

Sternentstehung - Star Formation

Winter term 2022/2023

Henrik Beuther, Thomas Henning & Jonathan Henshaw

<i>18.10 Today: Introduction & Overview</i>	<i>(Beuther)</i>
<i>25.10 Physical processes I</i>	<i>(Beuther)</i>
08.11 Physical processes II	(Beuther)
15.11 Molecular clouds as birth places of stars	(Henshaw)
22.11 Molecular clouds (cont.), Jeans Analysis	(Henshaw)
29.11 Collapse models I	(Beuther)
06.12 Collapse models II	(Henning)
13.12 Protostellar evolution	(Beuther)
20.12 Pre-main sequence evolution & outflows/jets	(Beuther)
10.01 Accretion disks I	(Henning)
17.01 Accretion disks II	(Henning)
24.01 High-mass star formation, clusters and the IMF	(Henshaw)
31.01 Extragalactic star formation	(Henning)
07.02 Planetarium@HdA, outlook, questions	
13.02 Examination week, no star formation lecture	

Book: Stahler & Palla: The Formation of Stars, Wileys

More Information and the current lecture files: http://www.mpia.de/homes/beuther/lecture_ws2223.html
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Last Week

- Main tools: Spectral line emission, and thermal emission and extinction from dust.

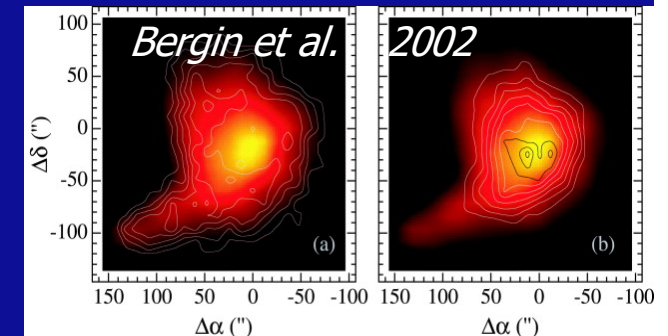
- Molecules interesting for themselves and chemistry.



- However, also extremely useful to trace physical processes.

- Molecules deplete on grains at low temperatures.

- Discussed main cooling and heating processes.



- Discussed basic line radiation transfer and column density determination.

Topics today

- Line profiles and a few applications for line emission
- Magnetic field measurements (Zeeman and dust)
- Maser emission
- Dust properties
- Physical distributions (Maxwell, Planck, Boltzmann, Saha)

Line broadening

- Natural line broadening: Disturbance of molecule by zero-point vibrations of electromagnetic field

$$d\nu = 32\pi^3\nu^3 \mu^2 / (3hc^3) \quad (\mu: \text{Dipole moment})$$

For CO(1-0) $\rightarrow d\nu \sim 3.5 \times 10^{-8}$ Hz or $d\nu \sim 9 \times 10^{-14}$ km/s \rightarrow Negligible!

- Pressure broadening: Arises from collisions between molecules.
Quantum-mechanical problem of intermolecular forces.
 \rightarrow At densities of star-forming regions negligible.

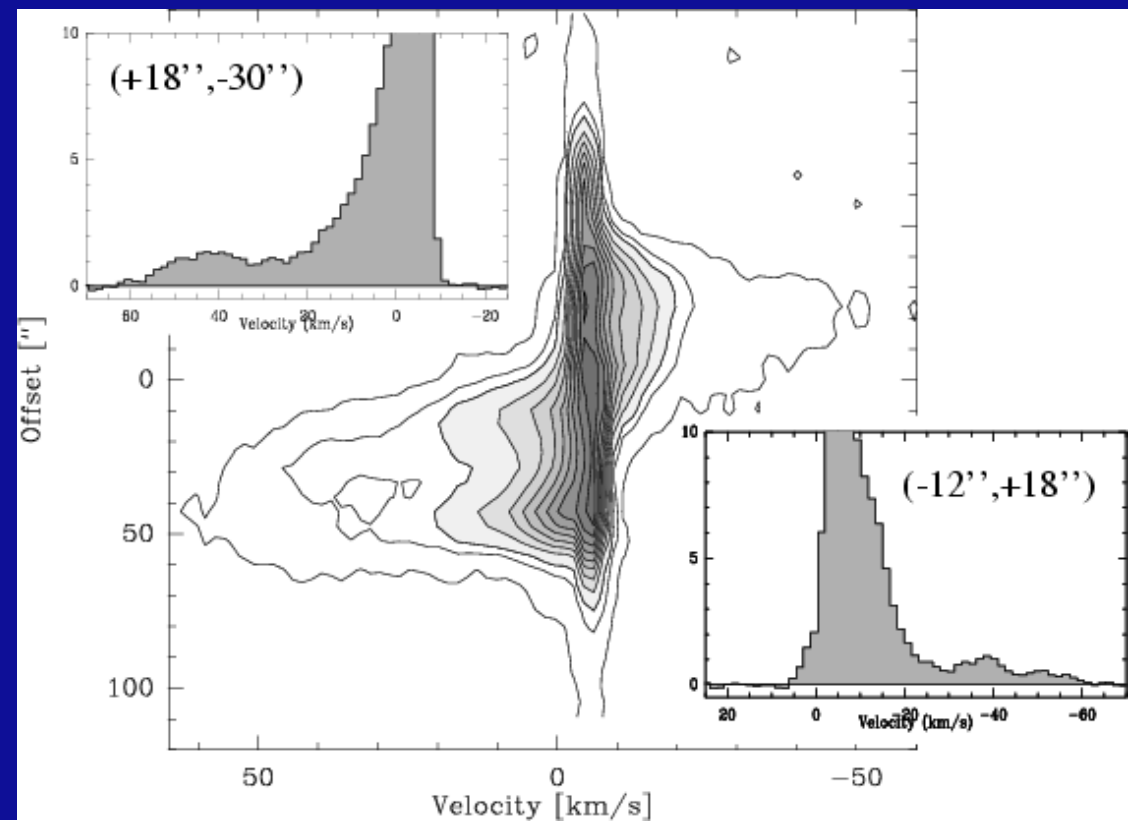
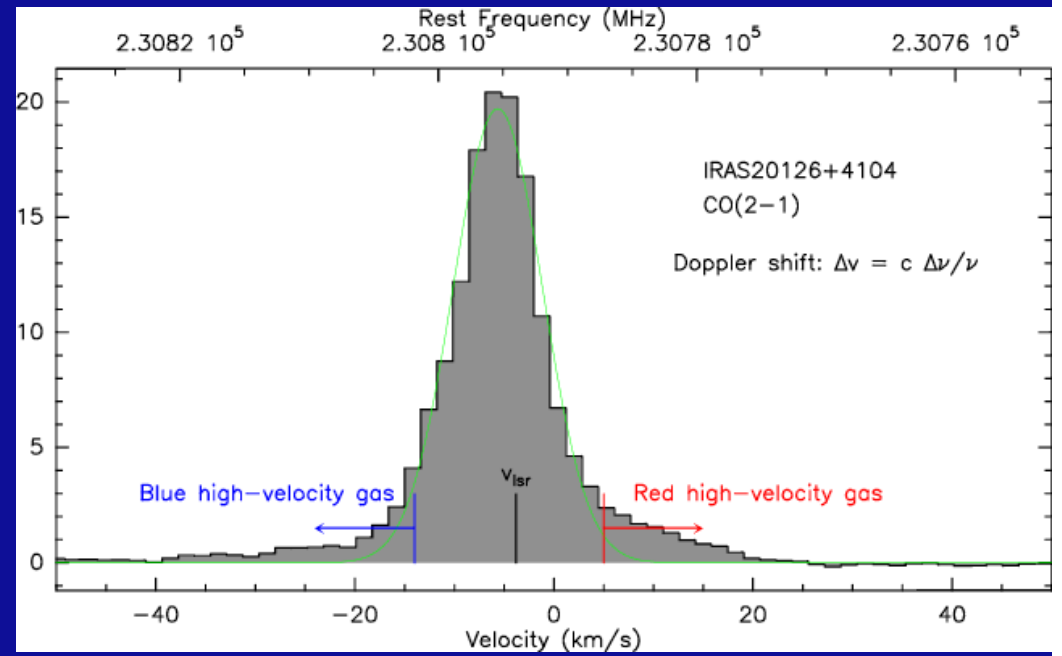
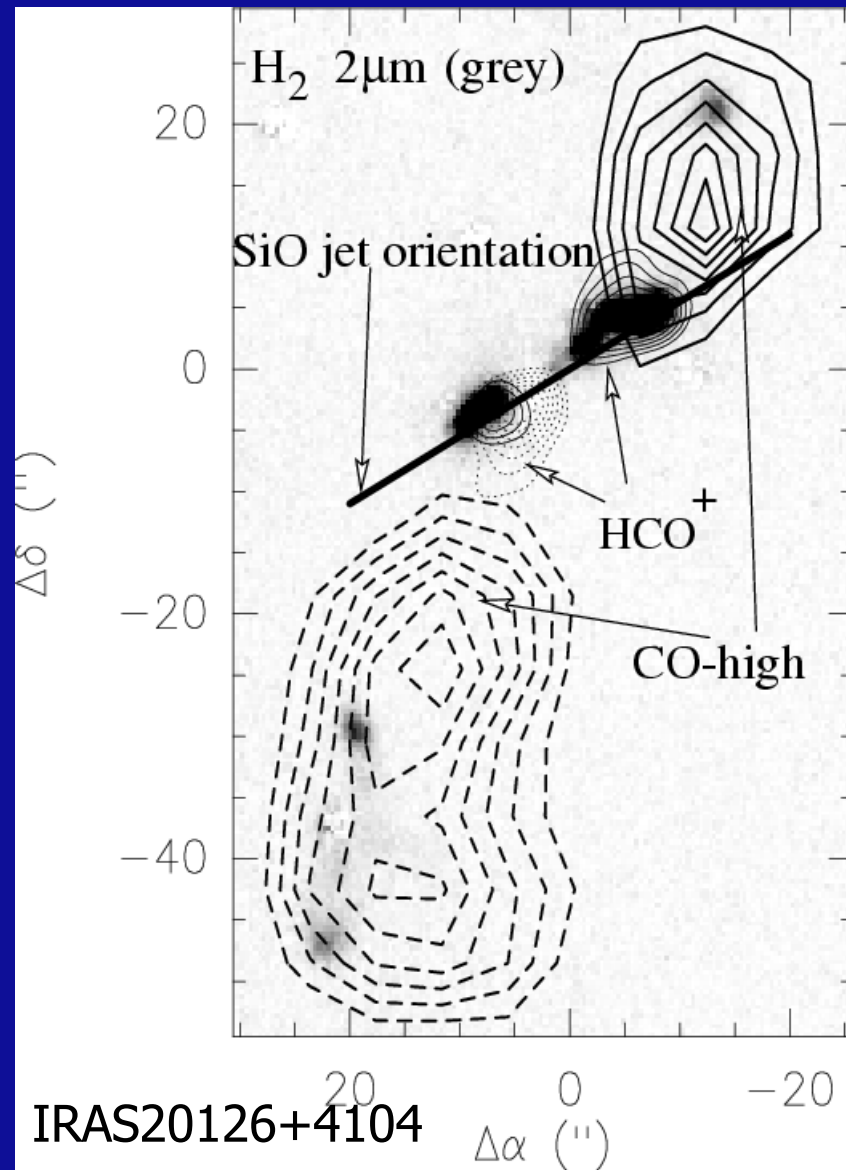
- Thermal line broadening: Thermal motions of gas cause doppler broadening:

$$d\nu = \sqrt{(8 \ln 2) kT / m_{\text{mol}}}$$

$$\rightarrow d\nu(\text{NH}_3 @ 30\text{K}) \sim 0.28 \text{ km/s}$$

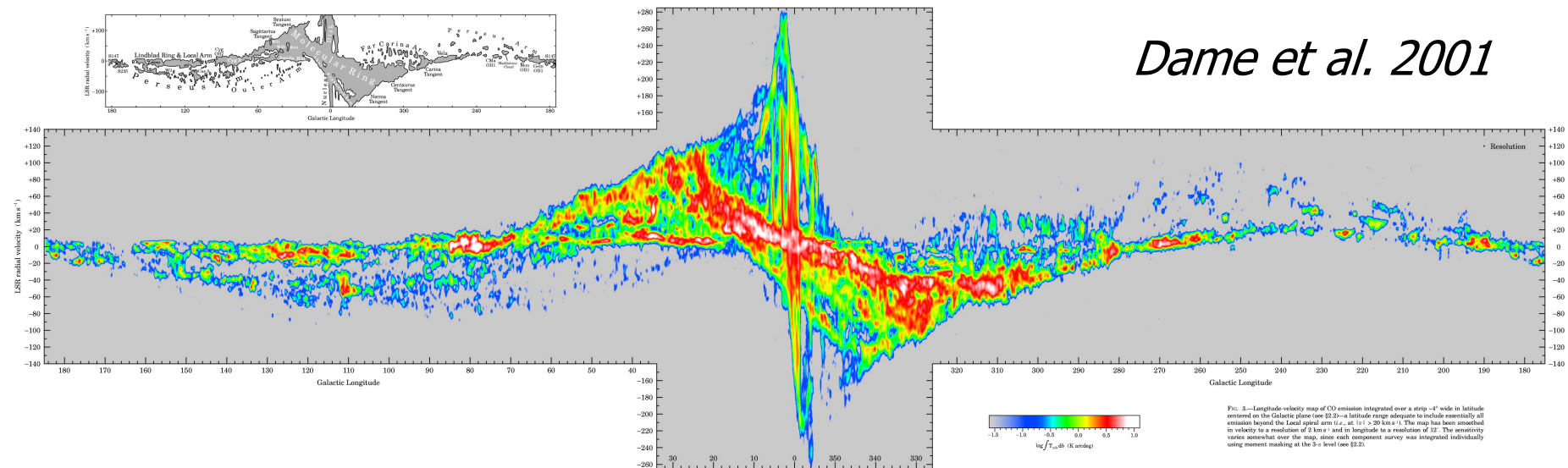
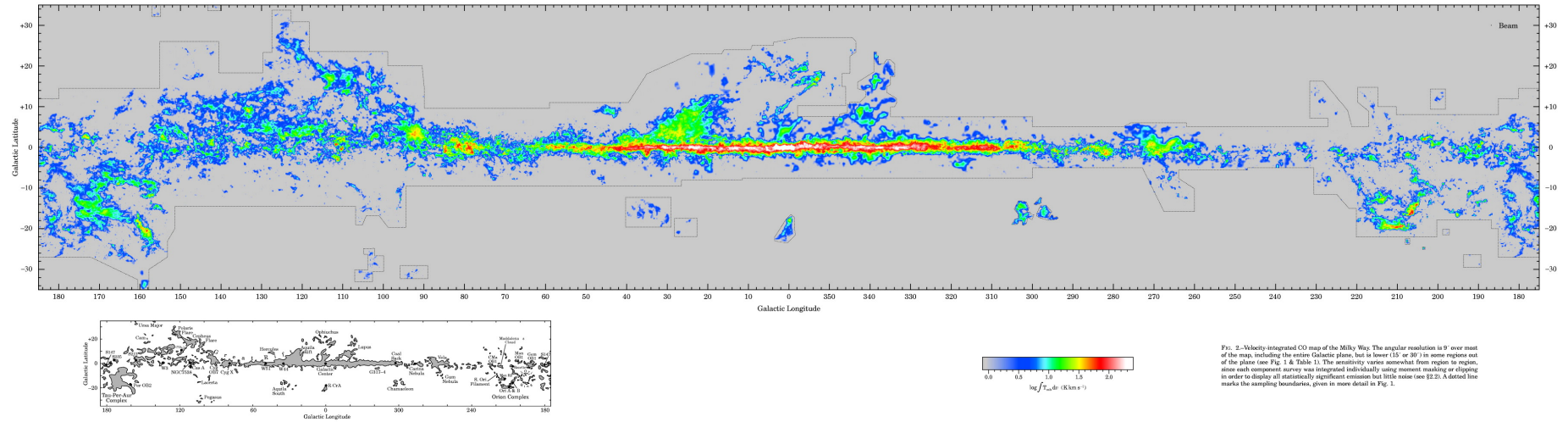
\rightarrow Other physical effects: Line broadening due to outflow motions, rotation ...

Molecular outflows



Lebron et al. 2006

Molecular gas structure of the Galaxy based on CO observations

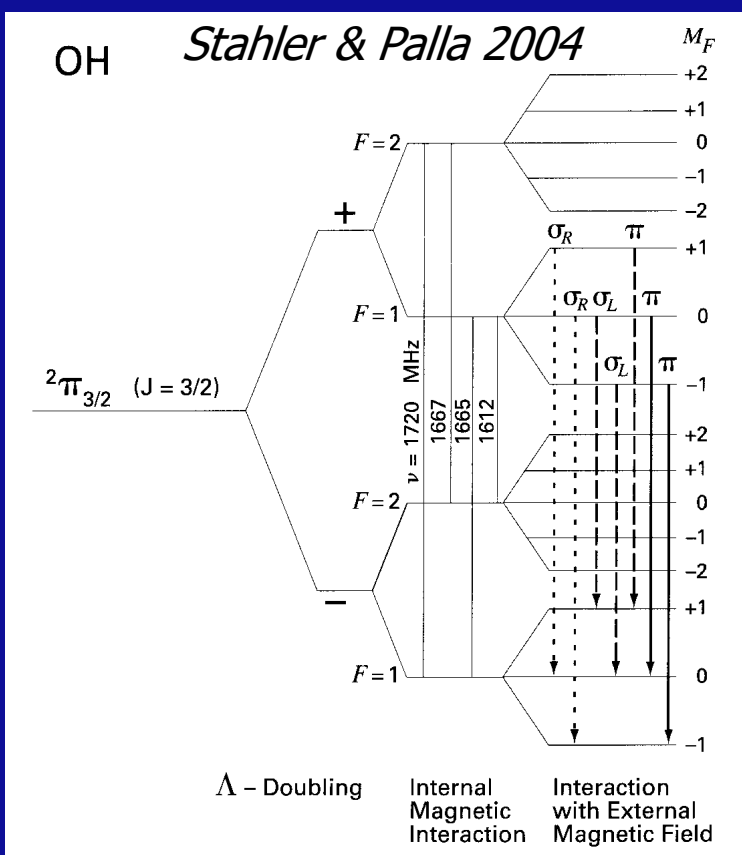
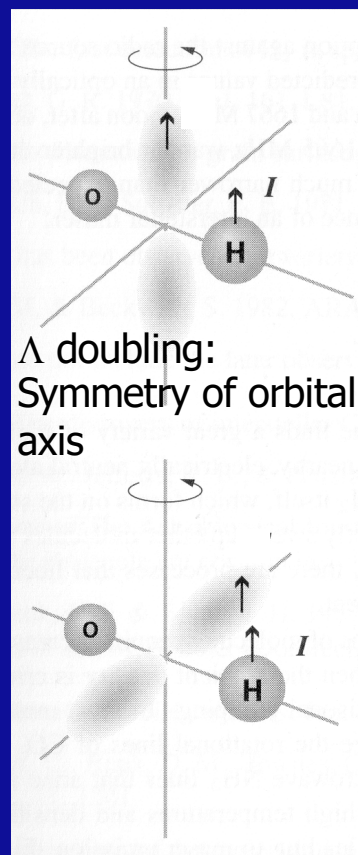
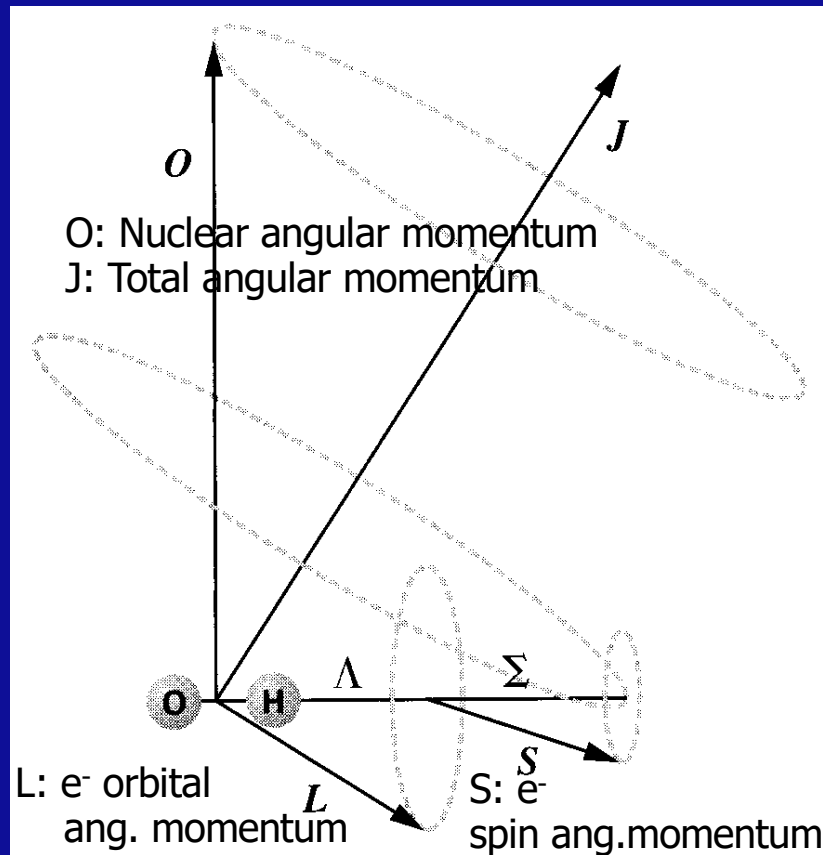


Dame et al. 2001

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- **Magnetic field measurements (Zeeman and dust)**
- Maser emission
- Dust properties
- Physical distributions (Maxwell, Planck, Boltzmann, Saha)

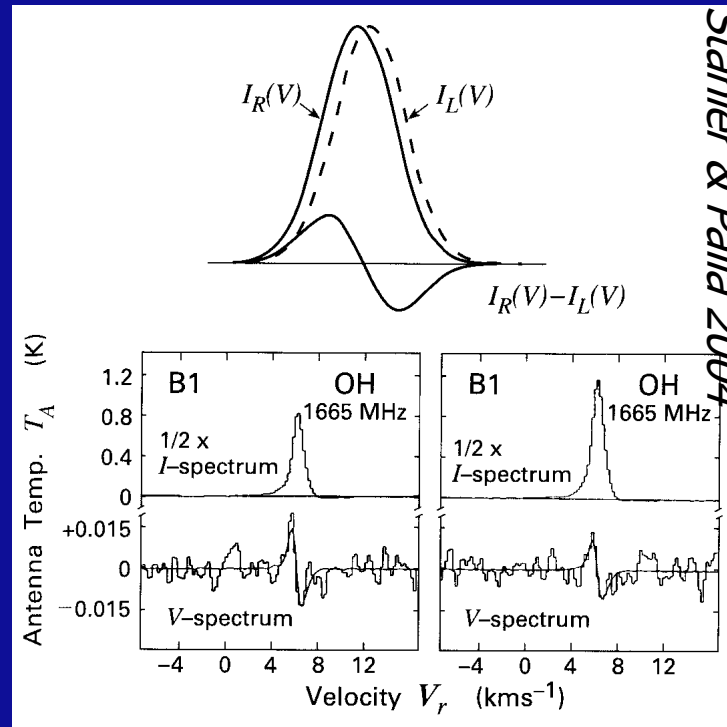
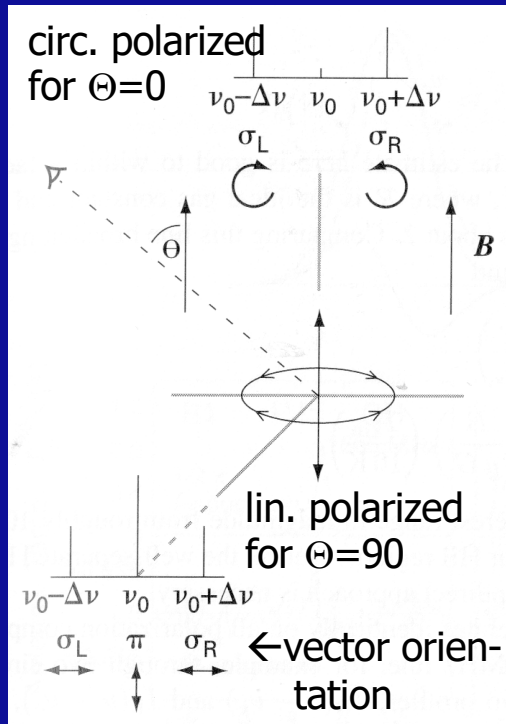
The Zeeman effect and magnetic fields I



- OH free radical with unpaired free e⁻ and hence non-zero electronic angular momentum. Highly reactive in lab, but can survive in space.
- Λ doubling \rightarrow symmetry difference of the e⁻ orbital to rotation axis \rightarrow energy splitting.
- Interaction between spins of e⁻ and H nucleus \rightarrow magn. hyperfine splitting.

External magnetic field \rightarrow produces Zeeman splitting.

The Zeeman effect and magnetic fields II

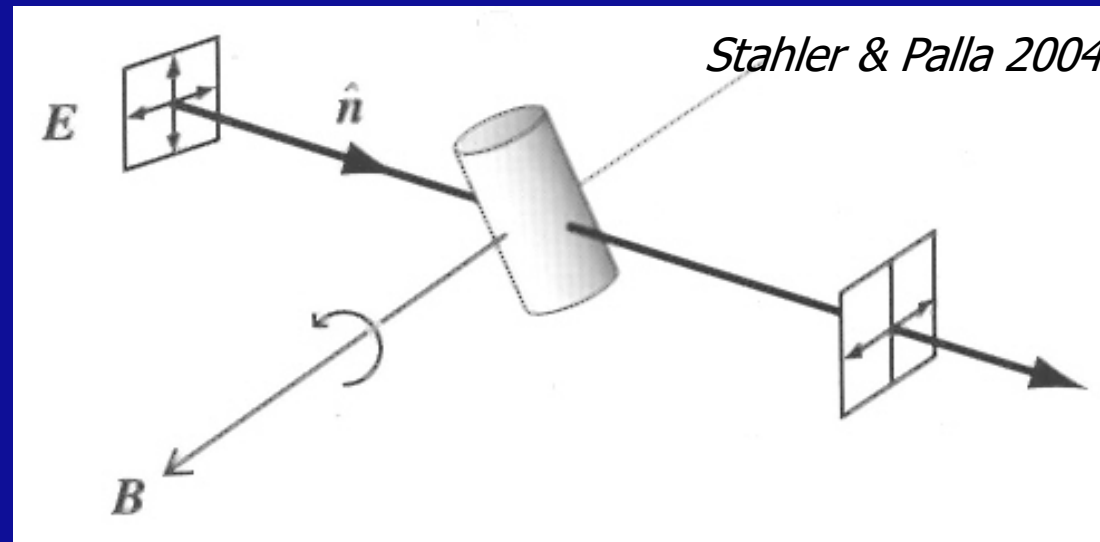


$\Delta\nu_{\text{mag}} \sim B$
usually of the order a few $10 \mu\text{G}$

← Subtraction of left- from right-handed circ. pol. results in Stokes-V spec.

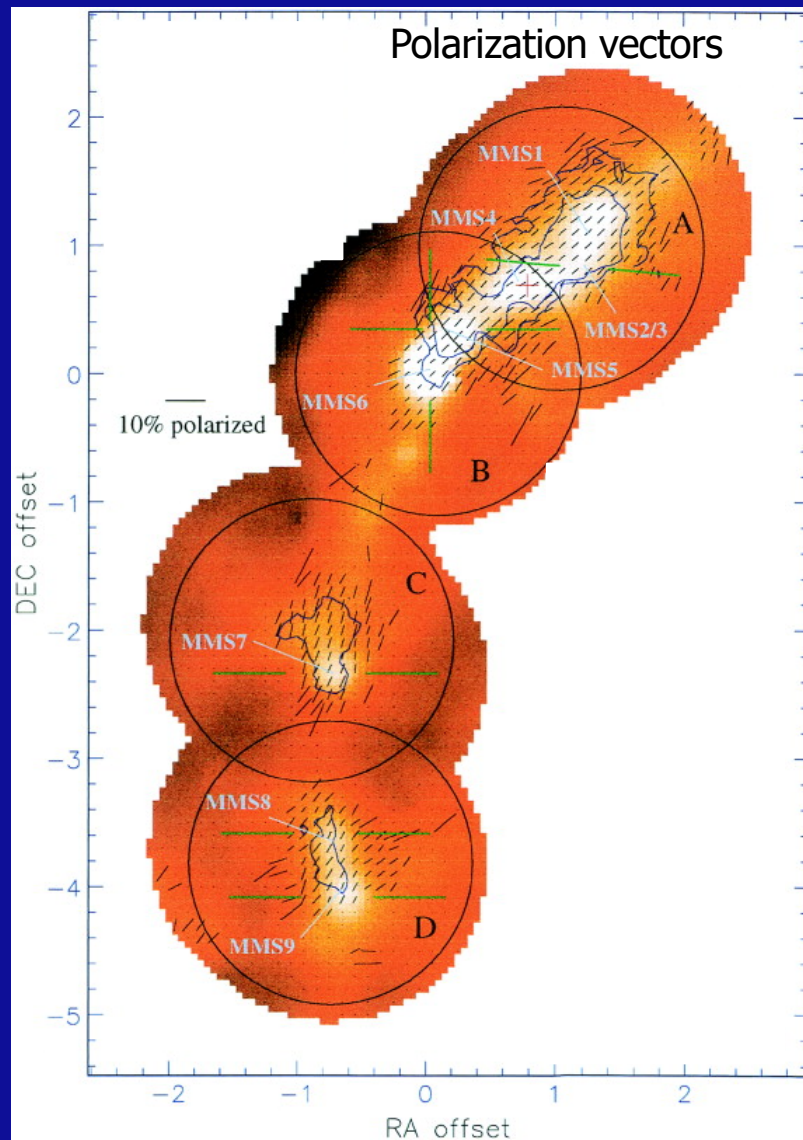
- Zeeman splitting of $\Delta\nu_{\text{mag}} = (b/2) B$ (b: constant, B: Magnetic field)
- Orientation between \mathbf{B} and line of sight causes different polarization properties
→ $\Theta=0$ (l.o.s) circular pol., $\Theta=90$ lin. pol., in reality elliptical polarization.
- Thermal line broadening complicates matter: $\Delta\nu_{\text{mag}}/\Delta\nu_{\text{therm}} \sim 10^{-3} B(\mu\text{G})$
 - One measures two polarizations differentially.
 - Only sensitive to the B component along the line of sight.

IR dust polarization & dichroic extinction



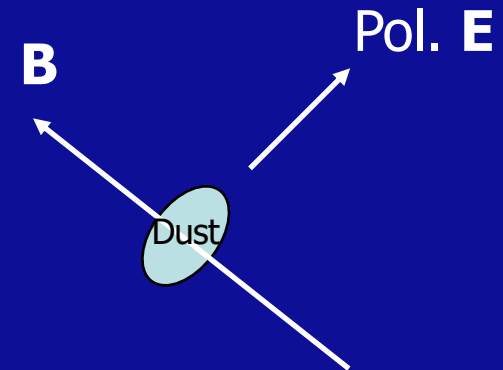
- Incident radiation unpolarized.
- Grains not spheres \rightarrow small electric charge and paramagnetic
 \rightarrow rotate about short axis, and magn. moment \mathbf{M} points along rotation axis.
- External \mathbf{B} field creates torque $\mathbf{D}=\mathbf{M}\times\mathbf{B}$ \rightarrow grain's short axis aligns with \mathbf{B} .
- Absorption best along major axis
 \rightarrow Polarization afterwards largely along axis of magn. field.

Dust polarization and magnetic fields



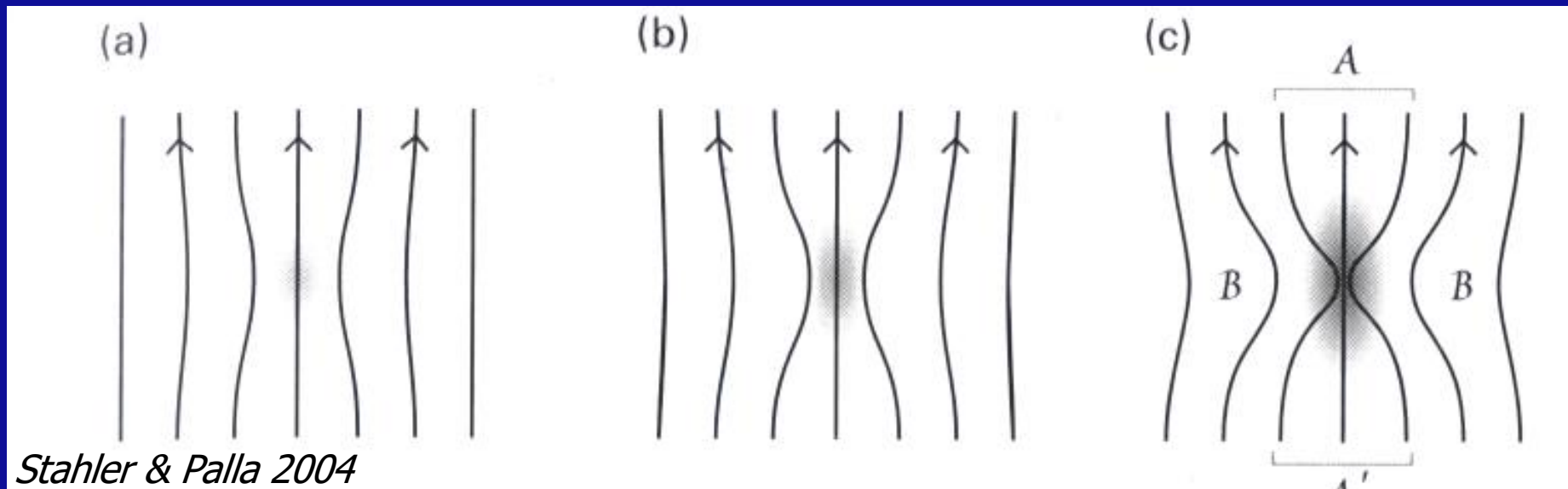
Polarized submm continuum emission

In contrast, thermal dust emission at (sub)mm wavelengths perpendicular to magnetic field!

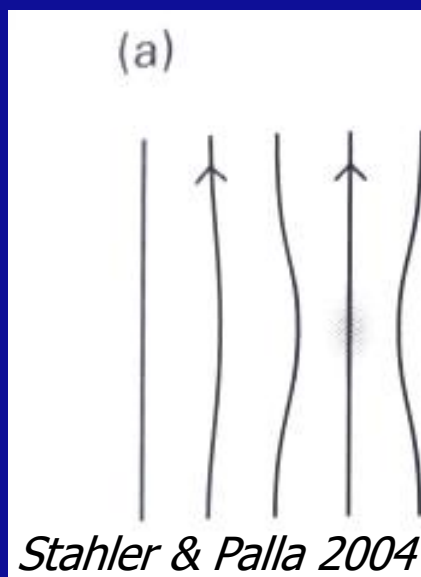


Molecular filaments can collapse along their magnetic field lines.

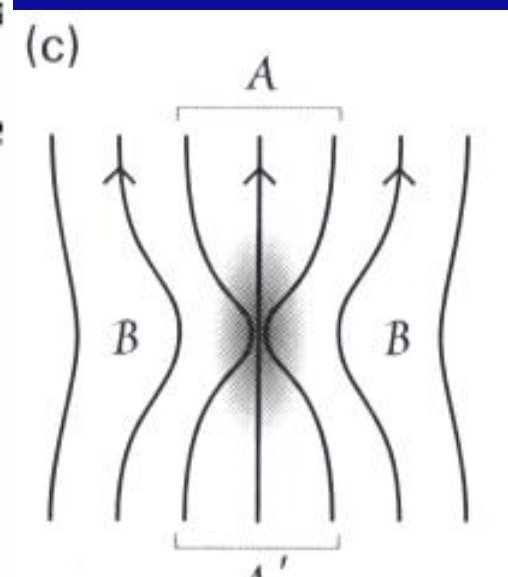
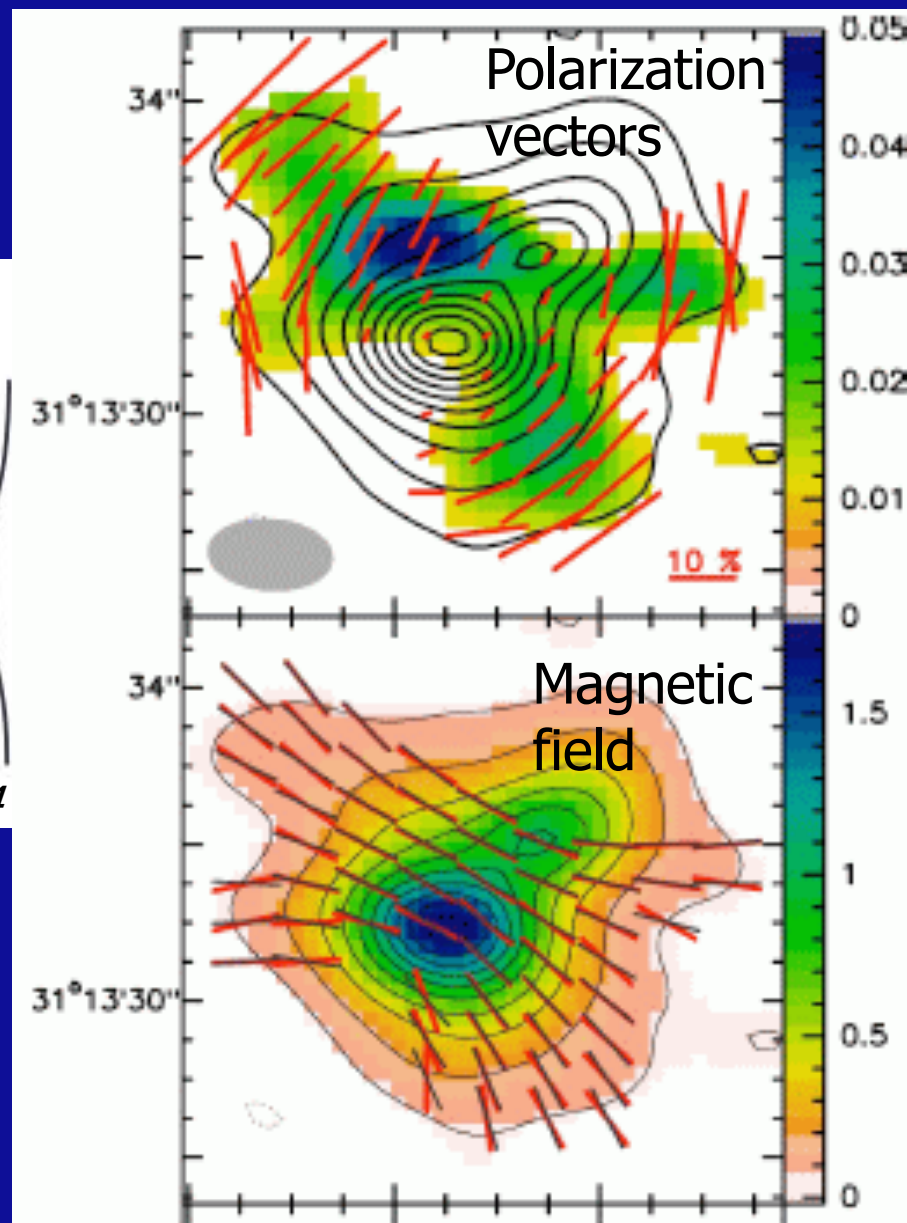
Ambipolar diffusion



Ambipolar diffusion



$B_{\text{pos}} \sim 5\text{mG}$

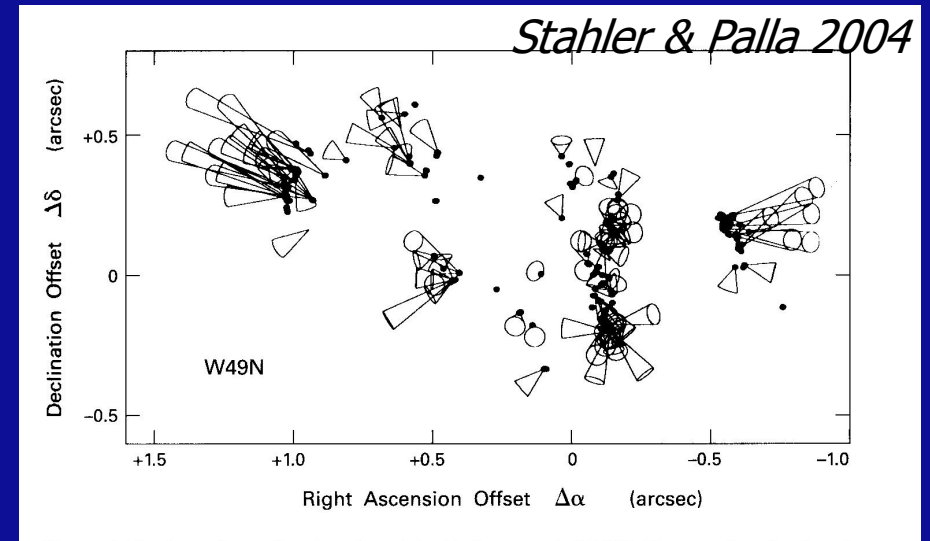
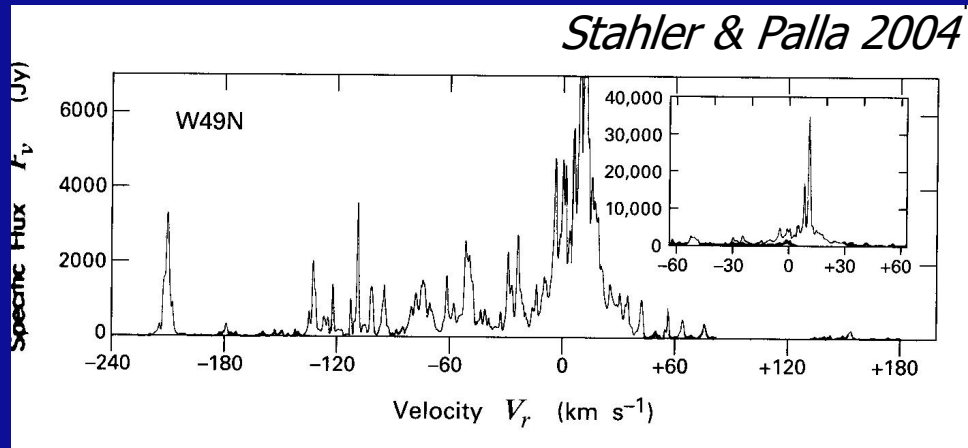


Girart et al. 2006

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- **Maser emission**
- Dust properties
- Physical distributions (Maxwell, Planck, Boltzmann, Saha)

Molecular Masers I

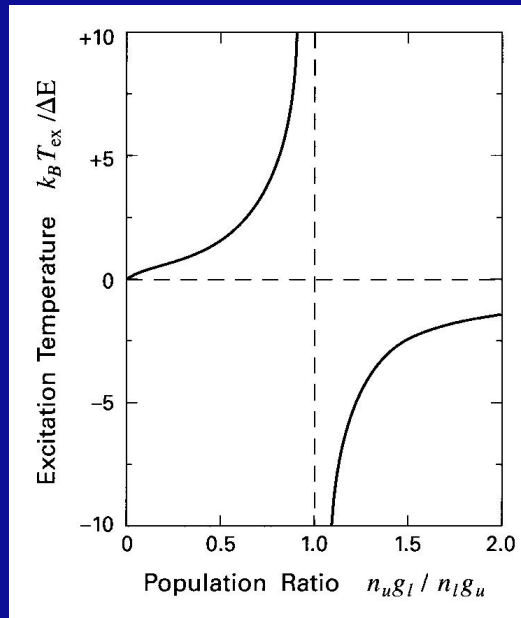


- Rayleigh-Jeans limit: $T = c^2/2k\nu^2I$ with $I=F/\Omega$ (Ω : solid angle).
- Small spot diameters (\sim some AU) \rightarrow T as high as 10^{15}K
 \rightarrow no thermal equilibrium and no Boltzmann distribution.
- Narrow line-width with potential broad velocity distribution (many components).
- They allow to study proper motions.

Molecular Masers II

- Excitation temperature for Boltzmann: $n_u/n_l = g_u/g_l \exp(-h\nu/kT_{\text{ex}})$.
- Maser activity requires population inversion: $n_u/g_u > n_l/g_l$.
 - Negative excitation temperatures
- In thermal conditions at a few 100K, for typical microwave lines $E_{\text{line}} = h\nu/k < T_{\text{kin}} \sim T_{\text{ex}} \rightarrow n_u/g_u \sim n_l/g_l$
 - Only a relatively small shift is required in get population inversion

Stahler & Palla 2004



$$T_{\text{ex}}/E_{\text{line}} = -1/\ln(n_u g_l / n_l g_u)$$

Rising T_{ex}

- Level populations approach each other
- Only "overcome the border".

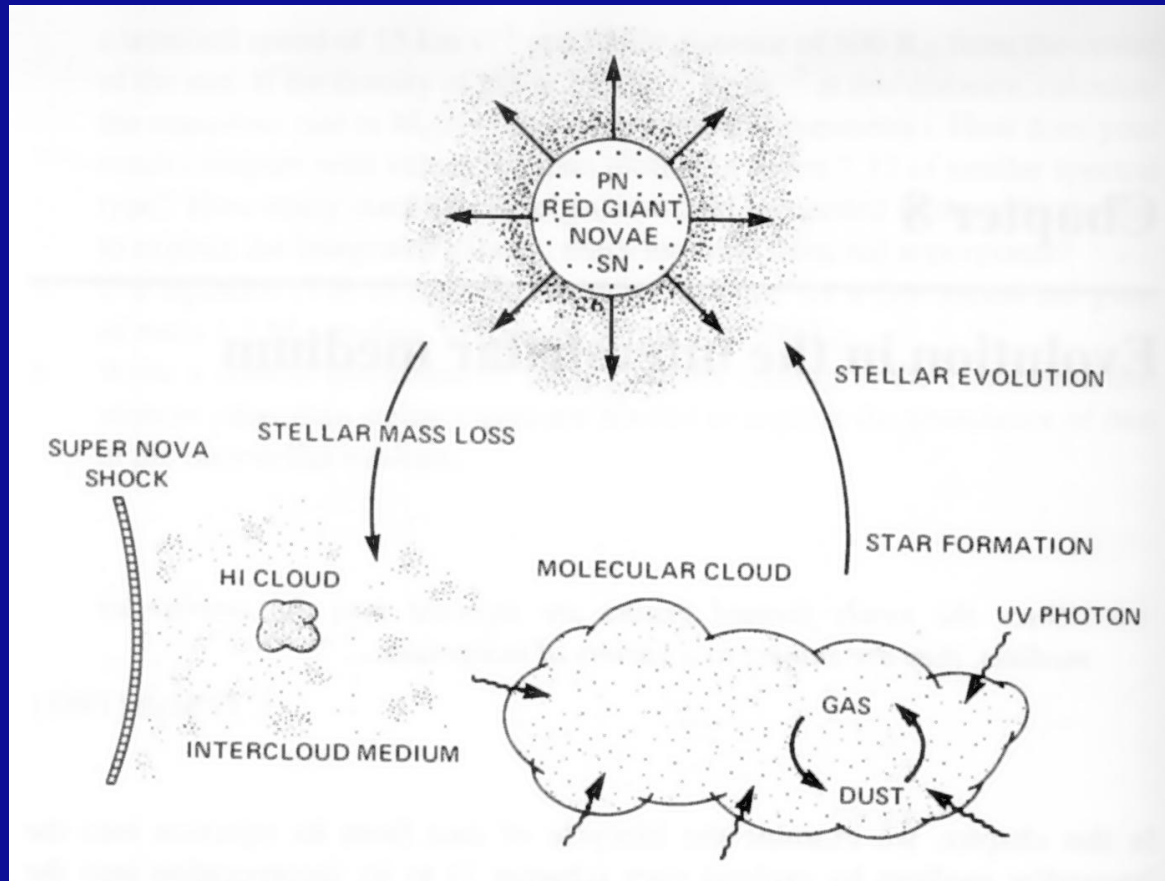
Pumping mechanisms, e.g.:

- Collisional pumping in shocks of protostellar jets for H₂O masers.
- Radiative pumping in shocks or from protostars (e.g., CH₃OH masers)
 - In both cases, very high densities and temperatures required.

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Dust within the big circle of matter



Dust composition:

Graphite/carbon	C
Silicon carbide	SiC
Enstatite	(Fe,Mg)SiO ₃
Olivine	(Fe,Mg) ₂ SiO ₄
Iron	Fe
Magnetite	Fe ₃ O ₄

Size distribution:

Between 0.005 and 1 μ m
 $n(a) \sim a^{-3.5}$ (a: size)
(Mathis, Rumpl, Nordsieck 1977)

Gas to dust mass ratio:

Canonical 1:100

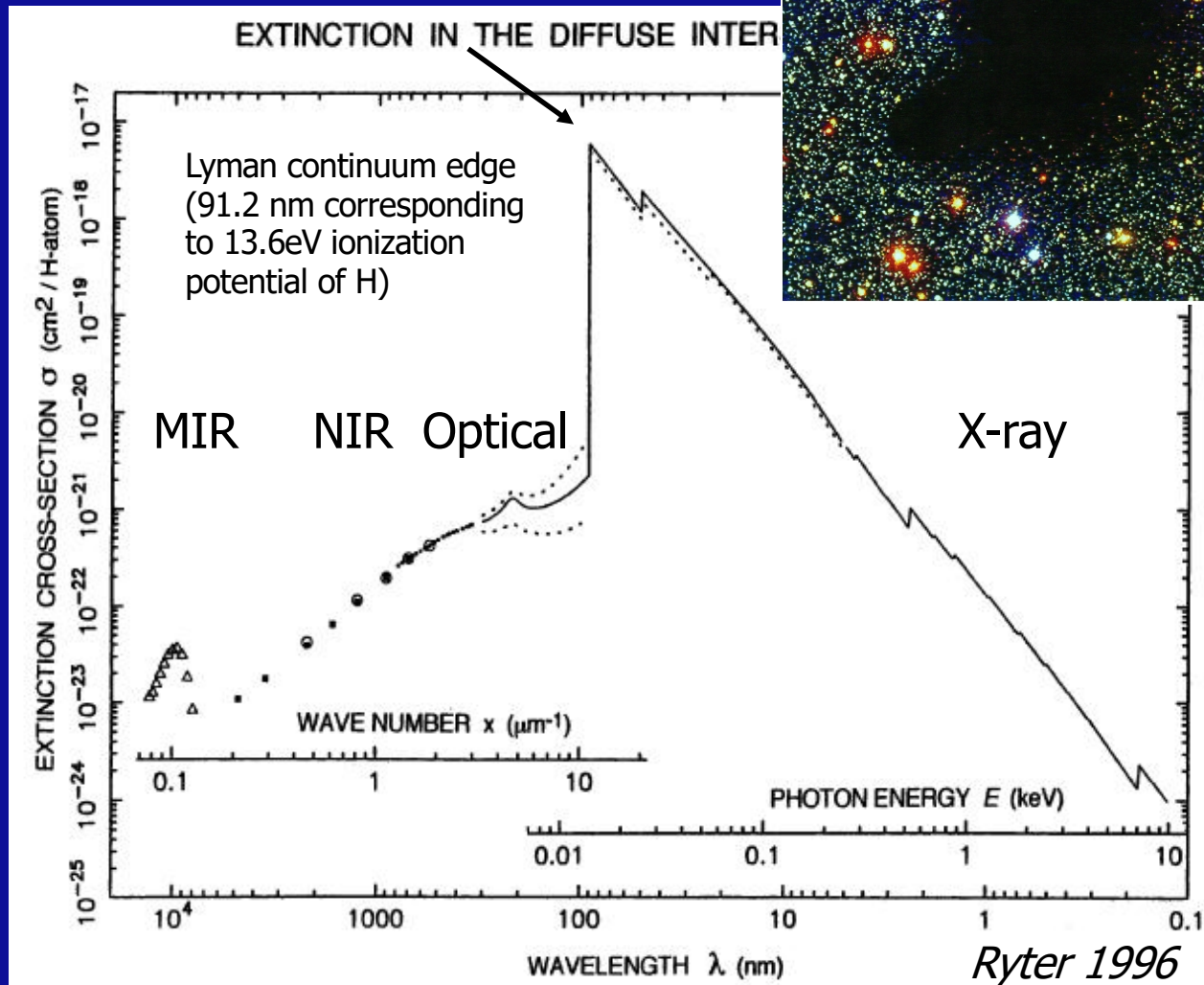
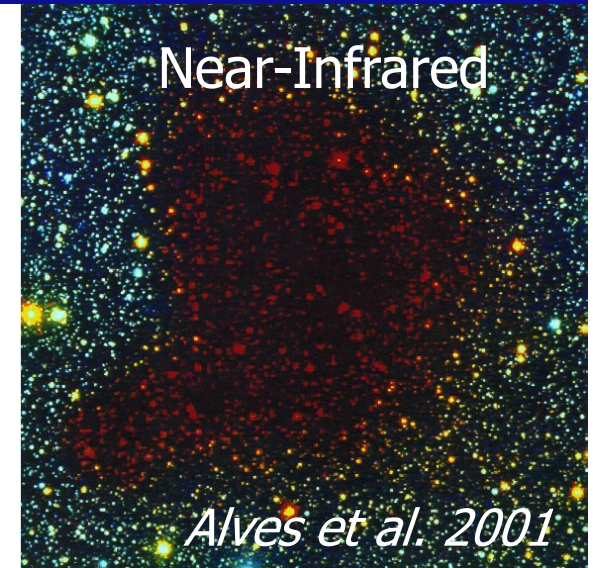
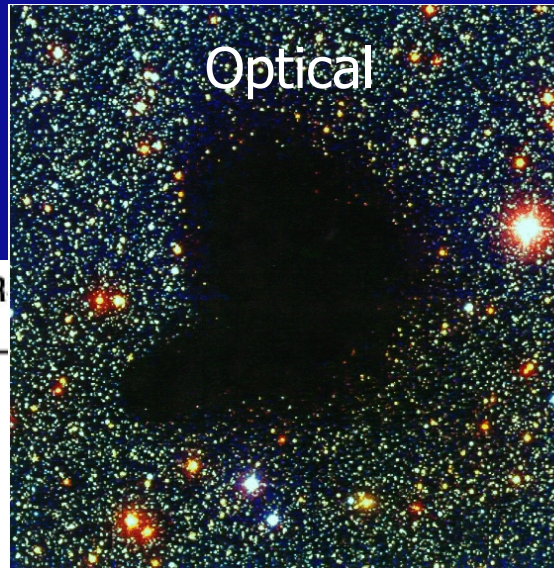
Recent work suggests

1:150 (Draine et al. 2011)

Producers:

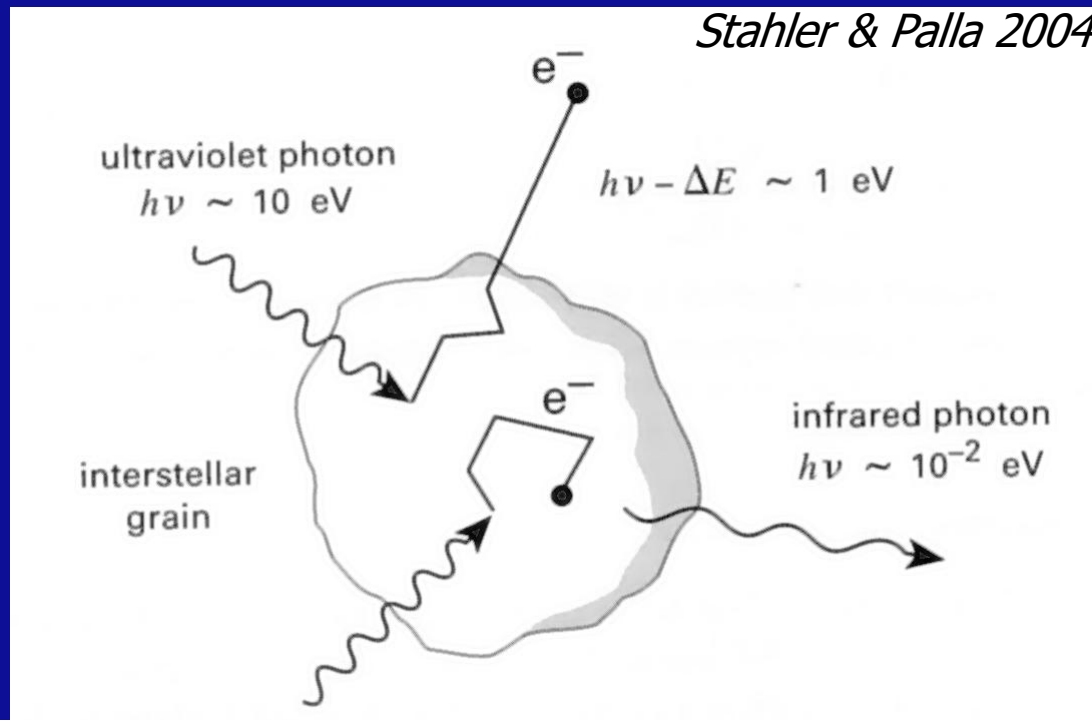
- Outer atmosph. of Red Giants, Planetary Nebulae (PN)
- Supernovae (SN)
- More recent: Dust can also form in the general interstellar medium (ISM).

Interstellar dust: Extinction at shorter wavelengths



Extinction dims *and* reddens the light

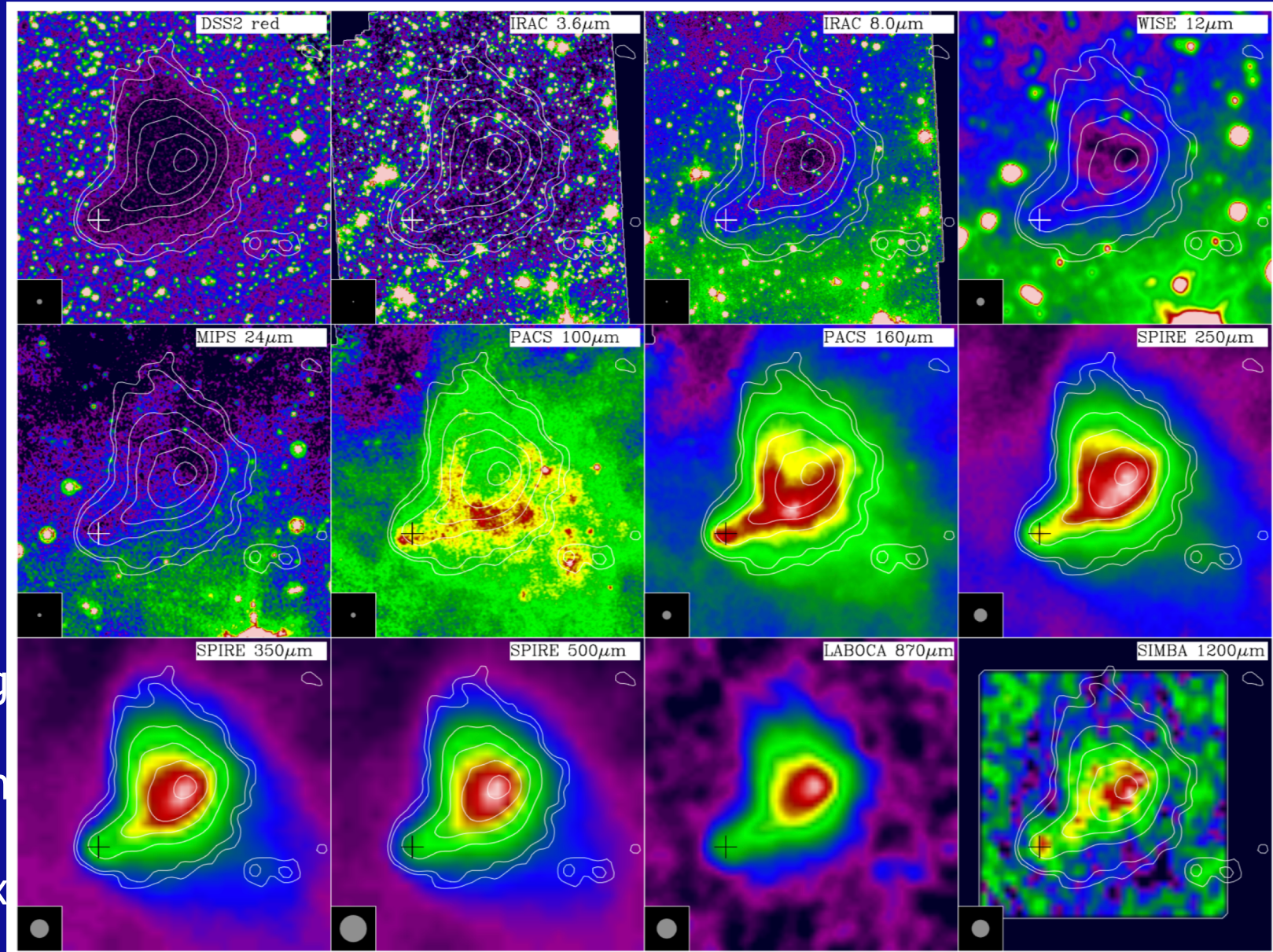
Dust action at longer wavelengths: Re-emission



Dust grain hit by UV photon:

- 1) Photoelectrical effect \rightarrow give energy to e^- \rightarrow leaves grain and heats gas.
- 2) Excites lattice vibrations \rightarrow transformed to (far)-IR photons and re-emitted.

Dust action at longer wavelengths: Re-emission



Dust g

1) Ph

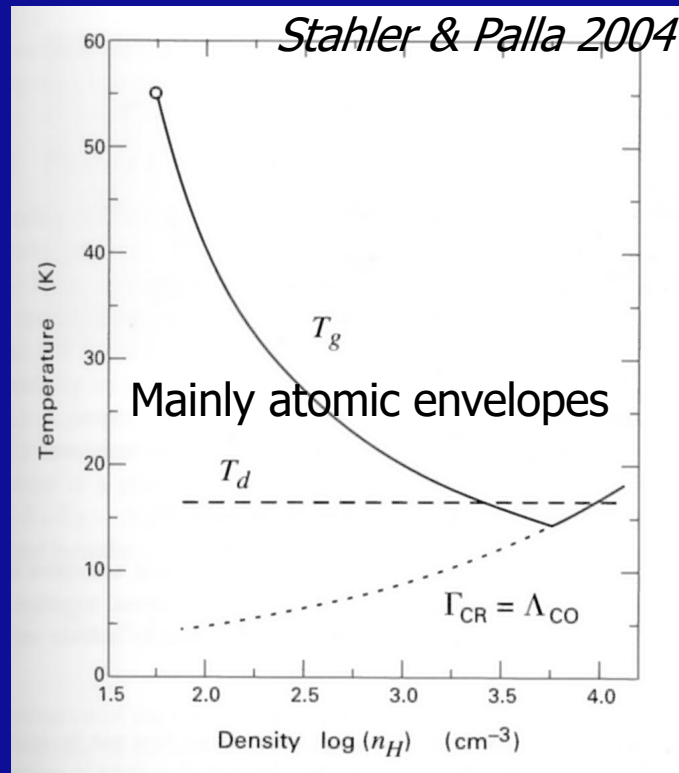
2) Ex

gas.

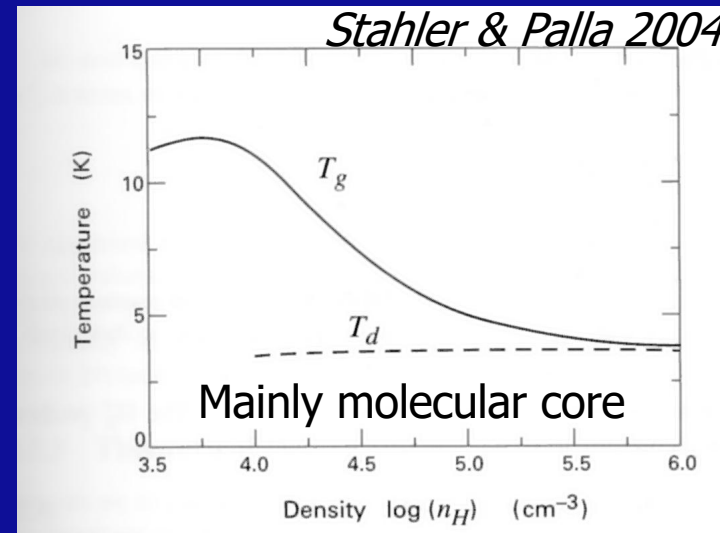
mitted.

Nielbock et al. 2012, Contours 870μm

Dust and gas coupling



Cosmic ray heating more sensitive to density than CO cooling. Hence T_g rises again.

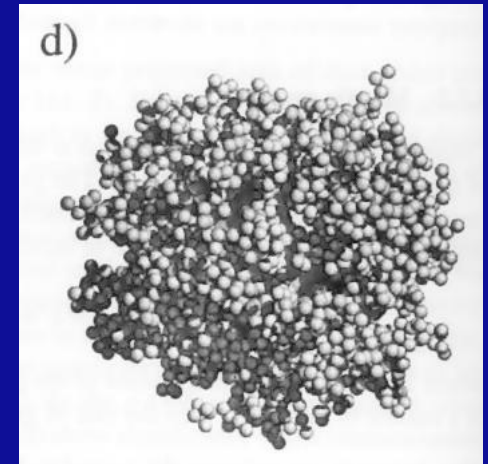
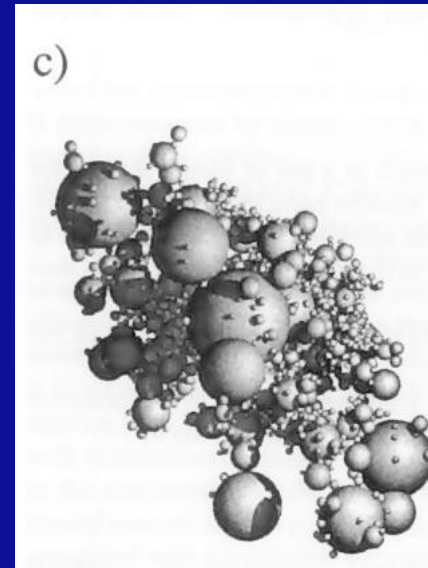
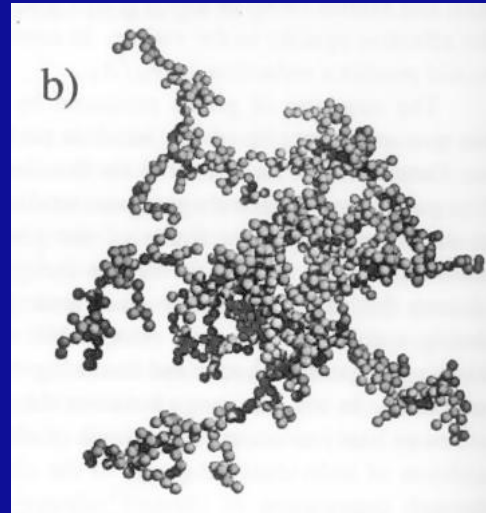
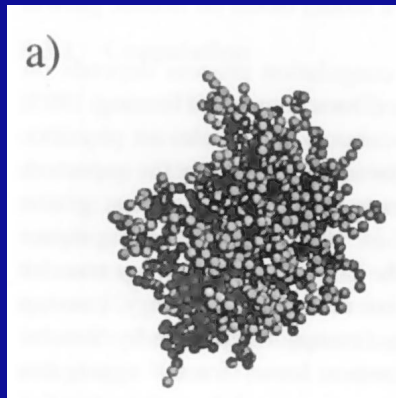


simplified model \rightarrow
lowest obs.
 $T_d \sim 7-10\text{K}$

Γ – heating rate Λ – Cooling rate

- Low densities: gas and dust de-coupled; at high densities coupled.
- Low densities gas cooling mainly CO; high densities via CO & dust.
- At very high densities gas and dust temperatures approach each other
 \rightarrow CO cooling becomes insignificant then!

Dust incarnations



Dust can grow and coagulate in very dense environments, e.g., disks.

Figures: Simulations of dust grain cluster growth for different initial parameters (gas and dust density, temperature, stickiness, grain charge, coagulation time ...).
(From Dorschner & Henning 1995)

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Physical conditions : Micro-Level

A medium in thermodynamic eq. can be described by 4 distribution laws:

1.) MAXWELL distribution of the particle velocity contributions (kinetic energy):

$$N(v;T) = 4\pi \left(\frac{m}{2kT} \right)^{3/2} v^2 \exp\left(-\frac{mv^2}{2kT} \right) \quad v : \text{particle velocities}$$

2.) BOLTZMANN distribution of the population numbers of the particle energy levels:

$$\frac{N_o}{N_u} = \frac{g_o}{g_u} \exp\left(-\frac{E_o - E_u}{kT} \right) \quad \begin{array}{l} E_{o/u} \longrightarrow \text{Energies of the upper (o) and lower (u) levels} \\ g_{o/u} \longrightarrow \text{Corresponding statistical weights} \end{array}$$

3.) PLANCK radiation law (distribution of the photon energies):

$$B_\nu = \frac{2h\nu^3 / c^2}{\exp(h\nu / kT) - 1} \quad \nu : \text{photon frequencies}$$

4.) SAHA equation (distribution of the ionisation levels in plasma):

$$\frac{N_{j+1} N_e}{N_j} = \frac{2 U_{j+1}(T)}{U_j(T)} \left(\frac{2\pi m_e kT}{h^2} \right)^{3/2} \exp(-\chi_{j,j+1} / kT)$$

N_{j+1}, N_j - Number densities of (j+1)-fold and j-fold ionised particles

N_e - electron density

$\chi_{j,j+1}$ - ionisation energy needed to get from ionisation level j to $j+1$

U_{j+1}, U_j - partition function for both states

Physical conditions : Micro-Level

Are these distribution functions valid in the ISM?

General rule: time scale for processes leading to equilibrium short compared to time scales of disturbing processes

1. Example : Collisions between H-atoms:

Consider:

$T = 100 \text{ K} \rightarrow \text{mean } v \sim 1 \text{ km/s}; \text{ cross section } \sigma = \pi R_H^2 \sim \pi (0.1 \text{ nm})^2$

Probability for collision: $P = v \sigma n_H \tau_s$

\rightarrow average time τ_s between two collision for $P=1$: $\tau_s = (v \sigma n_H)^{-1}$

\rightarrow with HI density of $1 \text{ cm}^{-3} \rightarrow \tau_s \sim 1000 \text{ yrs}$

\rightarrow short compared to most interstellar processes (except shock fronts)

\rightarrow Maxwell distribution valid, introduction of kinetic temp. T_{kin} reasonable

Physical conditions : Micro-Level

2. Example: Balance for energy level population numbers for ISM:

Correction factor to Boltzmann:
$$\frac{1}{1 + (A_{21} / (n Q_{21}))}$$

(Pure Boltzmann only if $(n Q_{21}) \gg A_{21}$)

A_{21} [s^{-1}] Einstein coefficient for
spontaneous radiative decay
 Q_{21} [$m^3 s^{-1}$] collision rate
 n [m^{-3}] number density

- In thin ISM collision rate small (Example 1) \rightarrow sub-thermal

- For dense cores: E.g. CO(1-0) at density $10^5 cm^{-3}$: $A_{21} = 7.2 \times 10^{-8} s^{-1}$,
 $Q_{21} = 3.3 \times 10^{-11} cm^3 s^{-1}$

$\rightarrow A_{21} / (n Q_{21}) \sim 0.02$

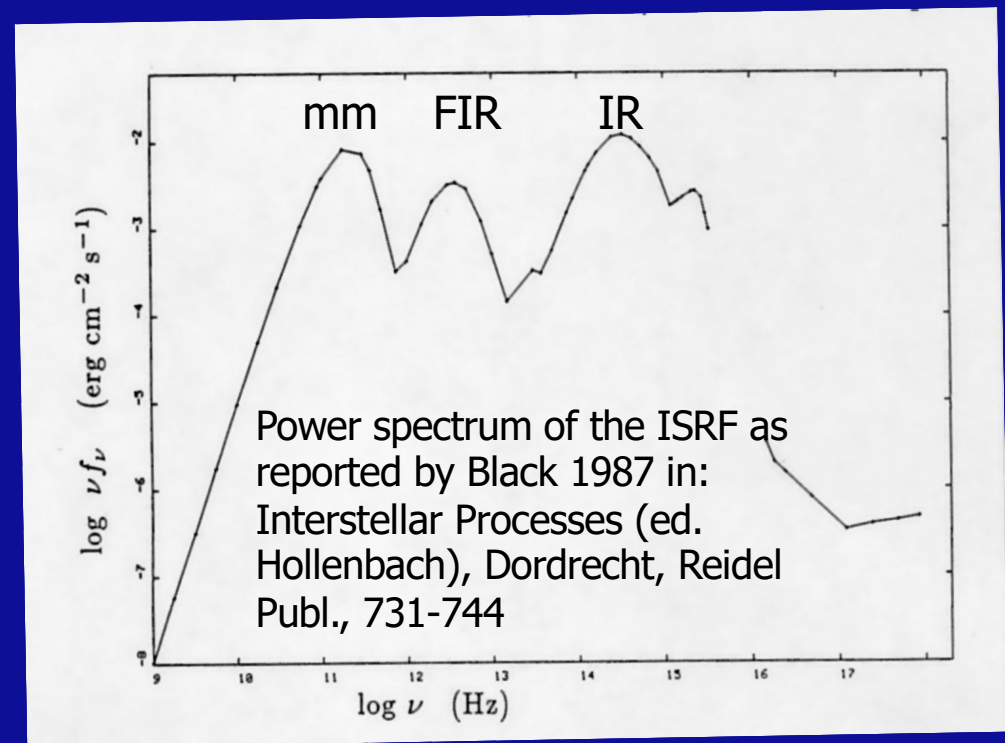
\rightarrow Boltzmann distribution valid in dense cores!

Physical conditions : Micro-Level

3. Example : Interstellar radiation field (ISRF) :

Sum of emission contributions from all emitting objects (stars, dust, gas) in the nearer and further vicinity of the gas cloud

ISRF cannot be approximated by a black body (i.e., Planck function not applicable)
ISRF hence far from thermodynamic equilibrium ...



However: Dense cores and stars can be fitted relatively well with single or multiple black body functions.

Summary

- Line profiles (thermal and kinematic broadening) and some applications
- Magnetic fields are very important but difficult to measure:
 - Zeeman effect traces **B** component along line of sight.
 - Dust polarisation traces **B** in plane of the sky.
(Other magnetic field measurements possible.)
- Masers are non-thermal processes. Good for high spatial accuracy and proper motion studies.
- Dust important from many points of view:
 - Traces warm and cold components of ISM.
 - Important coolant at high densities.
 - Traces magnetic field.
 - Chemical catalyst.
- Physical distributions and their applicability to the ISM.

Sternentstehung - Star Formation

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