
$P(\text{quasar} \mid \text{CLASS})$

small but high confidence
contamination of quasars
by stars



classifier output probability →

What is contaminating the quasar sample?

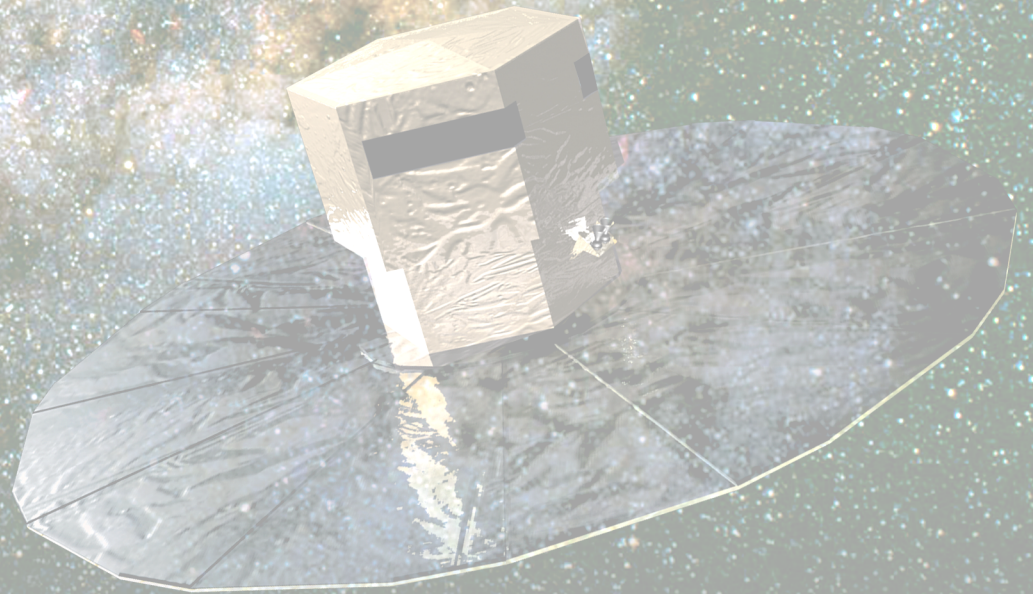


blue: star red: quasar

solid: median
dashed: upper and lower quartiles

Meet reality: population fractions

- ♦ in reality quasars are rare compared to stars (ca. 1000 times)
- ♦ don't modify training sample distribution/re-train
- ♦ instead
 - modify priors
 - treat SVM outputs as likelihoods



Meet reality: population fractions

- ♦ in reality quasars are rare compared to stars (ca. 1000 times)
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$$P^{mod}(i) \propto P^{nom}(i) \frac{f_j^{mod}}{f_j^{nom}}$$

$P(i)$ = posterior probability that object is in class i

f_j = prior fraction of objects in true class j

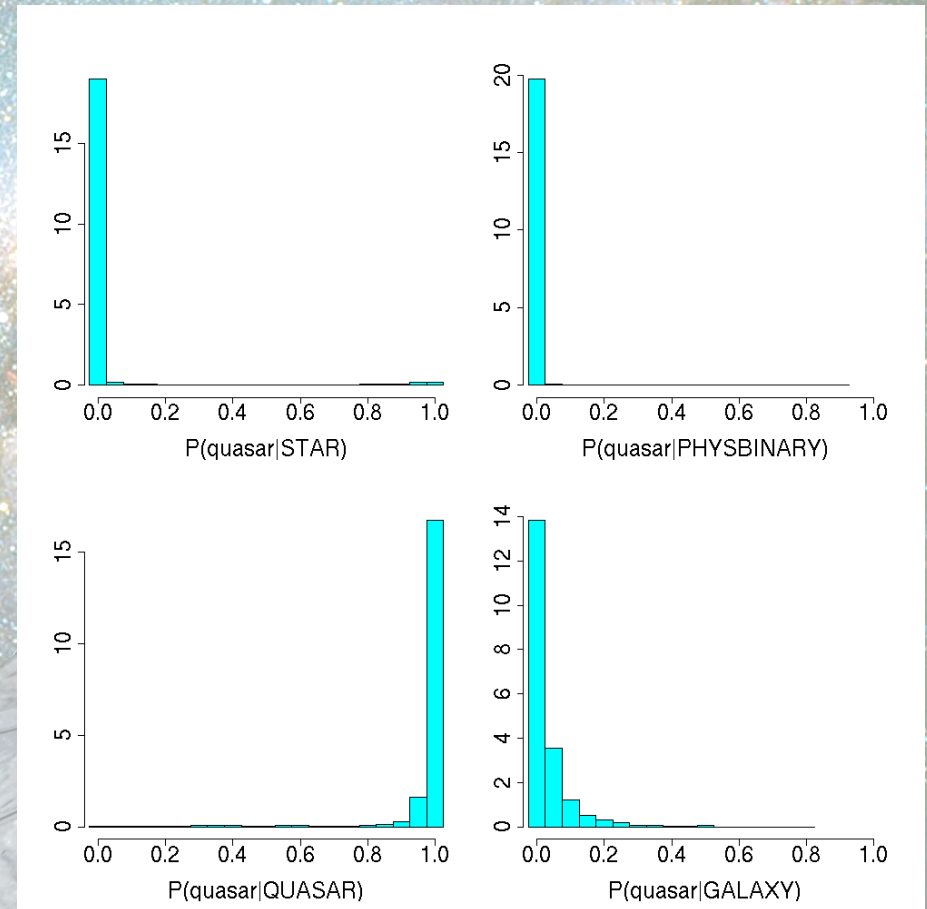
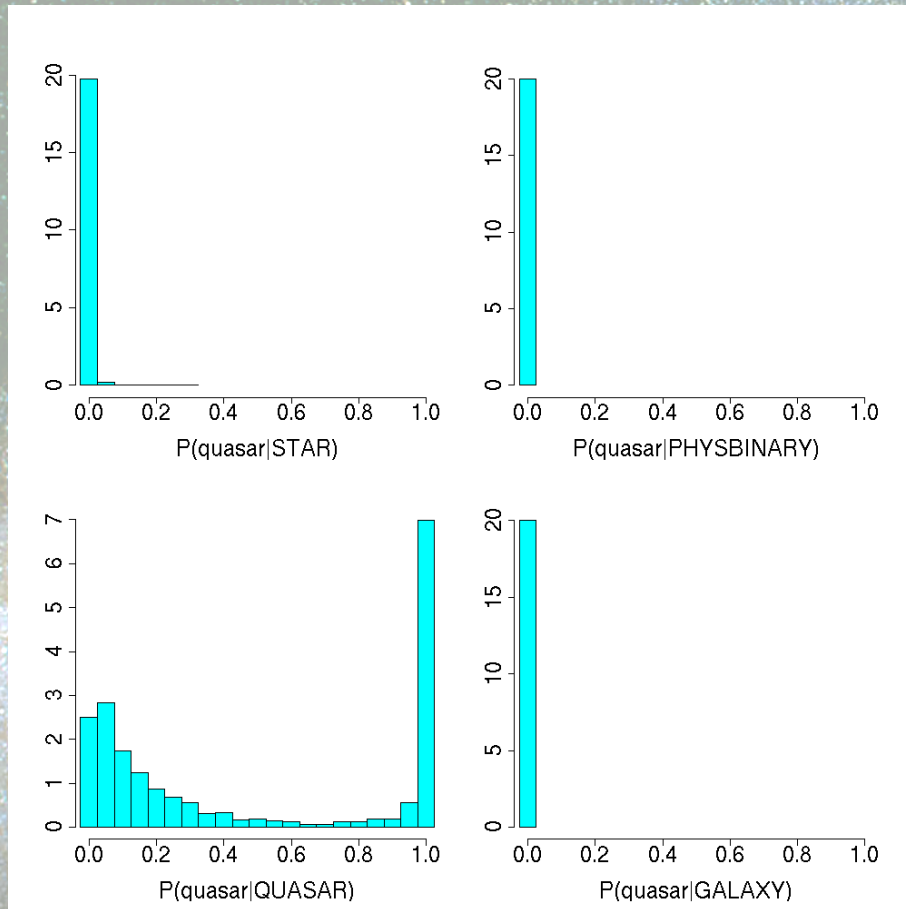
mod = modified, nom = nominal

Classifier confidence: nominal vs. modified

$P(\text{quasar} \mid \text{CLASS})$

modified population

nominal population



classifier output probability →

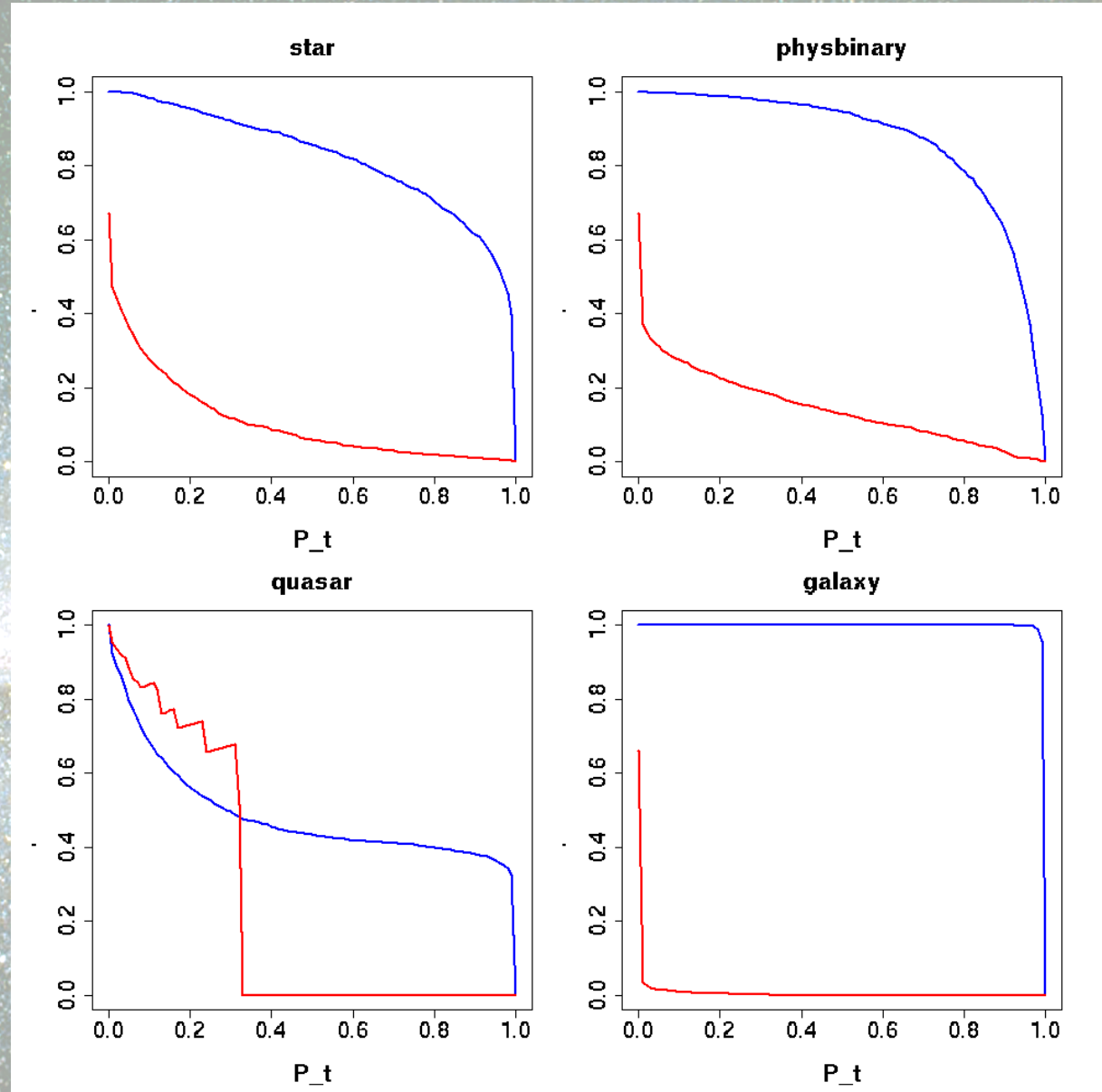
Modified population fractions (priors)

blue = completeness

red = contamination

relative fractions:

star	1
physbinary	1
quasar	0.001
galaxy	1



threshold probability \longrightarrow

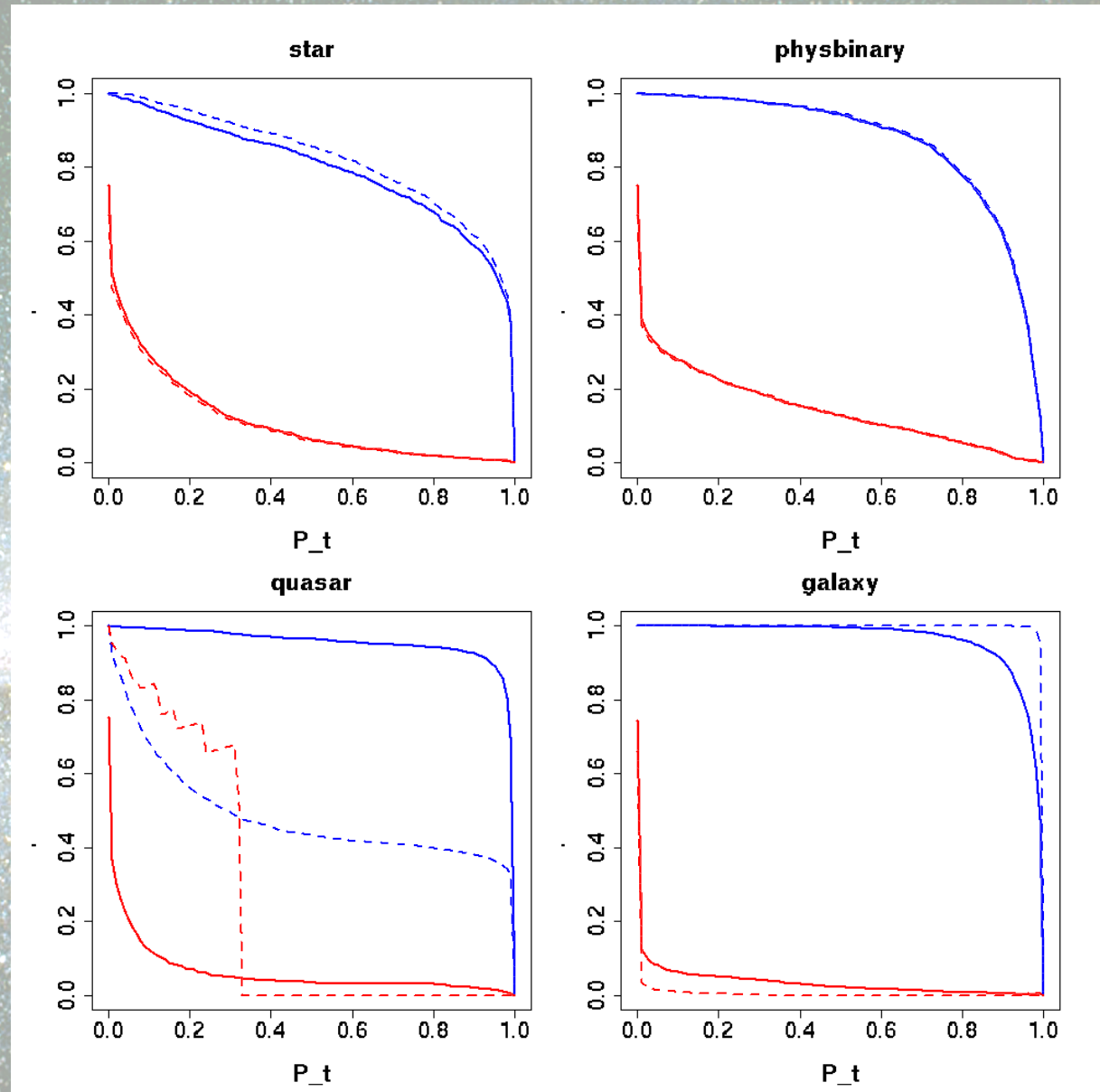
Modified population fractions (priors)

blue = completeness

red = contamination

solid = nominal
fractions
(equal)

dashed = modified
fractions
(quasars 1000
times rarer)



threshold probability \longrightarrow

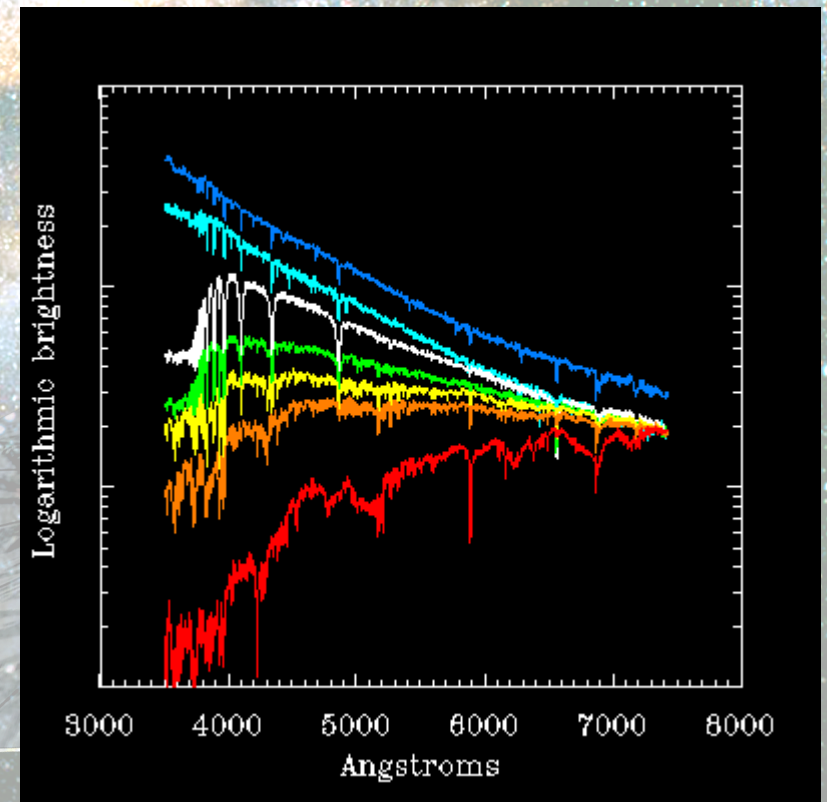
Comparison of different ML models

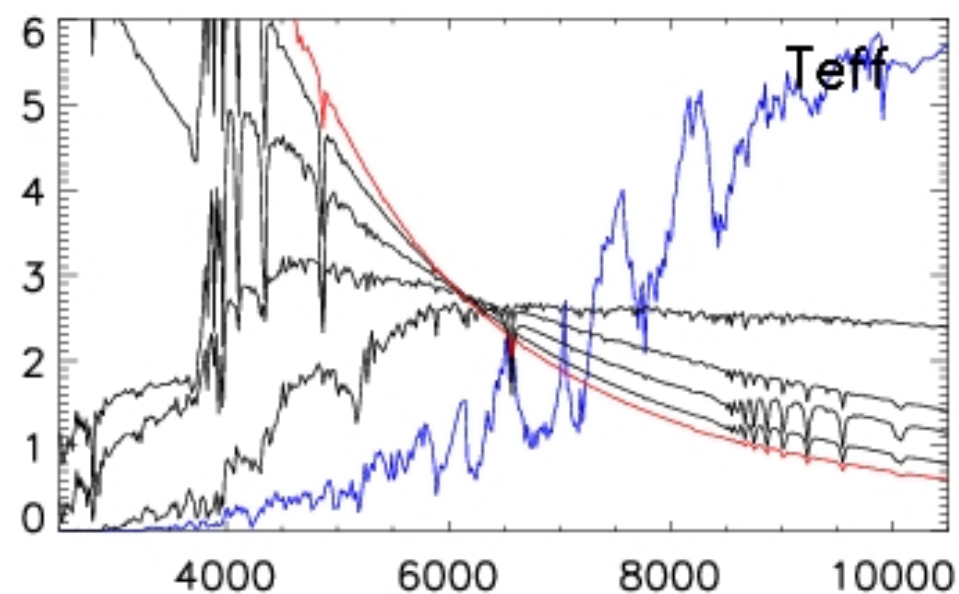
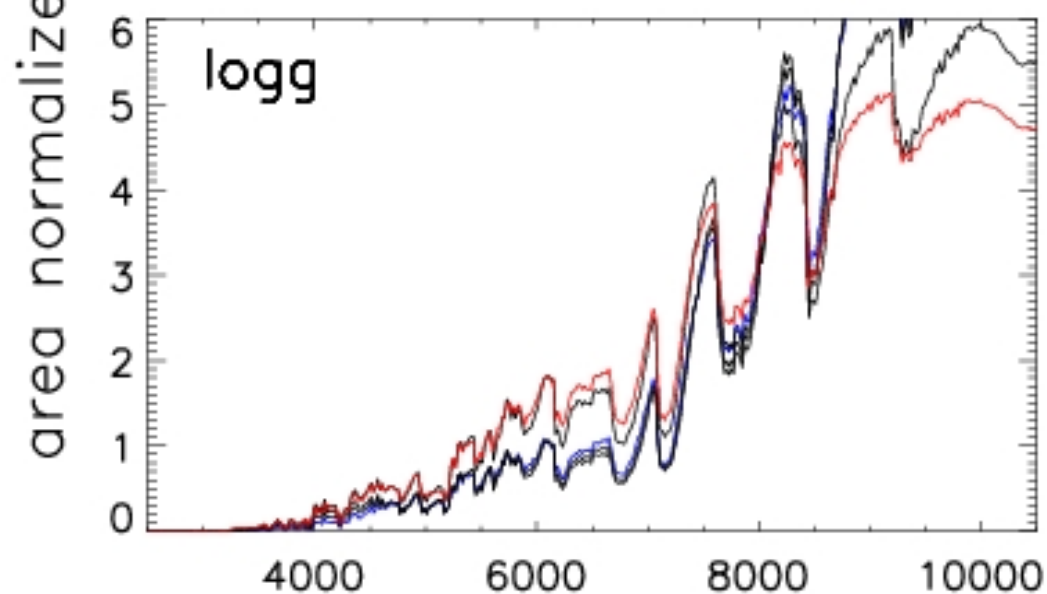
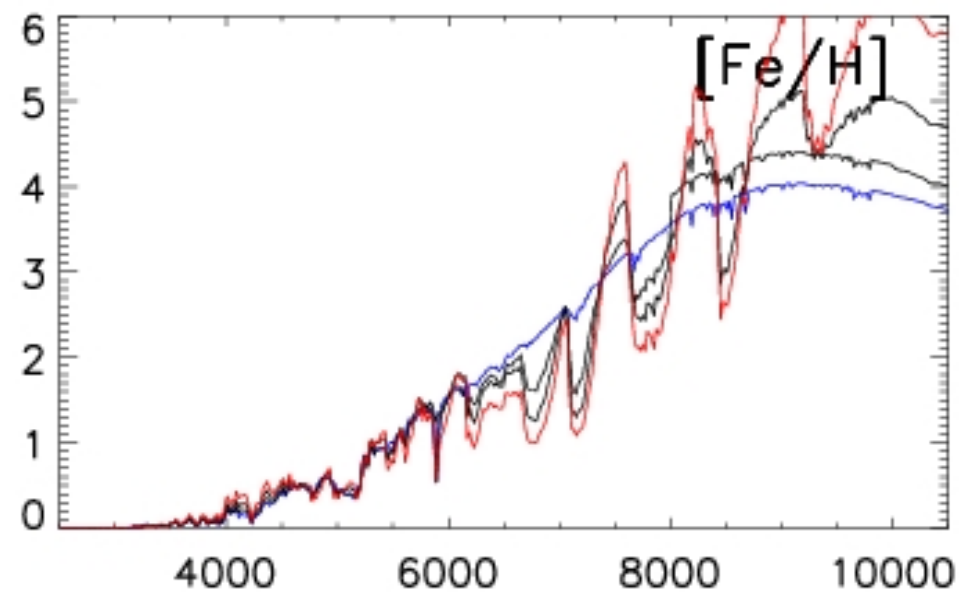
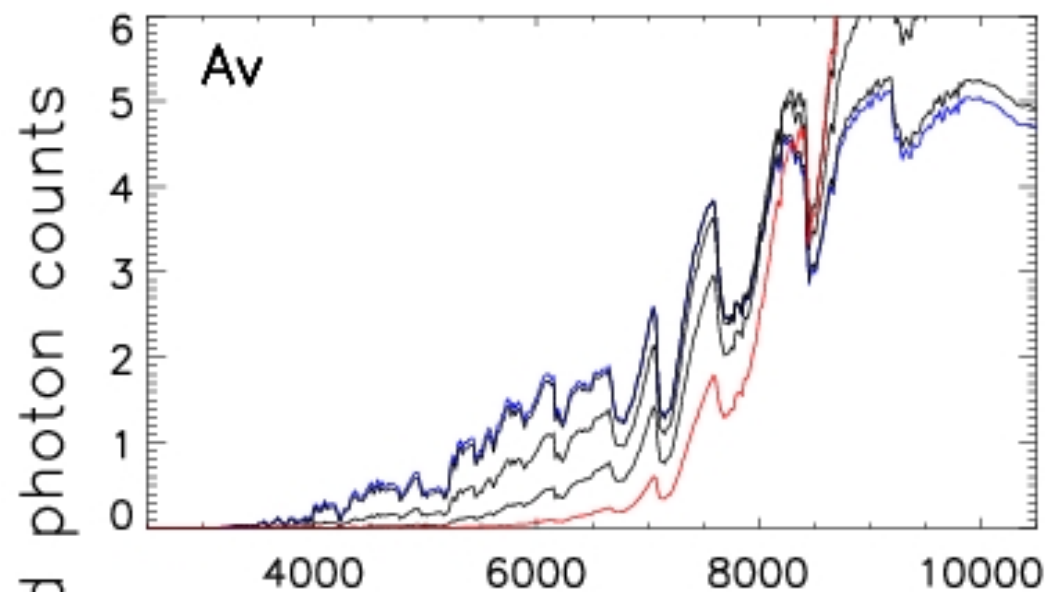
	spectra only		spectra + astrometry	
	K=4	K=3	K=4	K=3
SVM	10.4	2.5	8.3	0.6
Boosting	37.8	33.9	13.0	1.5
MLP	9.4	1.8	7.5	0.2
Mclust	10.9	0.8	9.4	0.1
RBF	38.5	24.0	27.1	15.3

overall classification error (percent)
class assignment via highest probability
K=3: 3 classes only (star and physbin merged)

Estimating stellar parameters

- ▶ several astrophysical parameters (APs) of interest
 - effective temperature, T_{eff}
 - surface gravity, $\log g$
 - abundance, $[\text{Fe}/\text{H}]$
 - interstellar extinction, A_V
- ▶ different nature and degree of impact on the spectra





wavelength / Å

Ranges:

$A_V = \{0, 10\}$

$[Fe/H] = \{-2.5, 0.5\}$

$\log g = \{0.5, 4.5\}$

$T_{\text{eff}} = \{3350, 35000\}$

Fixed values:

$A_V = 0, \quad [Fe/H] = 0.0$

$\log g = 4.5, \quad T_{\text{eff}} = 3500$

Strong vs. weak parameters

Minimum distance
(nearest neighbour)
method

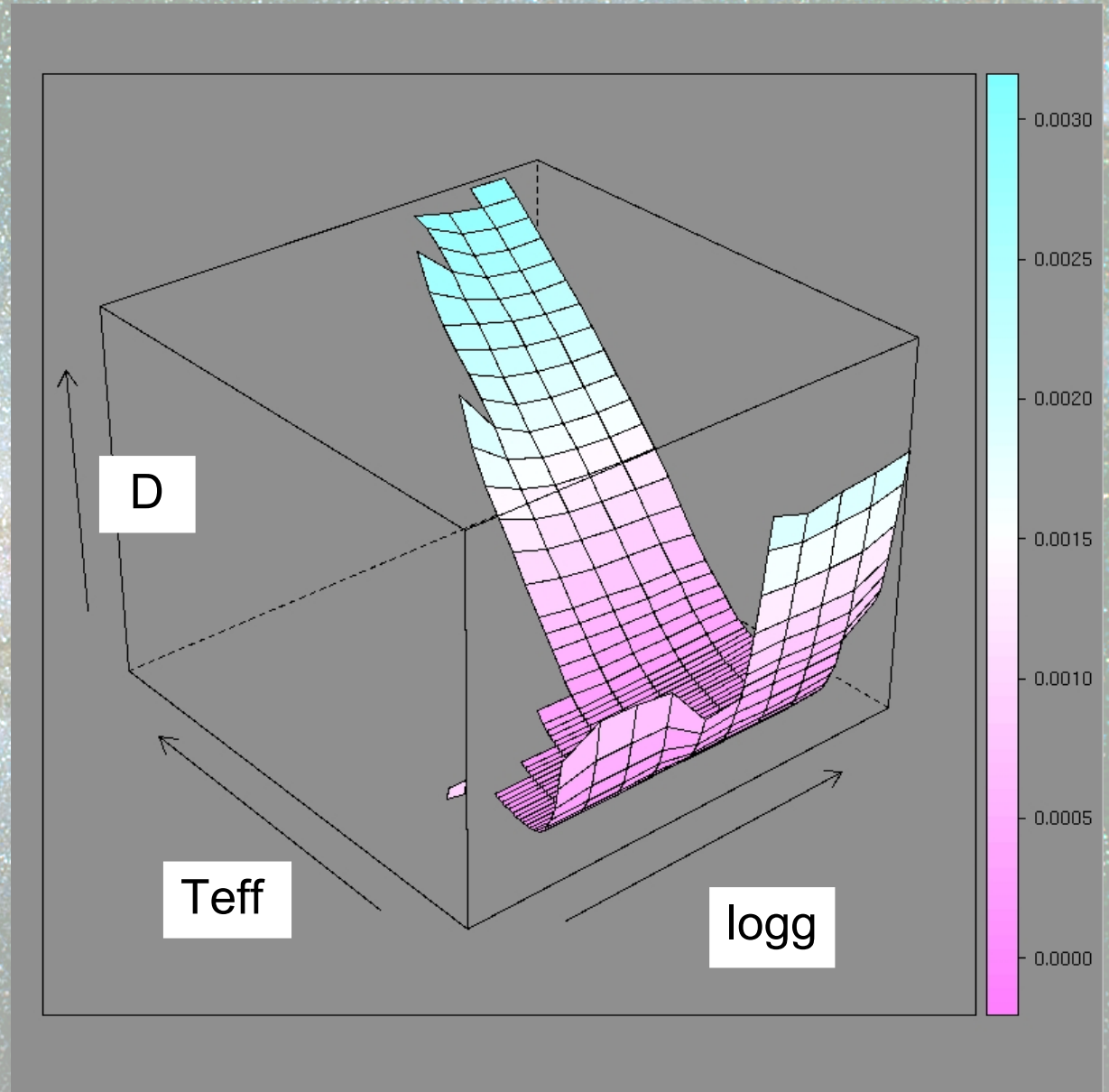
AP ranges:

$$A_v = 0$$

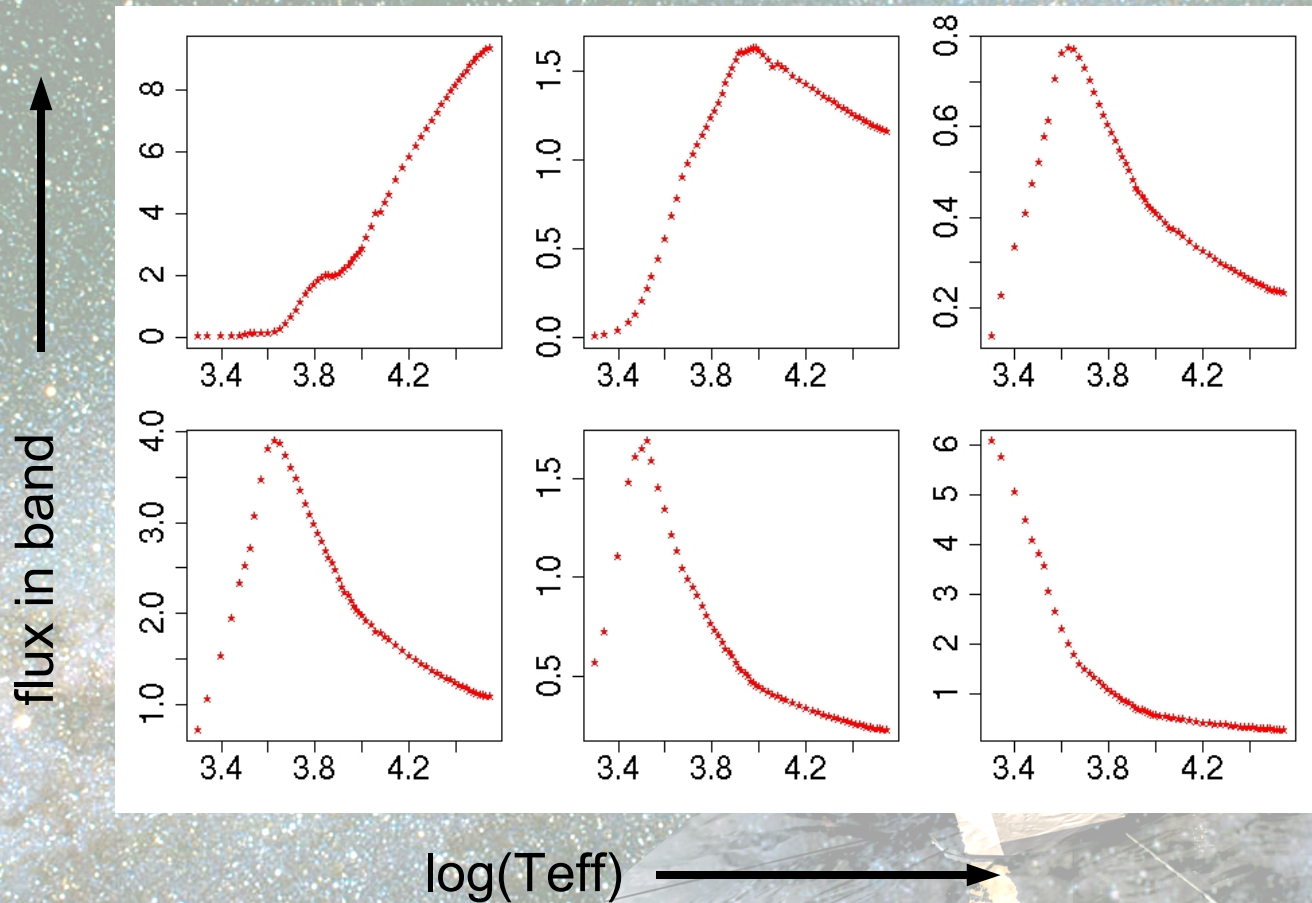
$$[\text{Fe}/\text{H}] = 0$$

$$\log g = \{-0.5, 5.5\}$$

$$T_{\text{eff}} = \{2000, 29000\}$$



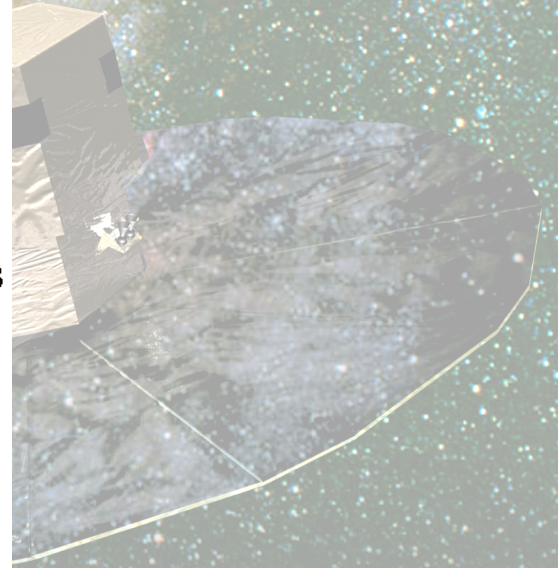
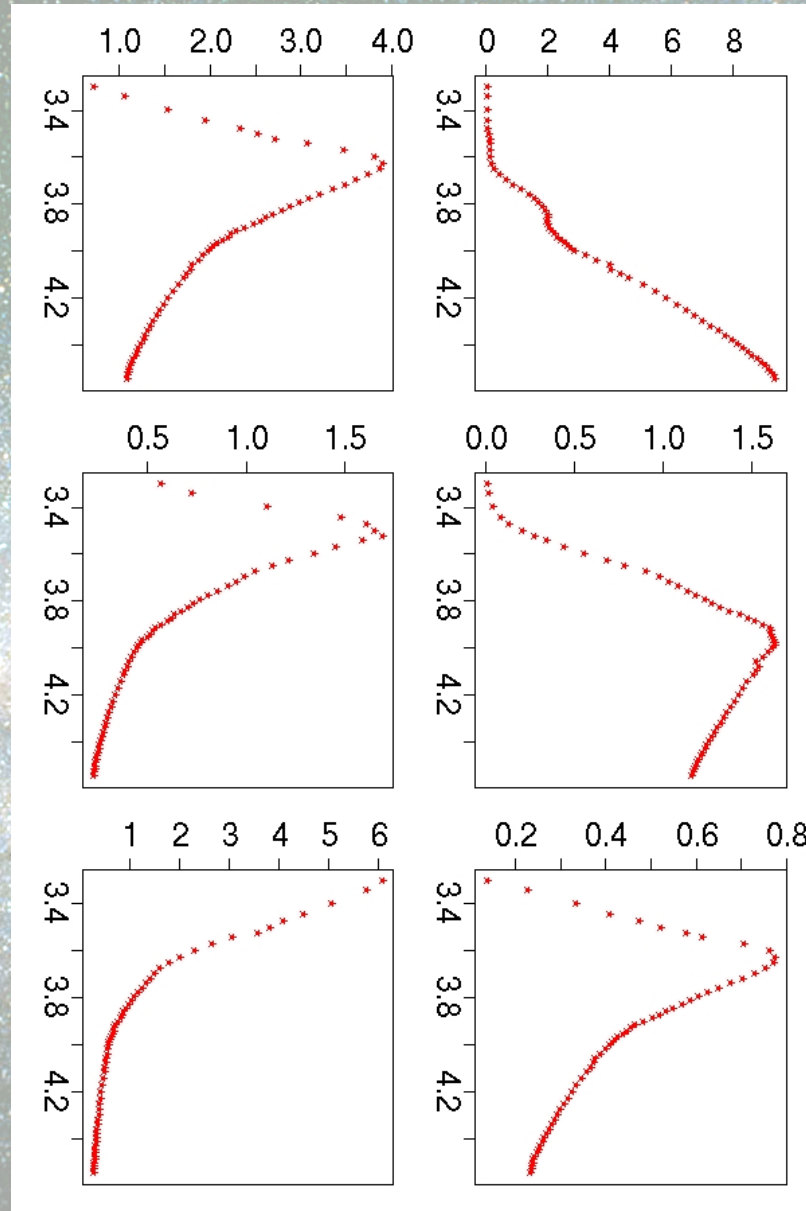
An inverse problem



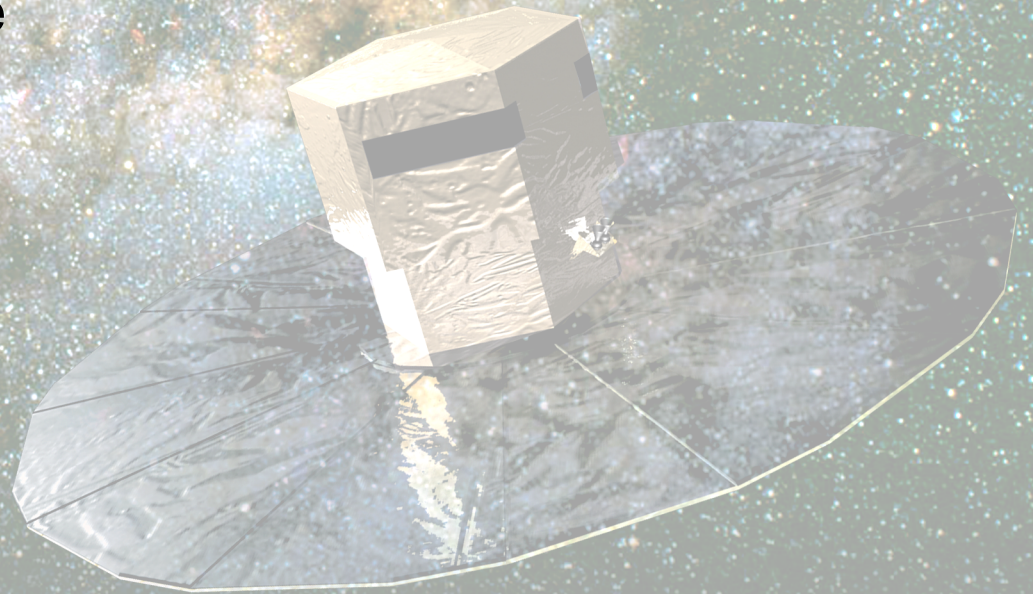
An inverse problem

flux in band \longrightarrow

$\log(T_{\text{eff}}) \longrightarrow$



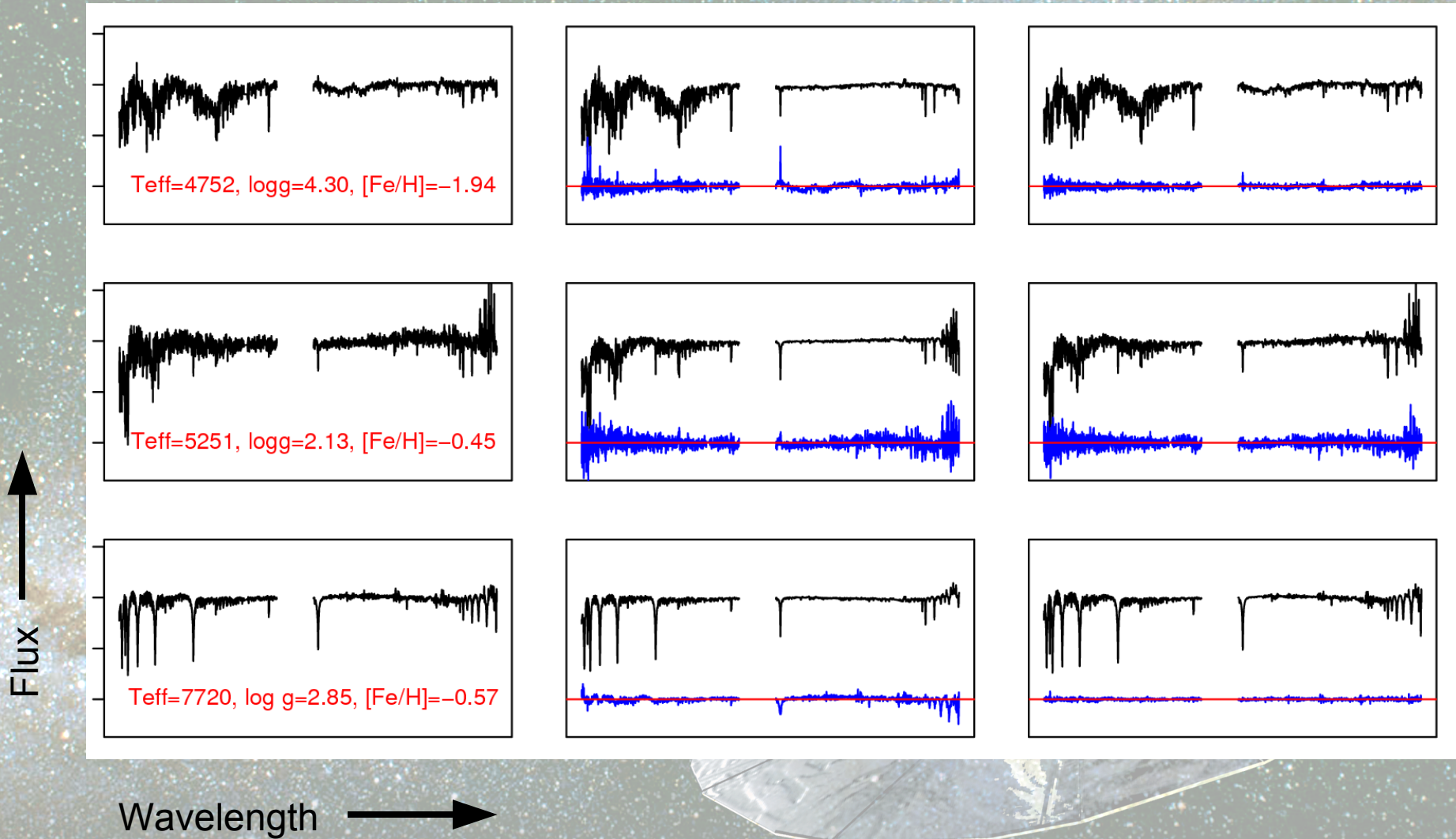
- ▶ train regression model using simulated spectra (true physical parameters are known)
- ▶ predict (unknown) parameters of real objects
- ▶ model: MLP neural network (statnet)
- ▶ large input space (thousands of correlated pixels)
 - dimension reduction via PCA
 - also removes some noise
 - can act as a junk filter

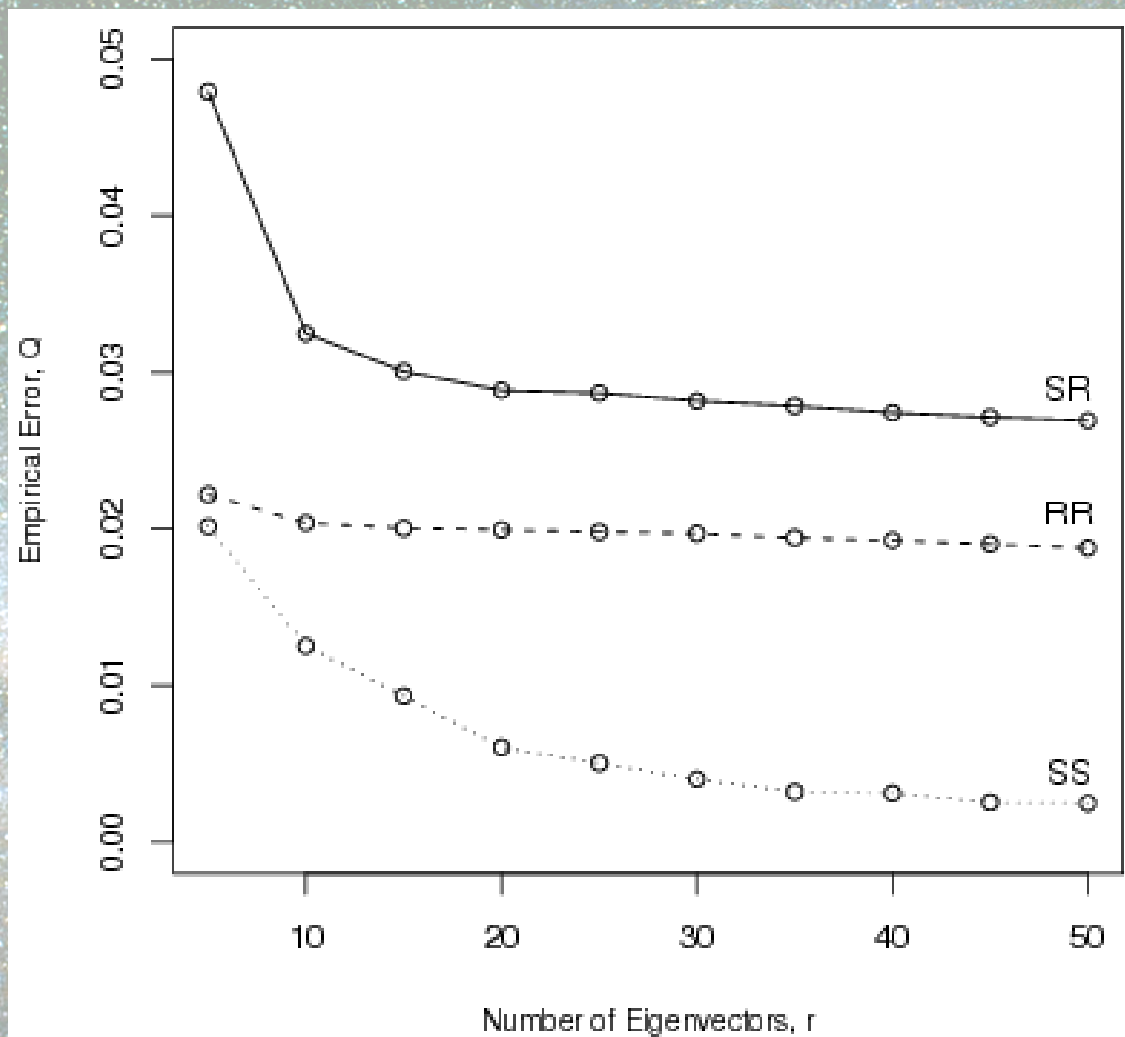


original spectra

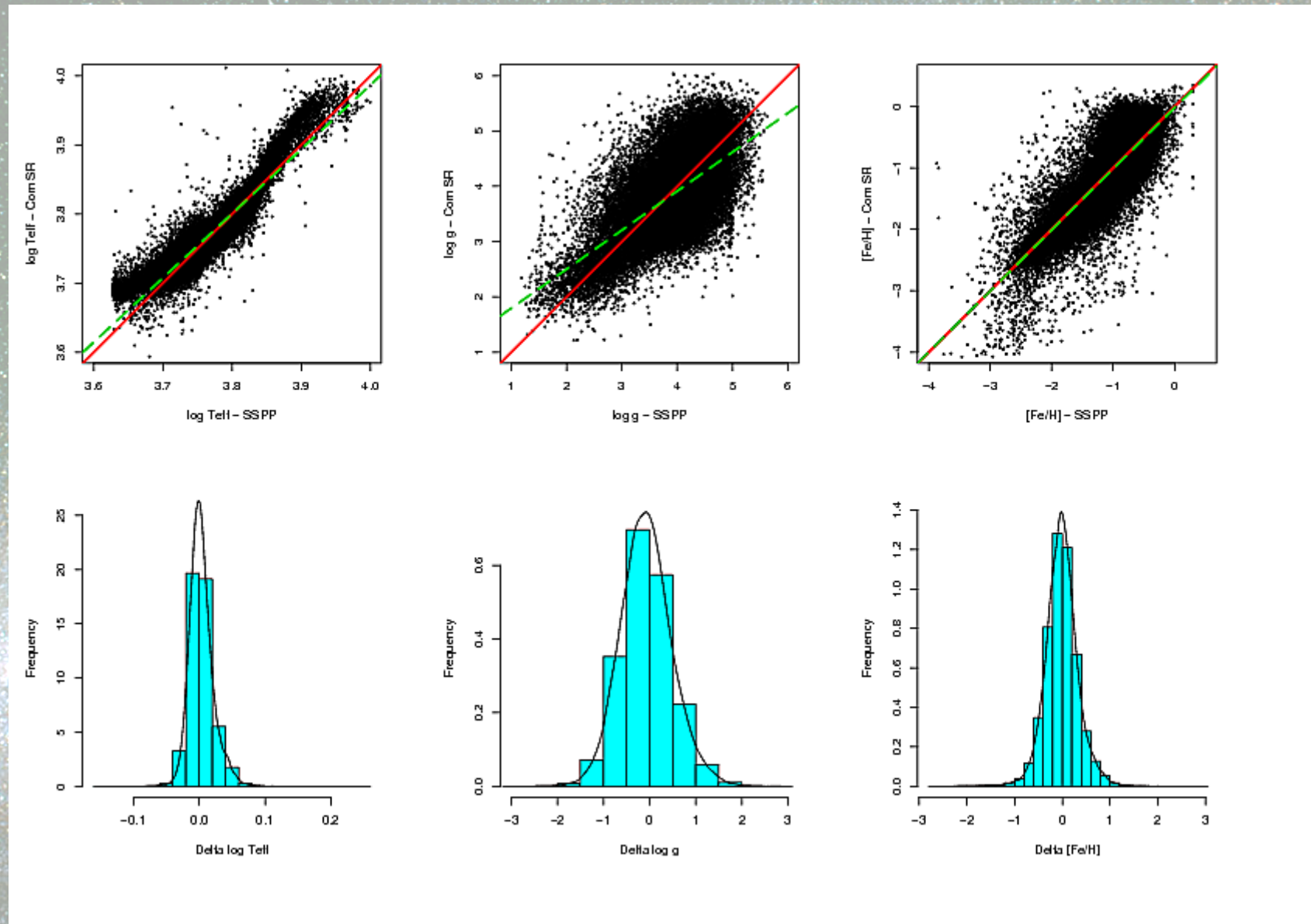
5+5 reconstruction

25+25 reconstruction





Results: comparison of parameter determinations with independent estimates



Physical parameter estimates are the basis for detailed physical studies

nature

Vol 450 | 13 December 2007 | doi:10.1038/nature06460

ARTICLES

Two stellar components in the halo of the Milky Way

Daniela Carollo^{1,2,3,5}, Timothy C. Beers^{2,3}, Young Sun Lee^{2,3}, Masashi Chiba⁴, John E. Norris⁵, Ronald Wilhelm⁶, Thirupathi Sivarani^{2,3}, Brian Marsteller^{2,3}, Jeffrey A. Munn⁷, Coryn A. L. Bailer-Jones⁸, Paola Re Fiorentin^{8,9} & Donald G. York^{10,11}

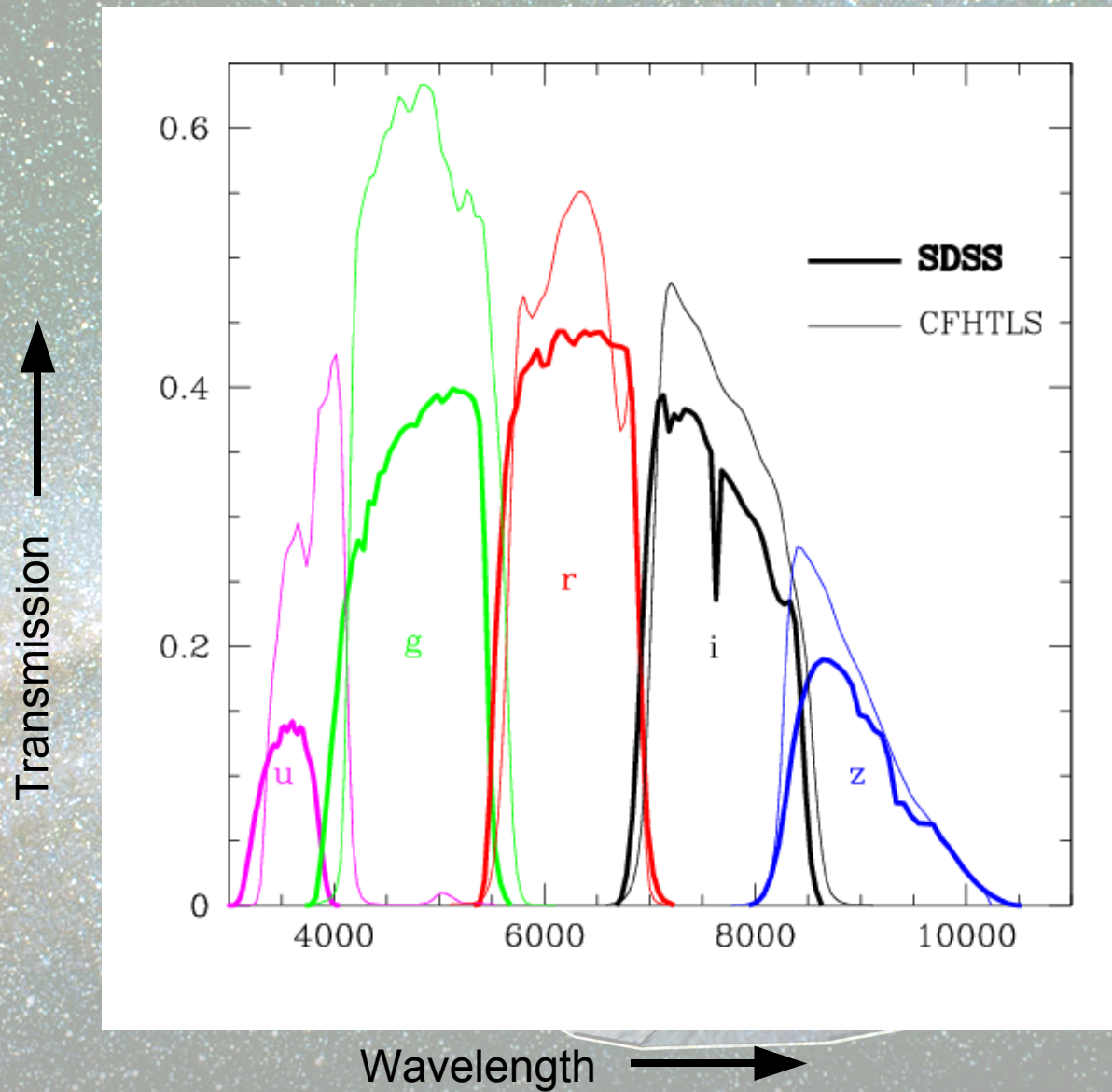
The halo of the Milky Way provides unique elemental abundance and kinematic information on the first objects to form in the Universe, and this information can be used to tightly constrain models of galaxy formation and evolution. Although the halo was once considered a single component, evidence for its dichotomy has slowly emerged in recent years from inspection of small samples of halo objects. Here we show that the halo is indeed clearly divisible into two broadly overlapping structural components—an inner and an outer halo—that exhibit different spatial density profiles, stellar orbits and stellar metallicities (abundances of elements heavier than helium). The inner halo has a modest net prograde rotation, whereas the outer halo exhibits a net retrograde rotation and a peak metallicity one-third that of the inner halo. These properties indicate that the individual halo components probably formed in fundamentally different ways, through successive dissipational (inner) and dissipationless (outer) mergers and tidal disruption of proto-Galactic clumps.

Incorporating domain knowledge

- ♦ much redundant information in spectra
- ♦ can directly extract sensitivity of inputs (pixels) from simulated data (physical models)
 - soft dimension reduction
- ♦ use in various ways
 - data weighting (global)
 - local regression via local weighting (iterative) *[in progress...]*
- ♦ ideal case
 - design optimal filters to use in telescope in first place



Photometric filters



- ♦ algorithm
 - parametrize filter system (three per filter)
 - establish a figure-of-merit (FoM) of filter system performance
 - maximize FoM with respect to filter system parameters
- ♦ optimizer
 - cannot define derivatives
 - local minima guaranteed!
 - evolutionary algorithm (genetic algorithm)

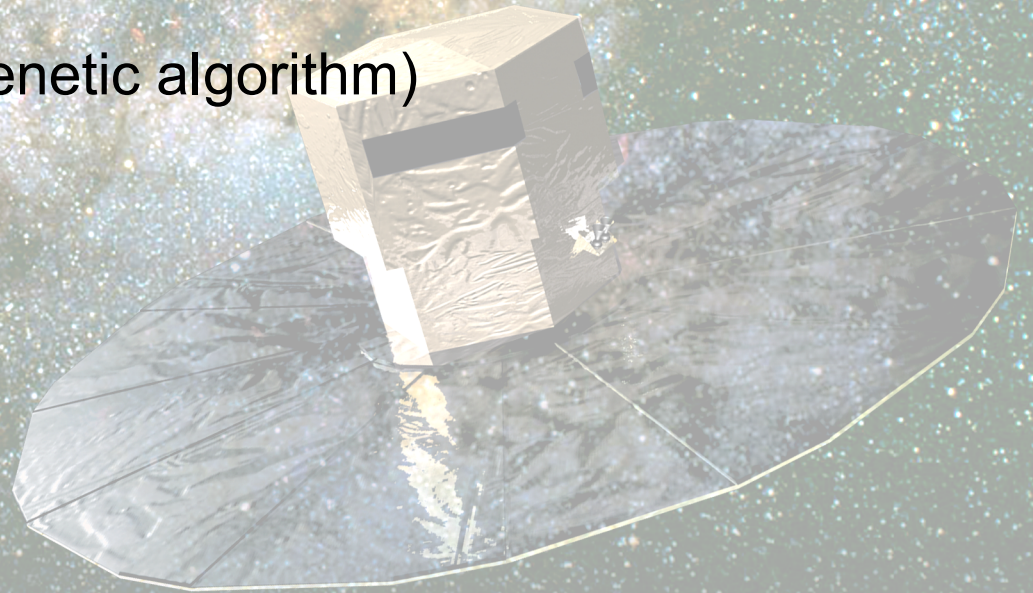
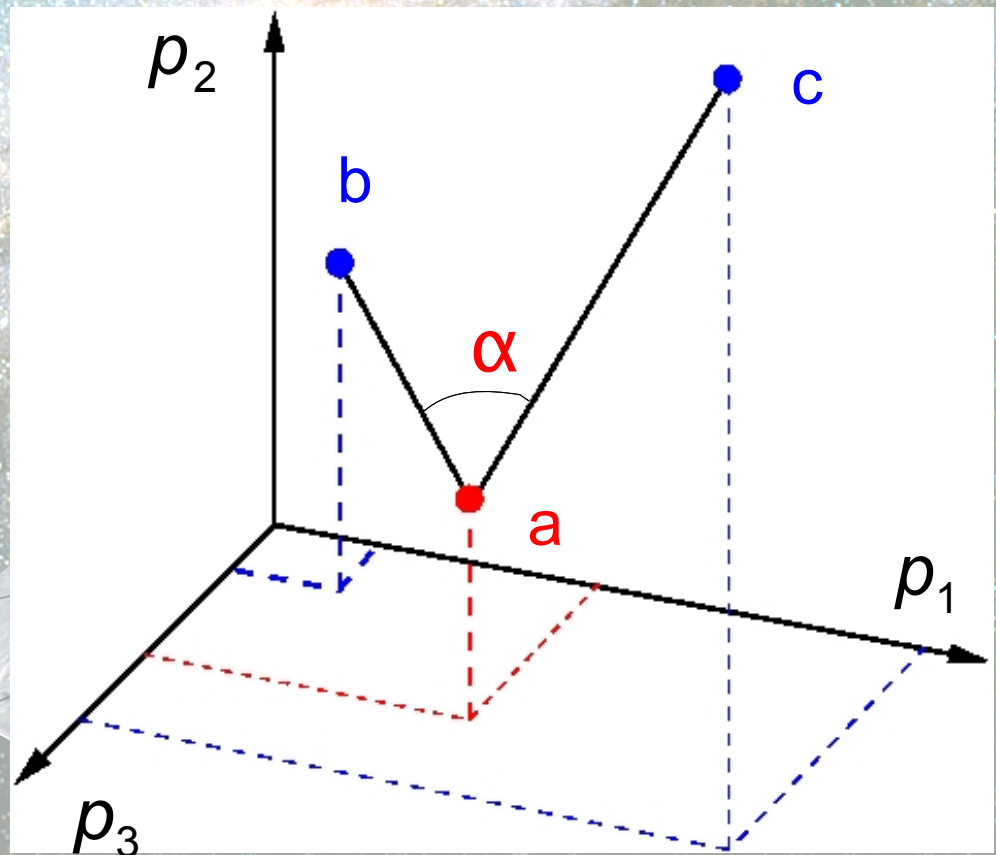
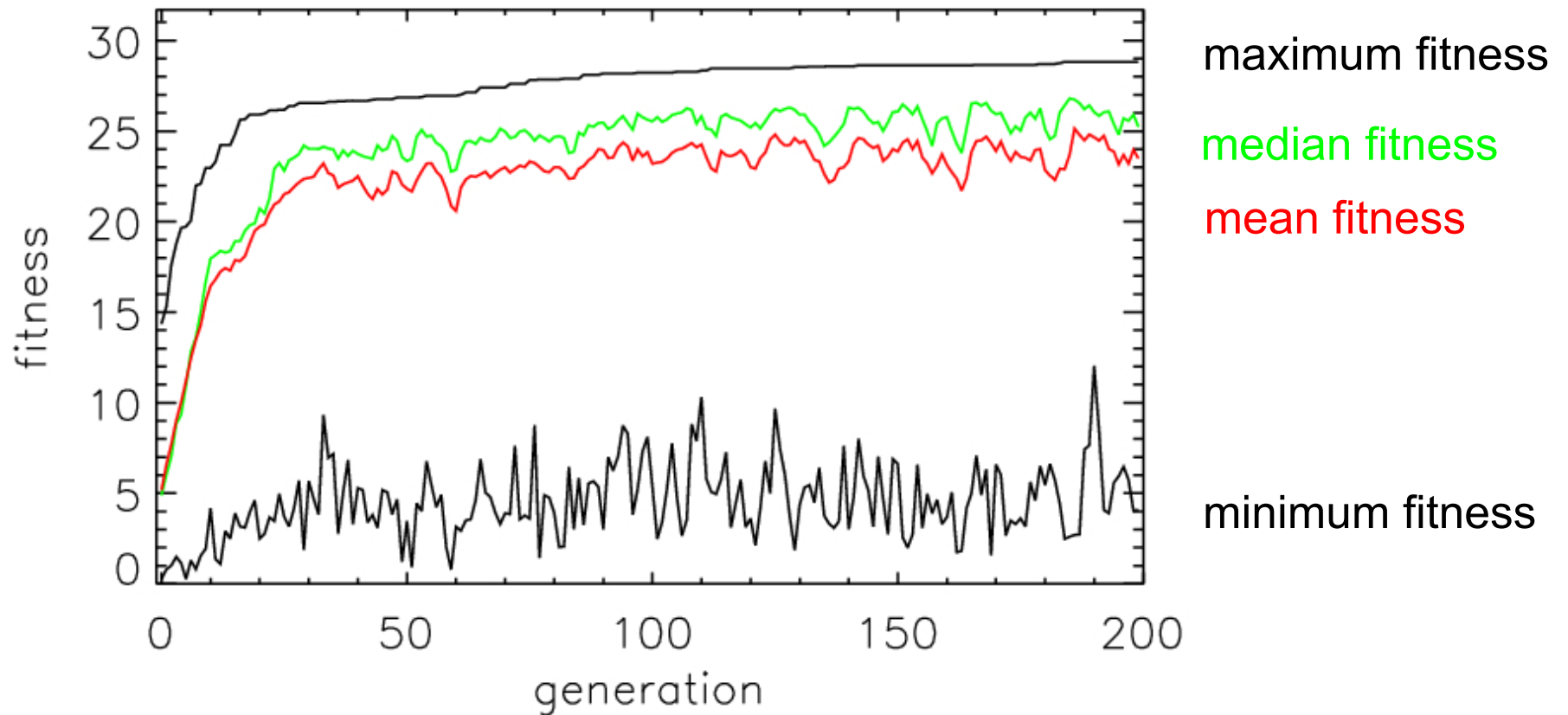


Figure of merit (fitness)

- space: flux in each filter of a filter system
- maximum fitness: local directions of variance of the different astrophysical parameters are orthogonal
- calculated from labelled data set

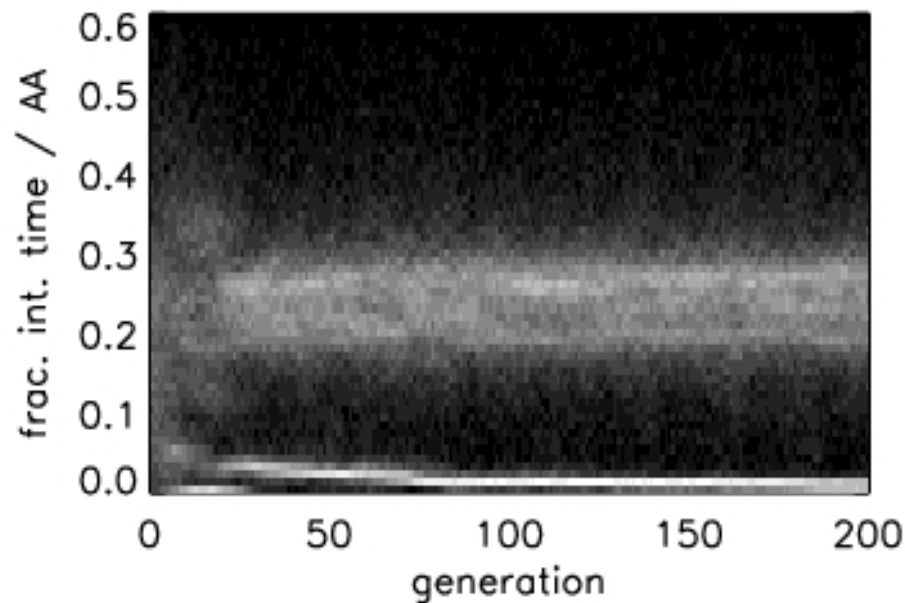
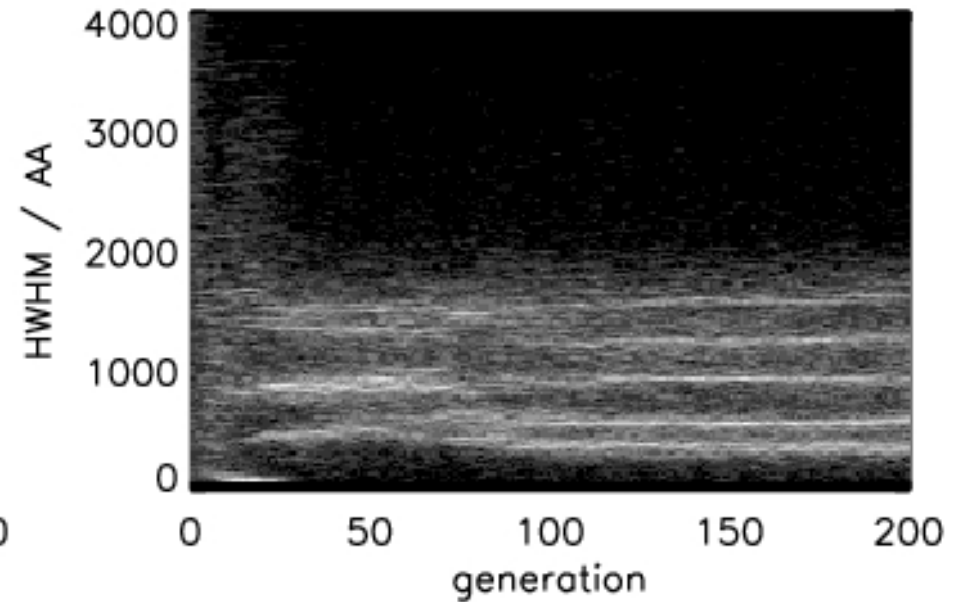
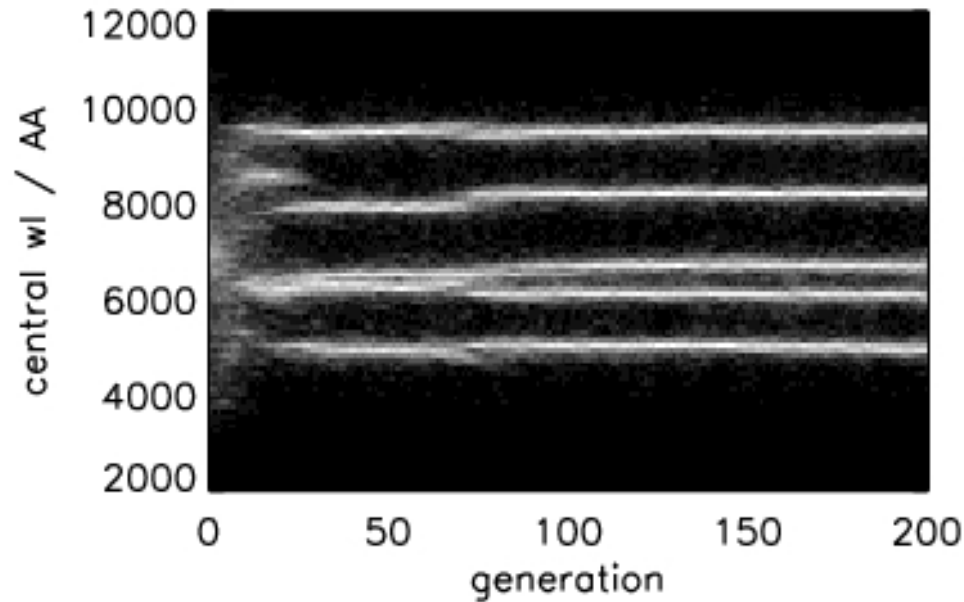


Fitness evolution



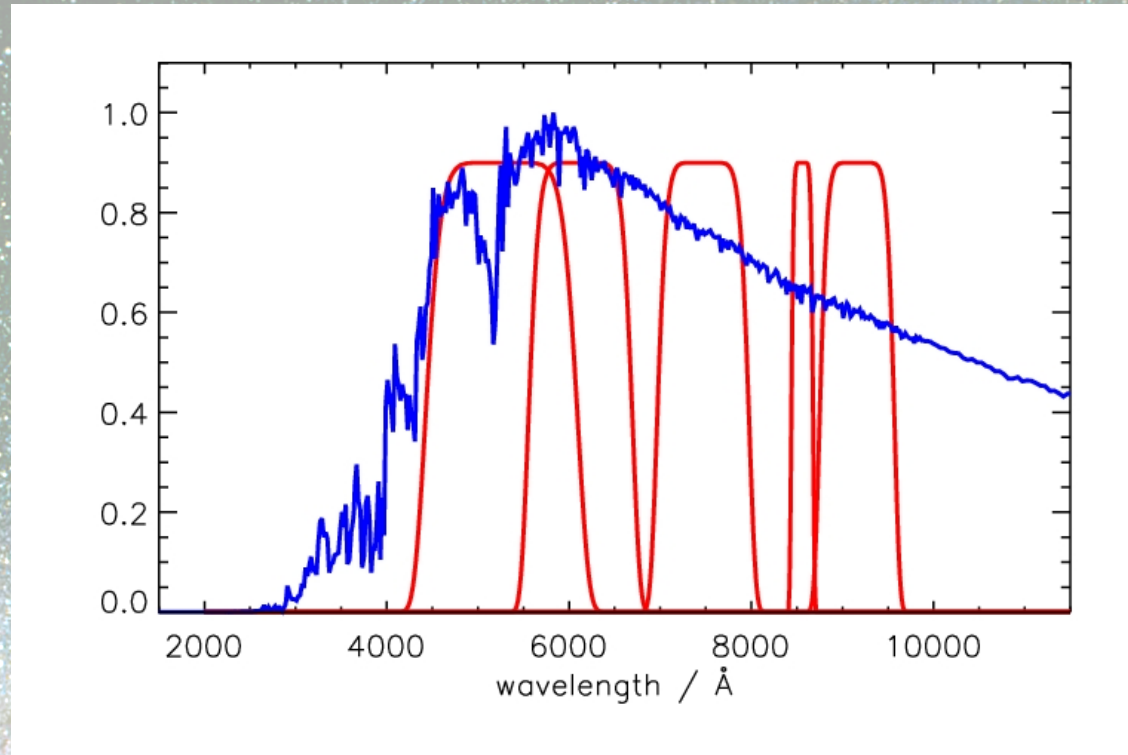
Bailer-Jones 2004

Filter system evolution



Evolution of all filter system parameters
(200*5 for each parameter type at each generation)

Discovered filter system



- ▶ unconventional: overlapping filters
- ▶ learned filter system competitive in parameter estimation work
- ▶ method could be extended to design “software filters” in algorithms (e.g. hierarchical classification system)

- ▶ astronomy driven by what we can learn from data (surveys)
- ▶ extract optimal information from spectra
 - classification (star, quasar etc.)
 - estimate physical parameters
- ▶ use of machine learning methods
 - probabilistic system for classification (SVM)
 - issues of inverse problem and “weak” parameters
- ▶ exploit domain knowledge
 - post hoc adjustment based on population fractions (priors)
 - deriving sensitivities from simulated data
 - EA-based heuristic filter design
- ▶ future work
 - nonlinear dimensionality reduction
 - degenerate solutions and error estimation